
Membrane Contactors for Stripping of Ammonia from Aqueous Solutions

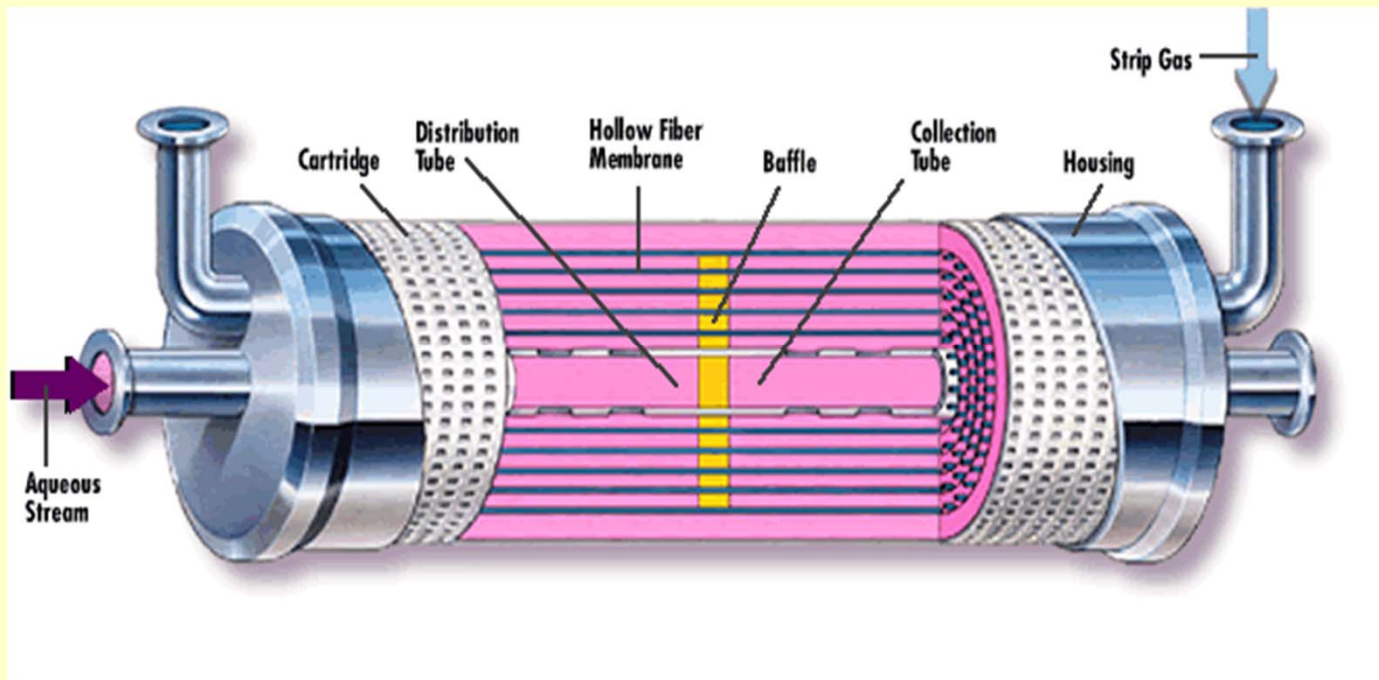
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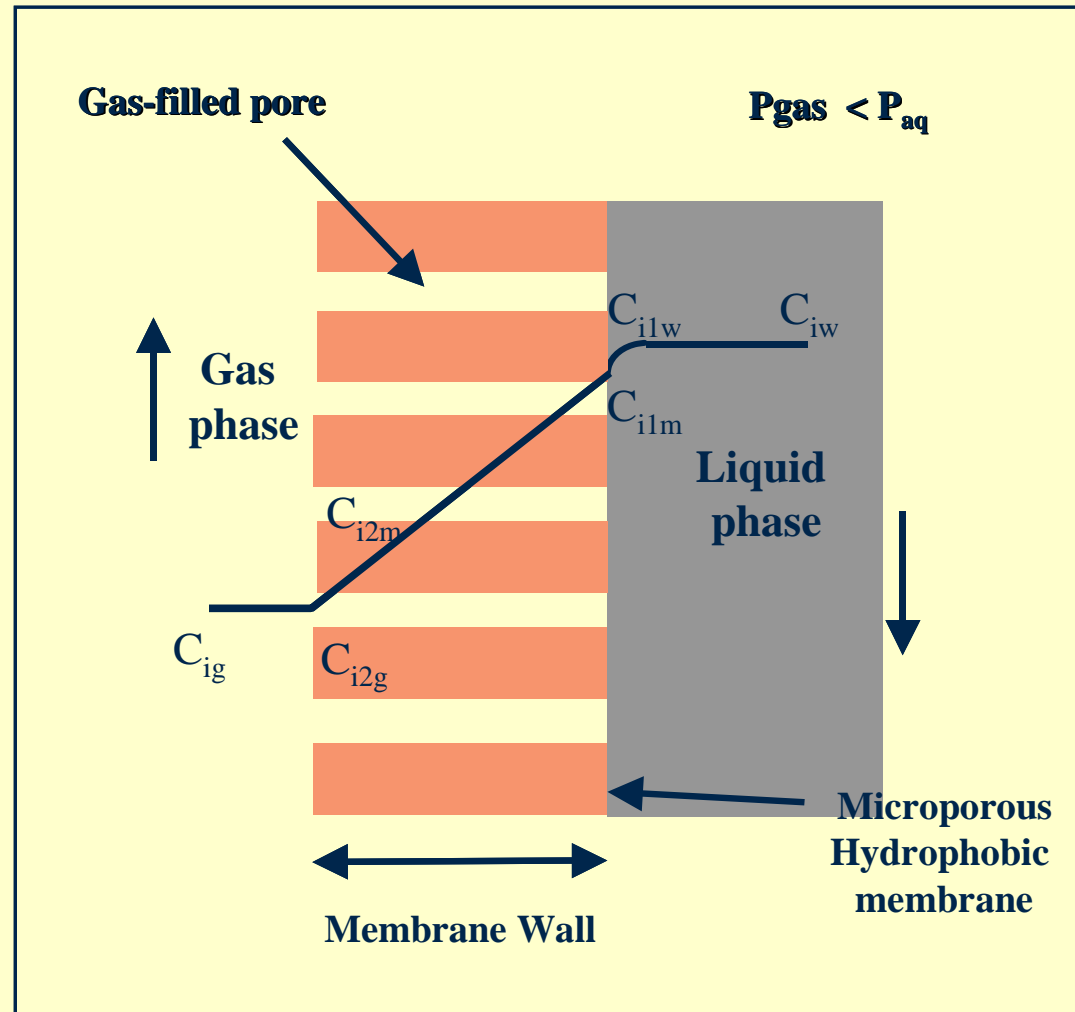
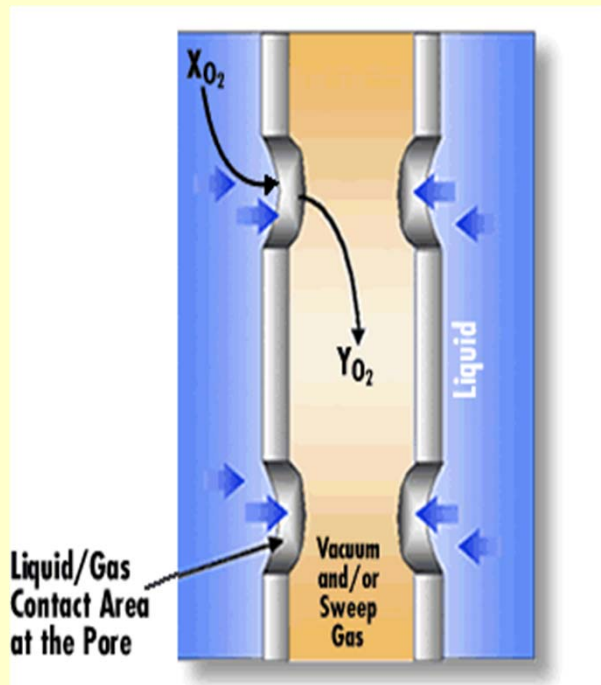
Scheme

