CHBE320 LECTURE VIII

DYNAMIC BEHAVIORS OF CLOSED-

DOP CONTOL SYSTEMS

LOOP CONTOL SYSTEMS

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Fall 2021

Dept. of Chemical and Biological Engineering

Factor of orchobiols on the change of original CHBE320 LECTURE VIII DYNAMIC BEHAVIORS OF CLOSED-LOOP CONTOL SYSTEMS

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Road Map of the Lecture VIII

- Dynamic Behavior of Closed-loop Control System
	- Closed-loop: controller is connected and working
	- Closed-loop transfer function
		- Response of output for set point change
		- Response of output for load/disturbance change
	- Effects of each block on closed-loop system
		- Effect of controller tuning parameters

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 K_m

BLOCK DIAGRAM REPRESENTATION

• Standard block diagram of a feedback control system

- Controller TF: Controller output (P) is calculated based on error (E)
-

- Individual TF of the standard block diagram
	- TF of each block between input and output of that block
	- Each gain will have different unit.
		- [Example] Sensor TF • Input range: 0-50 l/min $\overrightarrow{N_{\text{min}}}$ $\overrightarrow{G_{\text{m}}(s)}$ $\overrightarrow{F_{\text{max}}}$ • Output range: 4-20 mA Gain, $K_m = \frac{20 - 4}{50 - 0} = 0.32$ [mA/(l/min)]

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P&ID

- Piping and Instrumentation diagram
	- A P&ID is a blueprint, or map, of a process.
	- Technicians use P&IDs the same way an architect uses blueprints.
	-
	- (Scientific Apparatus Makers Association).

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2. Abbreviations of the user's choice may be used when necessary to specify location.
3. Inaccessible (behind the panel) devices may be depicted using the same symbol but with a dashed horizontal bar.
Source: Control Engin

Shared display: usually used to indicate video display in DCS Auxiliary location: panel mounted—normally having an analog faceplate

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HCC-101: How signlay: usually used to indicate video display in DCS

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- steam header pressure be less than 6 kg/cm².

- PI-100: Pressure Indicator, 0 to 15 kg/cm², (3.18 Kg/cm²). This

instrument displays the steam pressure at the shell side of the

heat exchanger.

 PI-103: Pressure Indicator, 0 to 15 kg/cm², (10.55 Kg/cm²).

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- PI-100: Pressure Indicator, 0 to 15 kg/cm², (3.18 Kg/cm²). This
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instrument displays the steam pressure at the shell side of the

heat exchanger.

- PI-103: Pressure Indicator, 0 to 15 kg/cm², (10.55 Kg/cm²).

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PI-103: Pressure Indicator, 0 to 15 kg/cm², (10. PI-100: Pressure Indicator, 0 to 15 kg/cm², 0.18 Kg/cm²). This instrument displays the steam pressure at the shell side of the net exchanger indicator, 0 to 15 kg/cm², (10.55 Kg/cm²). The listention of the techniq exame indicator, 0 to 15 kg/cm², (3.18 Kg/cm²). This is than 11°C. $P=100$: Pressure Indicator, 0 to 15 kg/cm², (1.0.85 Kg/cm²).

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This instr PI-100: Pressure Indicator, 0 to 15 kg/cm³, (3.18 Kg/cm³). This instrument displays the steam pressure at the shell side of the conduction of the steam entering the steam entering the steam entering the steam entering **P1100:** Pressure Indicator, 0 to 15 kg/cm³, (3.18 Kg/cm³). This

lastrument displays the steam pressure at the shell side of the

P1-103: Pressure Indicator, 0 to 15 kg/cm³, (10.55 Kg/cm²).

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heat exchanger.

PI-103: Pressure Indicator, 0 to 15 kg/cm², (10.55 Kg/cm²).

This in PI-100: Pressure Indicator, 0 to 15 kg/cm², (3.18 Kg/cm³). This

heat exchanger.

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CLOSED LOOP TRANSFER FUNCTION

• Block diagram algebra

• Transfer functions of closed-loop system

 $X_2(s) = G_n(s)G_n(s)G_c(s)E(s)$ $E(s) = K_m(s)R(s) - G_m(s)Y(s)$

- $Y(s) = G_L(s)L(s) + G_p(s)G_v(s)G_c(s)E(s)$
- $Y(s) = G_L(s)L(s) + G_p(s)G_v(s)G_c(s)(K_m(s)R(s) G_m(s)Y(s))$
- $(s)G_c(s)Y(s) = G_L(s)L(s) + K_m G_p(s)G_v(s)G_c(s)R(s)$

- For set-point change (L=0)
	- $\frac{Y(s)}{R(s)} = \frac{K_m G_p(s) G_v(s) G_c(s)}{1 + G_m(s) G_p(s) G_v(s) G_c(s)}$ (s)
- For load change (R=0)

 $\frac{Y(s)}{L(s)} = \frac{G_L(s)}{1 + G_m(s)G_p(s)G_p(s)G_c(s)}$

- Open-loop transfer function (G_{Ω})
	-
	- Feedforward path: Path with no connection backward
	- Feedback path: Path with circular connection loop
	- G_{OL} : feedback loop is broken before the comparator
- Simultaneous change of set point and load 1 + ை() ()

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MASON'S RULE

• General expression for feedback control systems

 $\frac{Y}{X} = \frac{\pi_f}{1 + \pi_e}$ π_f

-
- Assume feedback loop has negative feedback.
- If it has positive feedback, $1 + \pi_e$ should be $1 \pi_e$.
- In the previous example, for set-point change

 $\pi_f = K_m G_c(s) G_v(s) G_p(s)$ $\pi_e = G_{OL}(s)$

$$
Y(s) = K_m G_p(s) G_v(s) G_c(s)
$$

$$
\frac{\overline{R(s)}}{R(s)} = \frac{m \cdot p(s) \cdot \overline{R(s)}}{1 + G_{OL}(s)}
$$

- For load change, $X = L$ $Y = Y$ $\pi_f = G_L(s)$
-

(s) $\pi_e = G_{OL}(s)$ $\frac{1}{L_1} = \frac{1}{1 + G_{m2}G_1G_{C2} + G_{m1}G_3G_2G_1G_{c2}G_{c1}}$

• Example 2

$$
-\textbf{ Inner loop:} \quad M = \frac{G_c}{1 - G_2 G_c} X_1
$$

 $-$ TF between R and Y:

$$
\pi_f = \frac{G_c}{1 - G_2 G_c} G_1 \qquad \pi_e = \frac{G_c}{1 - G_2 G_c} G_1
$$

$$
\frac{Y}{P} = \frac{G_1 G_c}{1 - G_2 G_c + G_2 G_c} = \frac{G_1 G_c}{1 + G_2 G_c + G_1 G_c}
$$

- TF between L and Y:
$$
\frac{Y}{L} = \frac{1 - G_2 G_c}{1 - G_2 G_c + G_1 G_c} = \frac{1 - G_2 G_c}{1 + (G_1 - G_2) G_c}
$$

PID CONTROLLER REVISITED

• P control

$$
p(t) = \bar{p} + K_c e(t) \xrightarrow{\hat{v}} \frac{P(s)}{E(s)} = K
$$

- PI control $\frac{1}{\tau_I} \int_0^t e(\tau) d\tau \left\{ \frac{e}{E(s)} \right\} = K_c \left(1 + \frac{1}{\tau_I s} \right) = K_c \frac{(\tau_I s + 1)}{\tau_I s}$ $\tau_{I}S^{'}$ $\tau_{I}S$ L₁ and Y:
 $\frac{C_1(1 + G_{m2}G_1G_{c2})}{G_{c2} + G_{m1}G_2G_2G_1G_{c2}G_{c1}}$

Similarly consultive state of the same control
 $\frac{8}{E(S)} = K_c$
 $+ \frac{1}{T_1}\int_0^t e(\tau) d\tau \int_0^t \frac{e}{E(S)} = K_c(1 + \frac{1}{\tau_{1S}}) = K_c \frac{(\tau_{1S} + 1)}{\tau_{1S}}$
 $+ \frac{1}{\$ nd Y:
 $+\frac{C_{m2}C_1C_{c2}}{C_{m1}C_2C_2C_1C_{c2}C_{c1}}$