- Introduction
- Mass transfer for Membrane Contactor
- Equilibrium & Henry's Constant
- Mass transfer coefficient correlation
- Application of Lee et al. model
- Extension of Lee et al. model
- Conclusion

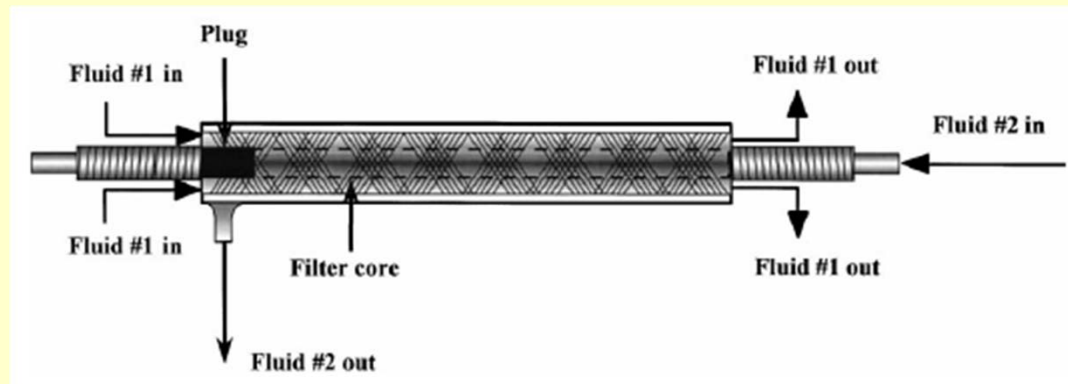
Hollow Fiber Membrane contactor?



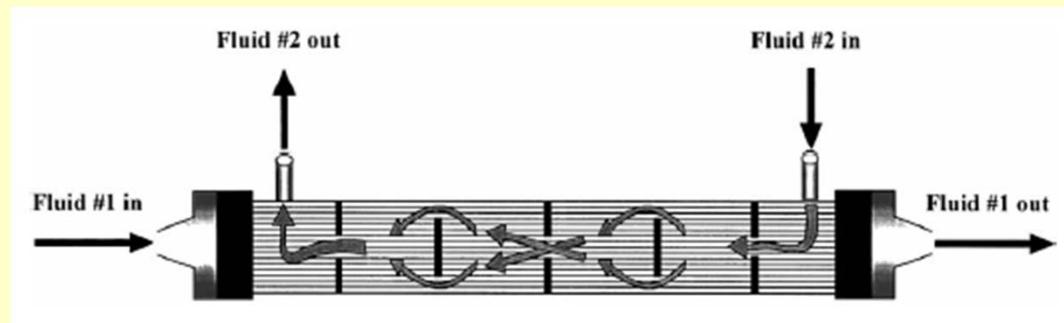
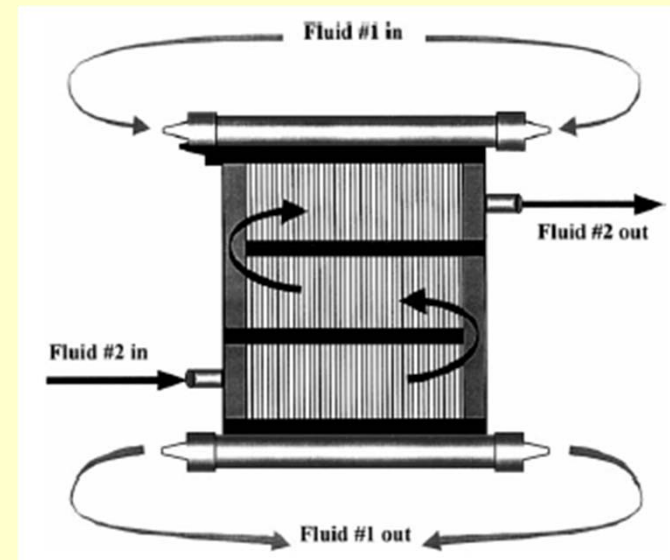
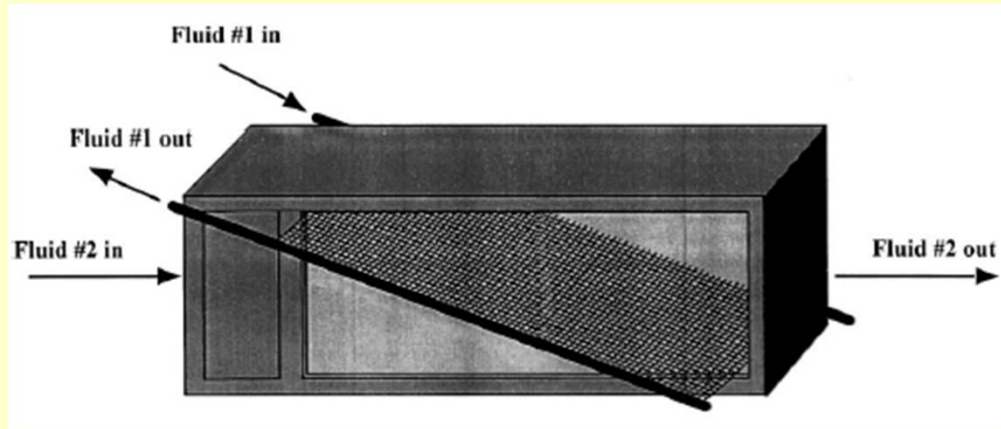
Hollow Fiber Membrane contactor?



Types of Hollow Fiber Membrane



Types of Hollow Fiber Membrane



Introduction

- **Membrane Contactor Process**

- ▶ **A new way to accomplish separation process**

- Liquid/liquid extraction
- Gas absorption/stripping

- ▶ **Applications**

- Fermentation
- Pharmaceuticals
- Wastewater treatment
- Chiral separations
- Semiconductor Manufacturing
- Metal ion extraction
- VOC removal from wastewater etc.

Introduction

- **Membrane Contactor Process**

- ▶ **Advantages**

- Large extensive interfacial area of mass transfer
1/30 in gas absorber, 1/500 in L/L extraction column
- No flooding, no unloading
- The possibility of realization of extreme phase ratios
- Nondispersive phase contact avoiding entrainment
- Direct scale-up

- ▶ **Disadvantages**

- Significant membrane resistances
- Limited applications : weak for organic solvents, solids
- Expensive

Membrane Contactor

- **Qi and Cussler (1985a,b)**
 - ▶ Mass transfer in gas absorption
 - ▶ Mechanism
 - Mass transfer out of feed solution
 - Diffusion across the membrane
 - Mass transfer into the product solution
- **Yang and Cussler (1986)**
 - ▶ Mass transfer in aqueous deaeration and CO₂ absorption
 - ▶ Basis for designing hollow fiber membrane module
- **Semmens et al. (1990)**
 - ▶ Experiment for ammonia removal with a parallel hollow fiber module
 - ▶ Correlation for mass transfer coefficients

Membrane Contactor

- **Dahuron and Cussler (1988)**
 - ▶ Protein extraction with hollow fiber contactors
 - ▶ Faster than conventional extraction equipment
- **Prasad and Sirkir (1988)**
 - ▶ Dispersion-free solvent extraction with hydrophobic and hydrophilic micoporous hollow fiber membrane module
 - ▶ Overall mass transfer coefficient characterized with distribution coefficients and interfacial tensions
- **Wang and Cussler (1993)**
 - ▶ Performance of baffled hollow fiber fabric module
 - ▶ Better performance than most conventional module geometries

Membrane Contactor

- **Sengupta et al.(1998)**
 - ▶ Empirical correlation of mass transfer for transverse flow
 - ▶ Removal of dissolved oxygen from water with excess sweep gas
- **Schöner et al.(1998)**
 - ▶ Correlation for calculation the shell side mass transfer coefficient in cross flow
 - ▶ Application to extraction
- **Gabelman and Hwang (1999)**
 - ▶ General review of membrane contactors
 - ▶ Summary for mass transfer coefficient correlation
 - In tube side : reasonable accuracy
 - In shell side : more difficult to determine

Membrane Contactor

Analysis of Membrane Contactor

Key information : Mass Transfer, Equilibrium,
Breakthrough pressure

- **Mass transfer : mass balance**

- ▶ **Mass transfer coefficient from experimental data**
- ▶ **Parallel hollow fiber**
 - **Countercurrent : Qi and Cussler (1985a), Sirkar (1992)**
 - **Cocurrent : Qi and Cussler (1985b)**
- ▶ **Baffled hollow fiber : cross flow**
 - **Sengupta et al. (1998), Schöner et al.(1998)**

Membrane Contactor

- **Correlation for mass transfer coefficients**
 - ▶ **Dimensionless group : Re , Sc , Sh**

- **Equilibrium at the gas-liquid interface**
 - ▶ **Henry's law**
 - From vapor-liquid equilibrium data
 - Henry's constant estimated for processes involving stripping fluids

In present work

- **Application to ammonia stripping**
 - ▶ One baffled commercial hollow fiber membrane contactor from Liqui-Cel®
- **Analysis of mass transfer in shell side according to the flow pattern**
 - ▶ Parallel flow and cross flow
- **Equilibrium : Henry's constant**
 - ▶ Ammonia stripping process
 - NaOH added : Ammonia molecule in $\text{pH} > 11$
 - $\text{NH}_3\text{-H}_2\text{O-NaOH}$ VLE data needed
- **Experiment : $\text{NH}_3\text{-H}_2\text{O-NaOH}$ VLE**
 - ▶ A modified static measurement