Control

(5)
 $\left(\frac{s}{s}\right) = K_c$
 $\int_0^t e(\tau) d\tau \left\{ \frac{e^{-\beta t}S}{E(s)} = K_c(1 + \frac{1}{\tau_1 s}) = K_c \frac{(\tau_1 s + 1)}{\tau_1 s} \right\}$
 $\int_0^t e(\tau) d\tau + \tau_0 \frac{de}{dt} \frac{e^{-\beta t}}{E(s)}$
 $\frac{1}{\tau_1 s} + \tau_0 s$
- PID control

$$
\pi_{e} = G_{0L}(s)
$$
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– Ideal PID controller: Physically unrealizable – Modified form has to be used.

• Nonideal PID controller

– Interacting type

$$
G_c^*(s) = K_c^* \frac{(\tau_l^* s + 1)}{\tau_l^* s} \frac{(\tau_D^* s + 1)}{(\beta \tau_D^* s + 1)} \underbrace{(0 < \beta \ll 1)}_{\text{Filtering effect}}
$$

– Comparison with ideal PID except filter

\n- \n**Nonideal PID controller**\n
	\n- \n
	$$
	c(t) = R_c \frac{(r_0 + 1)}{(r_0 + 1)} \frac{(r_0 + 1)}{(r_0 + r_0 + r_0)}
	$$
	\n
	\n- \n $c(t) = R_c \frac{(r_0 + 1) (r_0 + 1)}{(r_0 + r_0 + r_0)}$ \n
	\n- \n $c(t) = R_c \frac{(r_0 + 1) (r_0 + 1)}{(r_0 + r_0)}$ \n
	\n- \n $c(t) = R_c \frac{(r_0 + 1)}{(r_0 + r_0)}$ \n
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	\n- \n $c(t) = R_c \frac{(r_0 + 1) (r_0 + 1)}{(r_0 + r_0)}$ \n
	\n- \n $c(t) = R_c \frac{(r_0 + 1) (r_0 + 1)}{(r_0 + r_0)}$ \n
	\n- \n $c(t) = R_c \frac{(r_0 + 1) (r_0 + 1)}{(r_0 + r_0)}$ \n
	\n- \n $c(t) = R_c \frac{(r_0 + 1) (r_0 + 1)}{(r_0 + r_0)}$ \n
	\n- \n $$

- provides the prefiltering of the error signal.
- Generally, $\tau_l \ge \tau_D$ and typically $\tau_l \approx 4\tau_D$.
- In this form, $\tau_I \ge \tau_D$ is satisfied automatically since algebraic mean is not less than logarithm mean.

• Block diagram of PID controller

- $\frac{(\tau_i^* + \tau_p^*)}{(\tau_i^* + \tau_p^*)^s}$ > $\frac{(\tau_i^* + \tau_p^*)}{s}$ Removal of derivative kick (PI-D controller)
	-

$$
P(s) = K_c \left[\frac{1}{\tau_I s} R(s) - \frac{(\tau_I s + 1)}{\tau_I s} \frac{(\tau_D s + 1)}{(\beta \tau_D s + 1)} Y(s) \right]
$$

- Other variations of PID controller
	- Gain scheduling : modifying proportional gain

 $K_c^{GS} = K_c K^{GS}$ GS and S^{\dagger} are the set of \mathcal{S} and \mathcal{S} are the set of \mathcal

where
$$
\alpha
$$

$$
1. K^{GS} = \begin{cases} K_{Gap} & \text{for (lower gap)} \le e(t) \le \text{(upper gap)}\\ 1 & \text{otherwise} \end{cases}
$$

 $2. K^{GS} = 1 + C_{GS} |e(t)|$

- $3. K^{GS}$ is decided based on some strategy
- Nonlinear PID controller
	- Replace $e(t)$ with $e(t) | e(t) |$.
	- Sign of error will be preserved but small error gets smaller and larger error gets larger.
	- It imposes less action for a small error.