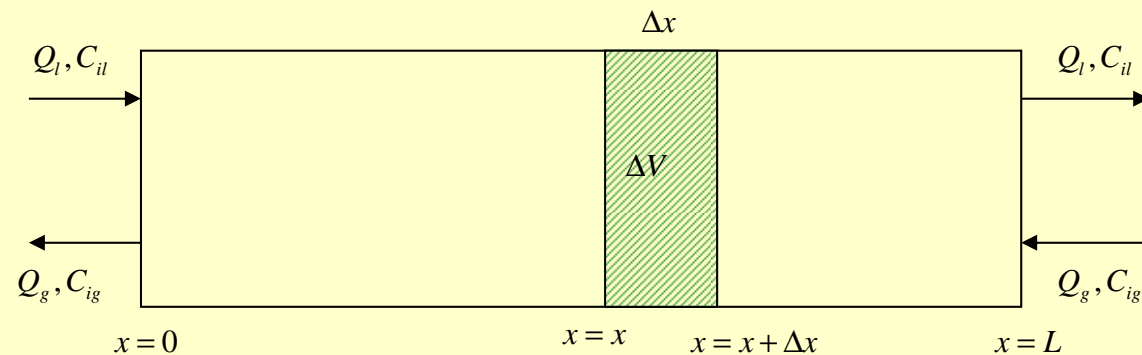
In present work

- Lee et al. model (1996)
 - ▶ Applied to $\text{NH}_3\text{-H}_2\text{O-NaOH}$
 - ▶ Assuming ammonia as a solvent species
- Application to mixed solvent systems with Lee et al. model
- Extension of Lee et al. model based on solvation

Mass Transfer

- **Steady state mass balance for shell side flow**

1. **Counter-current flow**

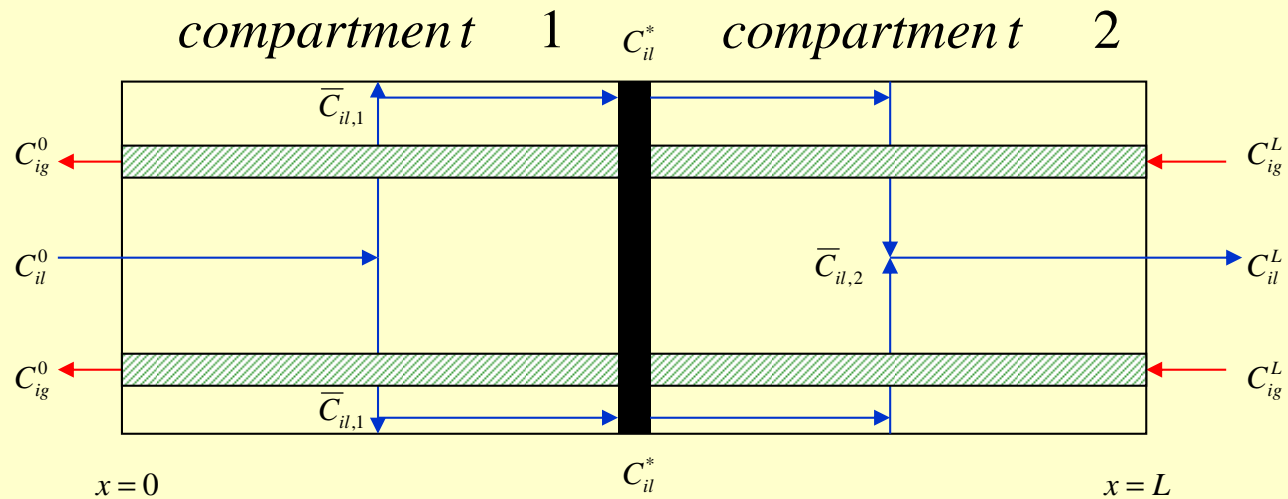


$$\frac{dC_{il}}{dx} + K_Q (1 - R) C_{il} = -K_Q (R C_{il}^L - C_{ig}^L / H_i) \quad K_Q = K_{il} A / Q_l \quad R_Q = Q_l / Q_g H_i$$

$$\frac{C_{il}^L}{C_{il}^0} = \frac{1 - R}{\exp [K_Q (1 - R) L] - R} + \frac{C_{ig}^L}{C_{il}^0 H_i} \frac{\exp [K_Q (1 - R_Q) L] - 1}{\exp [K_Q (1 - R_Q) L] - R_Q}$$

Mass Transfer

2. Cross flow



- **Gas phase : Tube side**
 - ▶ Concentration : Only dependent on x
- **Liquid phase : Shell side**
 - ▶ Concentration : dependent on x, r

Mass Transfer

- Mass Balance

$$\frac{2Q_g}{(R^2 - R_o^2)} \frac{dC_{ig}(x)}{dx} = \frac{Q_l}{rL} \frac{\partial C_{il}(x,r)}{\partial r} \quad Q_g \frac{dC_{ig}}{dx} = -k_{il} A \left(C_{il,2} - \frac{C_{ig}}{H_i} \right)$$

$$Q_g (C_{ig}^L - C_{ig}^0) = Q_l (C_{il}^L - C_{il}^0)$$

$$\frac{C_{ig}^0}{C_{il}^{R_0} H_i} = 1 - \exp[-R_Q(1-E)] + \frac{C_{ig}^L}{C_{il}^{R_0} H_i} \exp[-R_Q(1-E)] \quad E = \exp(-K_Q L)$$