DIGITAL PID CONTROLLER

- Discrete time system
	- Measurements and actions are taken at every sampling interval.
	- An action will be hold during the sampling interval.
- Digital PID controller

\n- \nThese types are physically realizable and the modification provides the preflucting of the error signal.\n
	\n- Geversal,
	$$
	i = 5
	$$
	 is a straightforwardly used.
	\n- Cheterically, $i = 5$ is a straightforwardly used.
	\n\n
\n- \nSubstituting the same as a second.

\n
\n- \nOther variations of PID controller\n
	\n- $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z)} \right)$
	\n- $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
	\n\n
\n- \nOther variations of PID controller\n
	\n- Caas bine
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\n- \nOther variations of PID controller\n
	\n- $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
	\n- Discrete time system\n
		\n- $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
		\n- Discrete time system\n
			\n- Exes $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
			\n- Exes $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
			\n\n
		\n- \nNotice that the process of the number of possible data for each other.
		
		\n
		\n- \nNonlinear PD controller\n
			\n- $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
			\n\n
		\n- \nNonlinear PD controller\n
			\n- $r(z) = K \left(\frac{1}{16} R(z) - \frac{1}{\sqrt{16} R(z+1)} \right)$
			\n- Discrete time system\n
				\n

- Most modern PID controllers are manufactured in digital form with short sampling time.
- If the sampling time is small, there is not much difference between continuous and digital forms.
- Velocity form does not have reset windup problem because there is no summation (integration).
- Other approximation such as trapezoidal rule and etc. can be used to enhance the accuracy. But the improvement is not substantial.

Most modern PID controls are manufactured in digital form

\nWith short sampling time is small, there is not much difference

\nIt the sampling time is small, there is not much difference

\nVector form does not have reset window and great, and the improvement is not

\nOrder approximation (integrating in the system,
$$
z
$$
 and z are

\nOther approximation (integrating in the system, z and z are

\nwhich is determined by the z and z are

\nincomplete time system, z and z are

\nindependent, z and z are

\n

counterpart of Laplace transform. (out of scope of this lecture) velocity form does not have reset what public there is no summation (integration).

there is no summation (integration).

Once a strapezional rule and etc. can be

used to enhance the aceracy. But the improvement is not

• P control for set-point change (L=0)

 $G_c(s) = K_c$ (K_c>0)

$$
G_{CL}(s) = \frac{H(s)}{R(s)} = \frac{K_c K_p/(\tau s + 1)}{1 + K_c K_p/(\tau s + 1)} = \frac{K_c K_p/(1 + K_c K_p)}{(\tau/(1 + K_c K_p))s + 1}
$$
 (closed-loop TF)

– Closed-loop gain and time constant

$$
K_{CL} = \frac{K_c K_p}{(1 + K_c K_p)}, \qquad \tau_{CL} = \frac{\tau}{(1 + K_c K_p)}
$$

– Steady-state behavior of closed-loop system

$$
_{CL} = \frac{K_c K_p}{(1 + K_c K_p)} < 1, \qquad \lim_{K_c \to \infty} G_{CL} = 1 \ \ (H(s) = R(s), \text{ no offset})
$$

$\frac{de(t_0)}{dt} = \frac{e(t_m) + \frac{\sum x}{2}(t_{m-1}) - 3e(t_{m-2}) - e(t_{m-2})}{2t}$	(Interpolation formula)		
• For discrete time system, z-transform is the \n <th>Example 4</th> \n <th>Example 4</th> \n	Example 4	Example 4	
• Confinert of Laplace transform. (out of scope of this lecture)	$h(s) = \frac{hc(s_0)}{1 + c(c_0)} = 1$		
• Proof of the function	$h(s) = \frac{hc(s_0)}{1 + c(c_0)} = 1$		
• Proof of the function	$h(s) = \frac{hc(s_0)}{1 + c(c_0)} = 1$		
• Proof of the equation	$h(s) = \frac{hc(s_0)}{1 + c(c_0)}$	$h(s) = \frac{hc(s_0)}{1 + c(c_0)}$	
• Proof of the equation	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	
• Proof of the equation	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	
• Proof of the equation	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	
• Proof of the equation	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$	$h(s) = \frac{hc(s_0)}{1 + c(s_0)}$
• Proof of the equation			