- Removal efficiency

$$1 - \frac{C_{il}^L}{C_{il}^{R_0}} = \frac{(1-F)\{R_Q(1+F) - (1-F)\}}{R_Q\{R_Q - (1-F)^2\}} - \frac{C_{ig}^L}{C_{il}^{R_0} H_i} \frac{R_Q(1-F^2) - (1-F)^2}{R_Q\{R_Q - (1-F)^2\}}$$

$$F = \exp\left[-R_Q\left(1 - E^{1/2}\right)\right]$$

Experiment

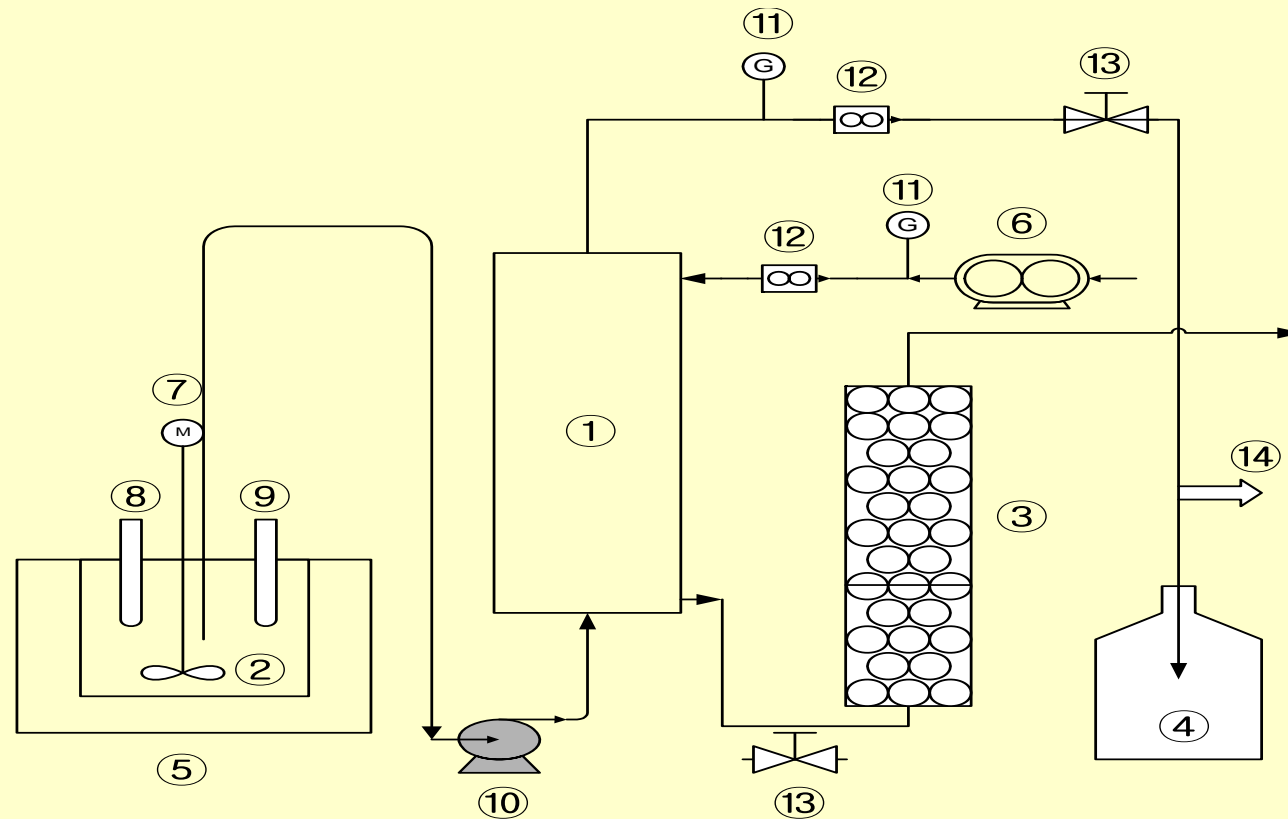


Fig. 1 Schematic diagram of experimental apparatus

Hollow fiber membrane contactor	Ammonia solution reservoir	Packed column
Storage tank	Water bath	Air blower
Stirrer	pH electrode	ATC probe
water pump	Pressure gauge	Flow meter
	Needle valve	Sampling valve

Characteristics of HFMC

Hollow fiber Membrane modules	2.5"x8"	4"x28"
Membrane fiber material	Polypropylene	Polypropylene
Potting material	Polyethylene	Polyethylene
Priming volume (dm ³) ^a	Shell side	4.2 liters
	Lumen side	1.1 liters
Equivalent diameter of shell side ^c	4.10 cm	6.94 cm
Shell side cross section area ^c	13.2 cm ²	37.8 cm ²
Lumen side cross section area ^c	2.92 cm ²	10.2 cm ²
Pore diameter ^a	0.03 micron	0.03 micron
Membrane module inside diameter ^a	2.5 in	4 in
Membrane Porosity ^a	25%	25%
Shell side geometric void fraction ^b	0.40	0.04
Fiber OD/ID ^a	300/200 micron	300/200 micron
Fiber wall thickness ^a	50 micro	50 micro
Maximum allowable working temperature/pressure ^a	60°C/7.4 kg/cm ²	60°C/7.4 kg/cm ²
Effective fiber length ^c	16 cm	62 cm
Effective membrane surface area based on fiber outside diameter ^a	1.40 m ²	19 cm ²
Fiber number (EA) ^c	10200	31800

^aGiven by Hoechst Celanese.

^bEstimated by Pierre et al. (2000)

^cEstimated by Sengupta et al.(1998)

Results

Table 2-1. Comparison of mass transfer coefficients of stripped gases in 2.5"x8" module

	Q ₁ (ml/min)	Parallel flow	Cross flow	Infinite gas phase
NH ₃	10	8.167 x10 ⁻⁶	8.501 x10 ⁻⁶	4.677 x10 ⁻⁶
	20	9.696 x10 ⁻⁶	9.983 x10 ⁻⁶	4.825 x10 ⁻⁶
	30	1.403 x10 ⁻⁵	1.465 x10 ⁻⁵	5.349 x10 ⁻⁶
	100	2.121 x10 ⁻⁵	2.135 x10 ⁻⁵	1.449 x10 ⁻⁵
	200	2.389 x10 ⁻⁵	2.398 x10 ⁻⁵	1.548 x10 ⁻⁵
	300	2.710 x10 ⁻⁵	2.719 x10 ⁻⁵	1.661 x10 ⁻⁵
	500	2.603 x10 ⁻⁵	2.608 x10 ⁻⁵	1.618 x10 ⁻⁵
O ₂	1920	6.970 x10 ⁻³	7.065 x10 ⁻³	6.943 x10 ⁻³
	3780	9.457 x10 ⁻³	9.473 x10 ⁻³	9.395 x10 ⁻³
	7560	1.330 x10 ⁻²	1.333 x10 ⁻²	1.316 x10 ⁻²
	11340	1.556x10 ⁻²	1.559 x10 ⁻²	1.535 x10 ⁻²