• P control for load change (R=0)

 $G_c(s) = K_c$ (K_c>0)

$$
G_{CL}(s) = \frac{H(s)}{L(s)} = \frac{K_p/(ts+1)}{1 + K_c K_p/(ts+1)} = \frac{K_p/(1 + K_c K_p)}{(\tau/(1 + K_c K_p))s + 1}
$$
 (closed-loop TF)

– Closed-loop gain and time constant

$$
K_{CL} = \frac{K_p}{(1 + K_c K_p)}, \qquad \tau_{CL} = \frac{\tau}{(1 + K_c K_p)}
$$

– Steady-state behavior of closed-loop system

$$
\frac{K_p}{+K_c K_p} > 0, \qquad \lim_{K_c \to \infty} G_{CL} = 0 \text{ (disturbance is compensated)}
$$

of
\n
$$
G_{\nu}(s) = G_{\nu}(s) = 1
$$

\n $H(s) = \frac{G_{\nu}G_{\nu}}{1 + G_{\nu}G_{\rho}}R(s) + \frac{G_{\nu}}{1 + G_{\nu}G_{\rho}}L(s)$
\nRiv 8-25
\nCHBE320 Process Pynames and Control
\nFor all intervals of B-26
\n $G_{\nu}(s) = K_{\nu}(K_{\nu} > 0)$
\n $G_{\nu}(s) = K_{\nu}(K_{\nu} > 0)$
\n $G_{\nu}(s) = \frac{H(s)}{1 + K_{\nu}(K_{\nu}/(ts + 1))} = \frac{K_{\nu}/(1 + K_{\nu}(K_{\nu})}{(T/(1 + K_{\nu}(K_{\nu})))s + 1}$ (closed-loop TF)
\n- Closed-loop gain and time constant
\n $K_{\nu} = \frac{K_{\nu}}{(1 + K_{\nu}K_{\nu})} \times \tau_{\nu} = \frac{1}{(1 + K_{\nu}(K_{\nu}))}$
\n- Steady-state behavior of closed-loop system
\n $K_{\nu} = \frac{K_{\nu}}{(1 + K_{\nu}(K_{\nu})} > 0$, $\lim_{K_{\nu} \to \infty} G_{\nu} = 0$ (disturbance is compensated)
\n $\frac{1}{1 + K_{\nu}(K_{\nu})}$
\n= Steady-state derivative of fixed - 100 p system
\nInteg product of size 0 - h(∞) = 0 - $K_{\nu} = -\frac{K_{\nu}}{1 + K_{\nu}(K_{\nu})}$
\n $\frac{1}{1 + K_{\nu}(K_{\nu})}$
\n \frac

 K_p

• PI control for load change (R=0)

 $G_c(s) = K_c(\tau_i s + 1)/\tau_i s$ (K_c>0)

Pl control for load change (R=0)

\n
$$
G_{c}(s) = K_{c}(\tau_{i}s + 1)/\tau_{i}s \quad (K_{c} > 0)
$$
\n
$$
G_{cL}(s) = \frac{K_{p}/(rs + 1)}{1 + K_{c}K_{p}(\tau_{i}s + 1)/(rs + 1)/\tau_{i}s} = \frac{K_{p}\tau_{i}s}{\tau_{i}rs^{2} + \tau_{i}(1 + K_{c}K_{p})s + K_{c}K_{p}}
$$
\n**Closed-loop gain, time constant, damping coefficient**

\n
$$
K_{num} = \frac{\tau_{t}}{K_{c}}, \qquad \tau_{cL} = \sqrt{\frac{\tau_{t}}{K_{c}K_{p}}}, \qquad \zeta_{cL} = \frac{1}{2} \frac{(1 + K_{c}K_{p})}{\sqrt{K_{c}K_{p}}} \sqrt{\tau_{i}/\tau}
$$
\n**Steady-state behavior of closed-loop system**

\nIm *G_{cL}(s) = 0* (disturbance is compensated for all cases)

\n**Usual effect**

\n**Usual effect**

\n**Usual effect**

\n
$$
G_{cL}(s) = 0
$$
\n**Usual effect**

\

– Closed-loop gain, time constant, damping coefficient

$$
K_{num} = \frac{\tau_I}{K_c}, \qquad \tau_{CL} = \sqrt{\frac{\tau \tau_I}{K_c K_p}}, \qquad \zeta_{CL} = \frac{1}{2} \frac{(1 + K_c K_p)}{\sqrt{K_c K_p}} \sqrt{\tau_I/\tau}
$$

– Steady-state behavior of closed-loop system

- $-$ As K_c increases, faster compensation of disturbance and less oscillatory response can be achieved.
- $-$ As τ_I decreases, faster compensation of disturbance and less overshooting response can be achieved.
- However, usually the response gets more oscillation as K_c increases or τ_I decreases. \Rightarrow very unusual!!
- **Control for load change (R=0)**
 $S = K_c(r_3 + 1)/r_1s$ ($K_c > 0$)
 $K_c(r_3 + 1)/r_1s$ ($K_c > 0$)
 $K_c r_3 = \frac{K_c}{r_1r_2r_3}$ (a) $\frac{K_{\gamma}T_{\gamma}S}{\sqrt{K_{\gamma}}}$

(1 + $K_{\gamma}K_{\gamma}$) s + $K_{\gamma}K_{\gamma}$

(1 + $K_{\gamma}K_{\gamma}$) $\sqrt{\tau_{\gamma}\tau_{\gamma}}$

(1 + – If there is small lag in sensor/actuator TF or time delay in As K_c increases, faster compensation of disturbance and less
oscillatory response can be achieved.
As τ_l decreases, faster compensation of disturbance and less
overshooting response can be achieved.
However, usually anomalous results will not occur. These results is only possible for very simple process such as 1st order system. For vector and the therepose gas to suppressed on the state of the series of the increase gets more oscillation as K_c linewere, usuall! If there is small lag in sensor/actuator TF or time delay in firtere is small lag i However, usually the response gets more oscillation as K_c

increases or τ_i decreases. \Rightarrow very unusual!!

If there is small lag in sensor/actuator TF or time delay in

a momalous results will not occur. These result stany the response gets more than the other of the behavior of τ_{f} decreases. \Rightarrow very nuisalal!!

If τ_{f} decreases. \Rightarrow very nuisalal!!

In the system becomes higher order and these

results will not occur. The bovects, assume treporates as the contract to the close of the close of the control and particulator TF or time delay in

the check samellage in ensemble the order and these the control of the close of the particulator
	- Usual effect of PID tuning parameters
		- As K_c increases, the response will be faster, more oscillatory.
		- As τ_I decreases, the response will be faster, more oscillatory.
		- As τ_D increases, the response will be faster, less oscillatory when there is no noise.

• P control for set-point change (L=0)

$G_c(s) = K_c$ (K_c<0)

$$
G_{CL}(s) = \frac{H(s)}{R(s)} = \frac{K_c/(-As)}{1 + K_c/(-As)} = \frac{1}{(-A/K_c)s + 1}
$$
 (closed-loop TF)

– Closed-loop gain and time constant

– Steady-state behavior of closed-loop system

- even with P control for the set point change.
- + - As K, increases, the response will be faster, more oscillatory.

As Trdecreases, the response will be faster, less oscillatory when

there is no noise.