Results

Table 2-2. Comparison of mass transfer coefficients of stripped gases in 4"x28"

	Q_1 (ml/min)	Parallel flow	Cross flow	Infinite gas phase
NH ₃	100	9.856×10^{-6}	1.023×10^{-5}	7.243×10^{-6}
	150	1.259×10^{-5}	1.309×10^{-5}	8.468×10^{-6}
	200	1.509×10^{-5}	1.573×10^{-5}	9.241×10^{-6}
	250	1.631×10^{-5}	1.694×10^{-5}	9.508×10^{-6}
O ₂	15138	7.900×10^{-3}	7.914×10^{-3}	7.792×10^{-3}
	18924	8.850×10^{-3}	9.162×10^{-3}	8.704×10^{-3}
	30282	1.124×10^{-2}	1.158×10^{-2}	1.096×10^{-2}
	37848	1.248×10^{-2}	1.283×10^{-2}	1.210×10^{-2}
	45420	1.353×10^{-2}	1.389×10^{-2}	1.306×10^{-2}
	56778	1.483×10^{-2}	1.520×10^{-2}	1.422×10^{-2}
	60558	1.520×10^{-2}	1.557×10^{-2}	1.455×10^{-2}
	75702	1.652×10^{-2}	1.689×10^{-2}	1.569×10^{-2}
	90840	1.765×10^{-2}	1.802×10^{-2}	1.664×10^{-2}
	94626	1.793×10^{-2}	1.829×10^{-2}	1.687×10^{-2}
	105978	1.875×10^{-2}	1.912×10^{-2}	1.756×10^{-2}
	121122	1.998×10^{-2}	2.037×10^{-2}	1.859×10^{-2}

Results

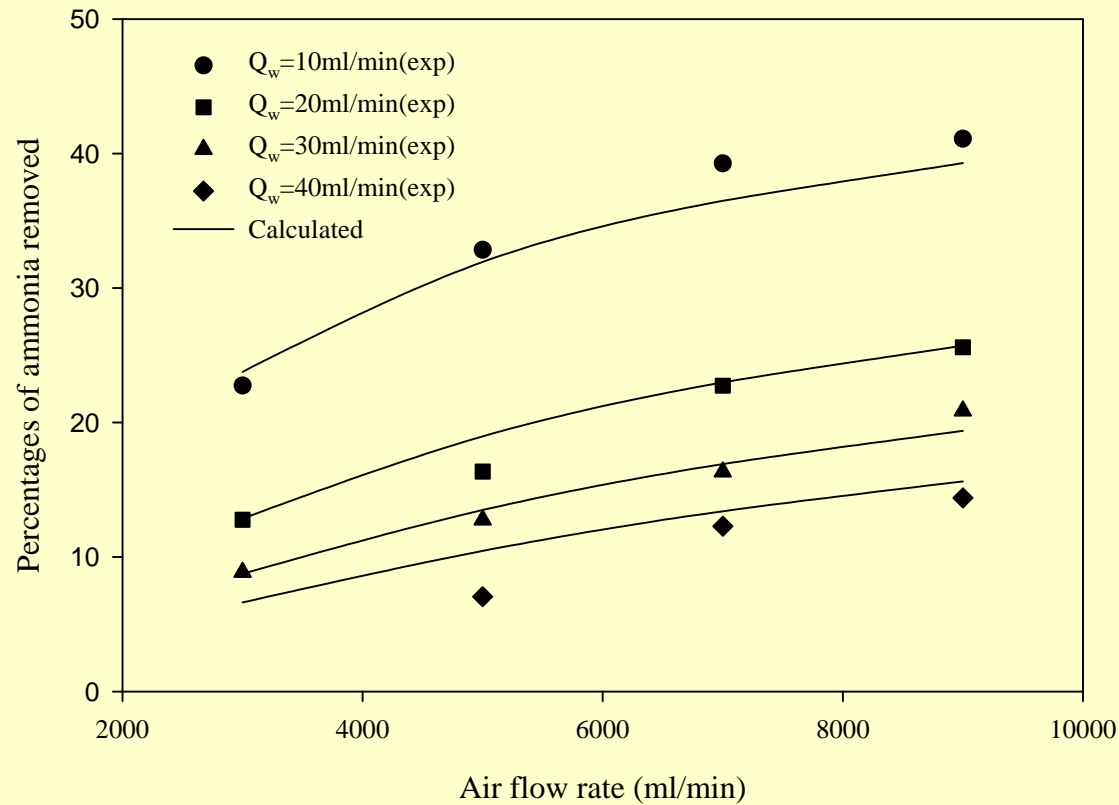


Fig.2-3 Comparison of experimental percentage of ammonia removed with calculated values using 2.5"x8" hollow fiber membrane module with aqueous ammonia solutions

Results

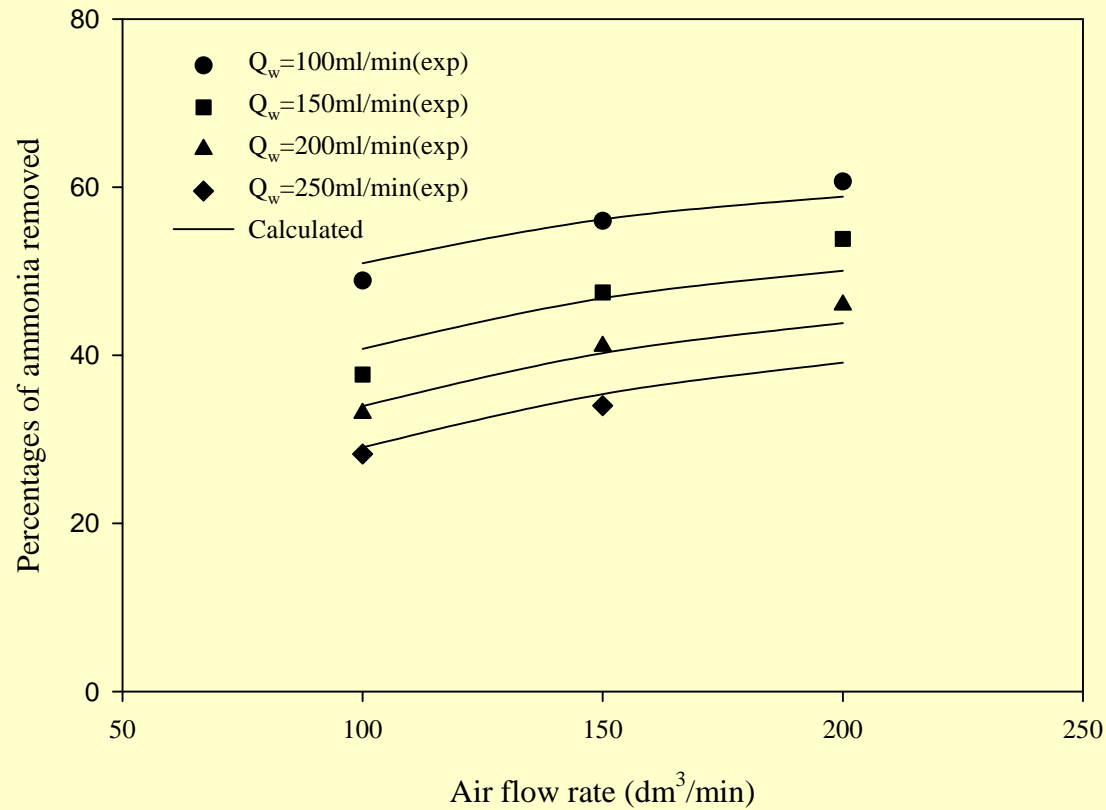


Fig.2-4 Comparison of experimental percentage of ammonia removed with calculated values using 4"x28" hollow fiber membrane module with aqueous ammonia solution

Results

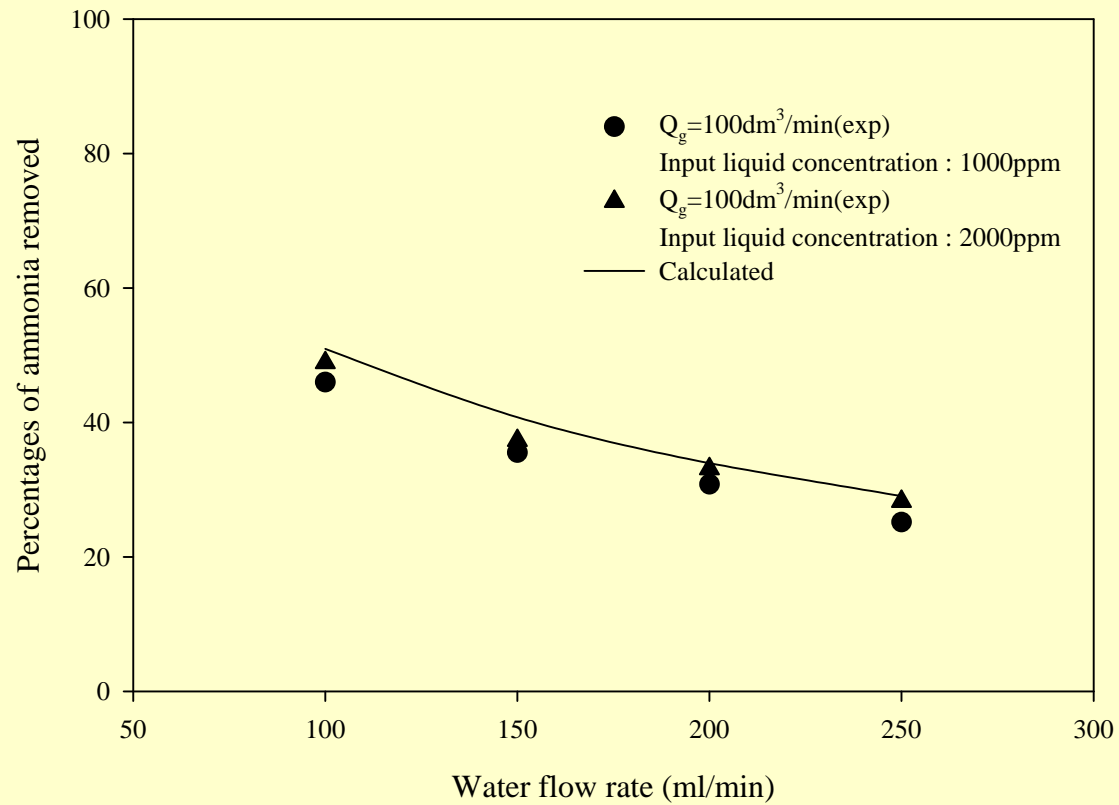


Fig.2-5 Comparison of experimental percentages of ammonia removed with calculated values using 4"x28" hollow fiber membrane module for different input concentrations

Henry's Law

- **Henry's Constant**

$$H_i = \lim_{C_{il} \rightarrow 0} \frac{C_{ig}}{C_{il}} = \frac{V_l}{RT} \lim_{x_i \rightarrow 0} \frac{P_i}{x_i}$$

- ▶ **Assuming ideal gas phase**
- ▶ **From ammonia-water vapor-liquid equilibrium data at several temperatures, ($x > 0.05$)**
- ▶ **From ammonia-water-NaOH VLE ($\text{pH} > 11$)**