 29 Process Dynamics and Control

 29 Process Dynamics and – Even though there are other dynamics in sensor or actuator, the offset will not be shown with P control for integrating systems.
	- Higher controller gain results faster closed-loop response: shorter time constant

CLOSED-LOOP RESPONSE OF INTEGRATING SYSTEM

• P control for load change (R=0)

 $G_c(s) = K_c$ (K_c <0)

control for load change (R=0)

(s) = K_c (K_c <0)
 $L(s) = \frac{H(s)}{L(s)} = \frac{1/(As)}{1 + K_c/(-As)} = \frac{-1/K_c}{(-A/K_c)s + 1}$ (closed-loop TF)
 Closed-loop gain and time constant
 $K_{CL} = (-1/K_c)$, $\tau_{CL} = -A/K_c$
 Steedy-state hebevior of closed Properties Control for load change (R=0)
 $G_c(s) = K_c$ ($K_c < 0$)
 $G_{C_L}(s) = \frac{H(s)}{L(s)} = \frac{1/(ds)}{1 + K_c/(- As)} = \frac{-1/K_c}{(-A/K_c)s + 1}$ (closed-loop TF)

- Closed-loop gain and time constant
 $K_{CL} = (-1/K_c)$, $\tau_{CL} = -A/K_c$

- Steady-state be $\frac{H(s)}{L(s)} = \frac{1/(As)}{1 + K_c/(-As)} = \frac{-1/K_c}{(-A/K_c)s + 1}$ (closed-loop TF) $(-A/K_c)s + 1$ (where $\{x \in F : r \}$)

– Closed-loop gain and time constant

$$
K_{CL} = (-1/K_c), \qquad \tau_{CL} = -A/K
$$

– Steady-state behavior of closed-loop system
 $K_{CL} = \lim_{\epsilon \to 0} G_{CL}(s) = 1$ ($H(s) = R(s)$, no offset)

1 + 1 (− →ஶ

• P control for load change (R=0)
 $C_6(s) = K_6(s) - K_7(s)(s)$
 $C_6(s) = K_8(s) - K_9(s) - K_1(s)$
 $C_7(s) = \frac{F(s)}{4(s)} = \frac{F(s)}{4(s)(-4s)} = \frac{-1/8s}{\sqrt{4(k)s^2 + 1}}$ (dosel-boy Ff)

- Clocod-loop pain and the constant
 $K_7 = (-1/8s)$
 $K_8 = (-1/8s)$
 – Higher controller gain results faster closed-loop response: shorter time constant Control for load change (R=0)
 $s_i = k_c$ ($K_c < 0$)
 $\frac{H(s)}{L(s)} = \frac{1/(6s)}{1 + K_c/(s + 1)/(-4s)} = \frac{-1/K_c}{(-A/K_c)s + 1}$ (closed-loop TF)
 $C_{G}(s) = K_c(r_s s + 1)/r_s$ ($K_c = 1,$ $K_{G, t} = -1/K_c$)

Closed-loop gain and time constant
 $K_{G, t} = (-1/K_c)$
 ntrol for load change (R=0)

= K_c ($K_c < 0$)

= $\frac{H(s)}{L(s)} = \frac{11/As}{1 + K_c I(-As)} = \frac{-1/K_c}{(-A/K_c)s + 1}$ (closed-loop TF)

osed-loop gain and time constant

= $(-1/K_c)$
 $\pi_{cL} = -A/K_c$
 $K_{cL} = 1$
 $K_{cL} = \frac{1}{1 + K_c I(-As)}$
 $\pi_{cL} = -A$) > 0, lim **19 (R=0)**
 \bullet **PI control for s:**
 $\frac{-1/K_c}{-A/K_c}$ (closed-loop TF)
 $\frac{-1/K_c}{-A/K_c}$) \cdot (closed-loop TF)
 $\frac{C_{C}(S)}{1 + K_c(r_S + 1)}/r_s$

constant
 K_c
 Exaction and the subset of the subset of the subset of the set of t

• PI control for set-point change (L=0)

 $G_c(s) = K_c(\tau_1 s + 1)/\tau_1 s$ (K_c<0)

 $K_c(\tau_I s + 1)/(-As)/\tau_I s$ ($\tau_I s + 1$) (τ_{15} + 1)
 $(\tau_{15}$ + 1)
 $(\tau_{16})s^2 + \tau_{15}$ + 1

mping coefficient
 $\sqrt{-\frac{\tau_1 K_c}{A}}$

p system

fset) $(-\tau_I A/K_c) s^2 + \tau_I s + 1$

– Closed-loop gain, time constant, damping coefficient

Pl control for set-point change (L=0)

\n
$$
G_{c}(s) = K_{c}(\tau_{1}s + 1)/\tau_{1}s \quad (K_{c}<0)
$$
\n
$$
G_{cL}(s) = \frac{K_{c}(\tau_{1}s + 1)/(-As)/\tau_{1}s}{1 + K_{c}(\tau_{1}s + 1)/(-As)/\tau_{1}s} = \frac{(\tau_{1}s + 1)}{(-\tau_{1}A/K_{c})s^{2} + \tau_{1}s + 1}
$$
\n- Closed-loop gain, time constant, damping coefficient

\n
$$
K_{cL} = 1, \qquad \tau_{cL} = \sqrt{-\frac{\tau_{1}A}{K_{c}}}, \qquad \zeta_{cL} = \frac{1}{2} \sqrt{-\frac{\tau_{1}K_{c}}{A}}
$$
\n- Steady-state behavior of closed-loop system

\n
$$
K_{cL} = \lim_{s \to 0} G_{cL}(s) = 1 \quad (H(s) = R(s), \text{ no offset})
$$

– Steady-state behavior of closed-loop system

- $-$ As (- K_c) increases, closed-loop time constant gets smaller (faster response) and less oscillatory response can be achieved. **control for set-point change (L=0)**
 $= K_c(\tau_1 s + 1)/\tau_1 s$ ($K_c < 0$)
 s) $= \frac{K_c(\tau_1 s + 1)/(-As)/\tau_1 s}{1 + K_c(\tau_1 s + 1)/(-As)/\tau_1 s} = \frac{(\tau_1 s + 1)}{(-\tau_1 A/K_c)s^2 + \tau_1 s + 1}$
 Closed-loop gain, time constant, damping coefficient
 Close nt change (L=0)
 $\frac{r_5}{r_{\lfloor r_5\rfloor}} = \frac{(r_5+1)}{(-r_4A/K_c)s^2 + r_5s + 1}$

constant, damping coefficient
 $\frac{\zeta_{CL}}{r} = \frac{1}{2} \sqrt{\frac{r_1K_c}{A}}$
 constant composite that is the set of the set of the set of the set of the set of
- $-$ As τ_I decreases, closed-loop time constant gets smaller (faster response) and more oscillatory response can be achieved. control for set-point change (L=0)

= $K_c(\tau_1 s + 1)/\tau_1 s$ ($K_c < 0$)
 s) = $\frac{K_c(\tau_1 s + 1)/(-As)/\tau_1 s}{\tau_1 + K_c(\tau_1 s + 1)} = \frac{(\tau_1 s/3)^{2s^2} + \tau_1 s + 1}{(\tau_1 s/16)^{2s^2} + \tau_1 s + 1}$

Closed-loop gain, time constant, damping coefficie
-
- Pl control for set-point change (L=0)
 $G_n(s) = K_n(r_s + 1)/r_s(s)$ $(K_n \infty)$
 $G_{GL}(s) = \frac{K_n(r_s + 1)}{1 + K_n(r_s + 1)/(-As)/r_s s} = \frac{(r_s s + 1)}{(-A/K_s)s^2 + r_s s + 1}$

 Closed-loop gain, time constant, damaing coefficient
 $K_{ex} = \lim_{s \to a} G_{ex}$ $K_{cs} = \$ **Pl control for set-point change (L=0)**
 $G_c(s) = K_c(r_s s + 1)/r_s s$ $(K_c s + 0)/(-A s)/r_s s$ $= \frac{(r_s s + 1)}{(r_s k / k_s s + 1)(-A s)/k_s s + r_s s + 1)}$
 $-$ Closed-loop gain, time constant, damping coefficient
 $K_{cL} = 1$, $\tau_{cL} = \sqrt{\frac{r_s A}{k_c}}$, $C_{cL} = \$ different. Thus, rules of thumb cannot be applied blindly.