Experiment

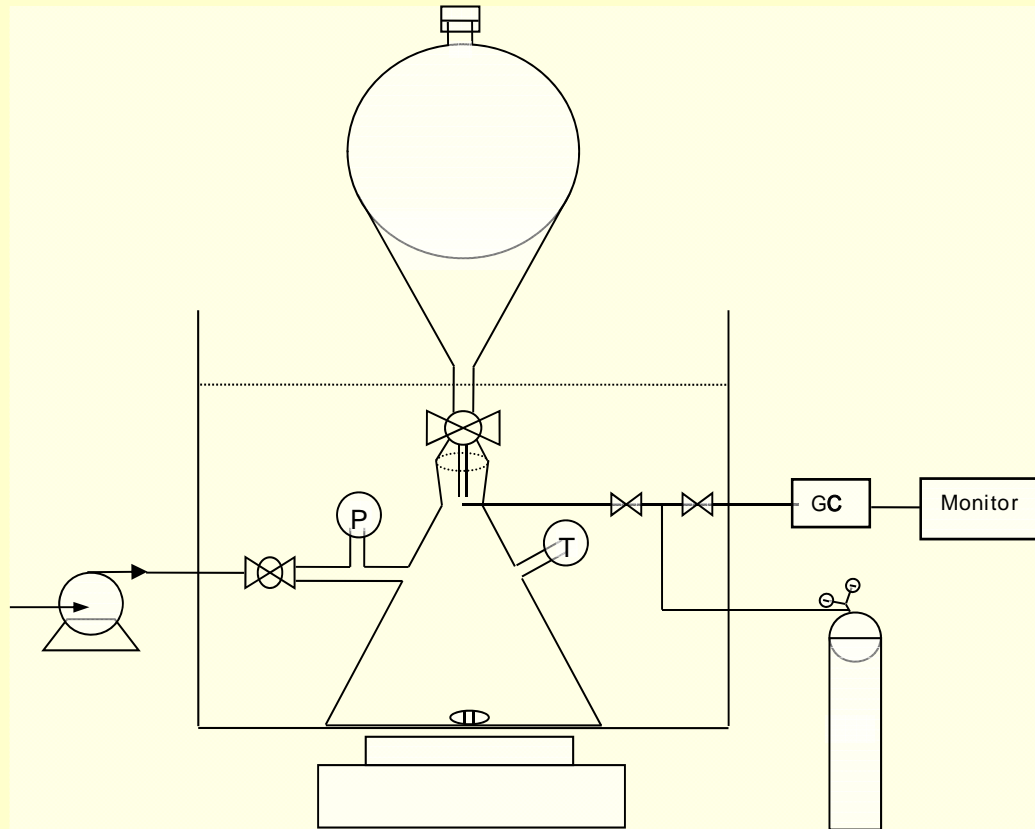


Fig.3.3 Schematic diagram of a modified static measurement

Equilibrium Cell Pressure Transducer Thermometer Vacuum Pump
Helium Gas Magnetic Stirrer Gas Chromatograph A/D Converter
Cork Sampling loop

Results

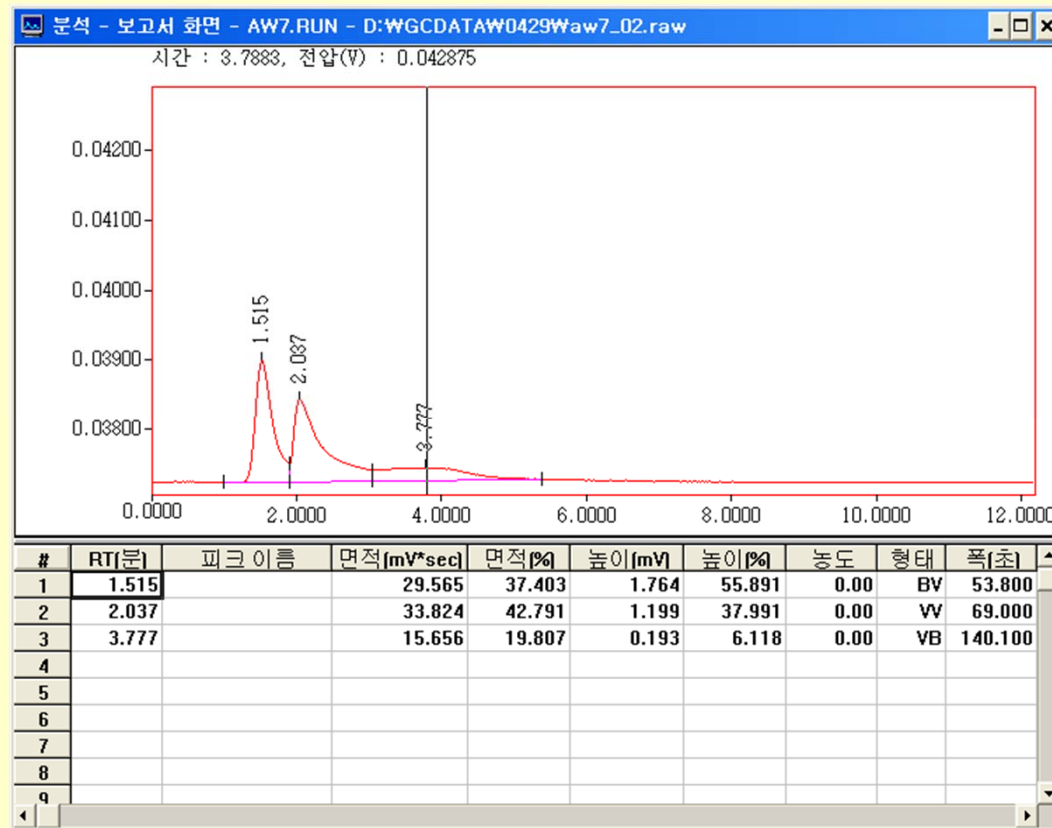


Fig.3-6 The diagram of analysis for vapor phase composition of 7.4% ammonia solution with GC.

Results

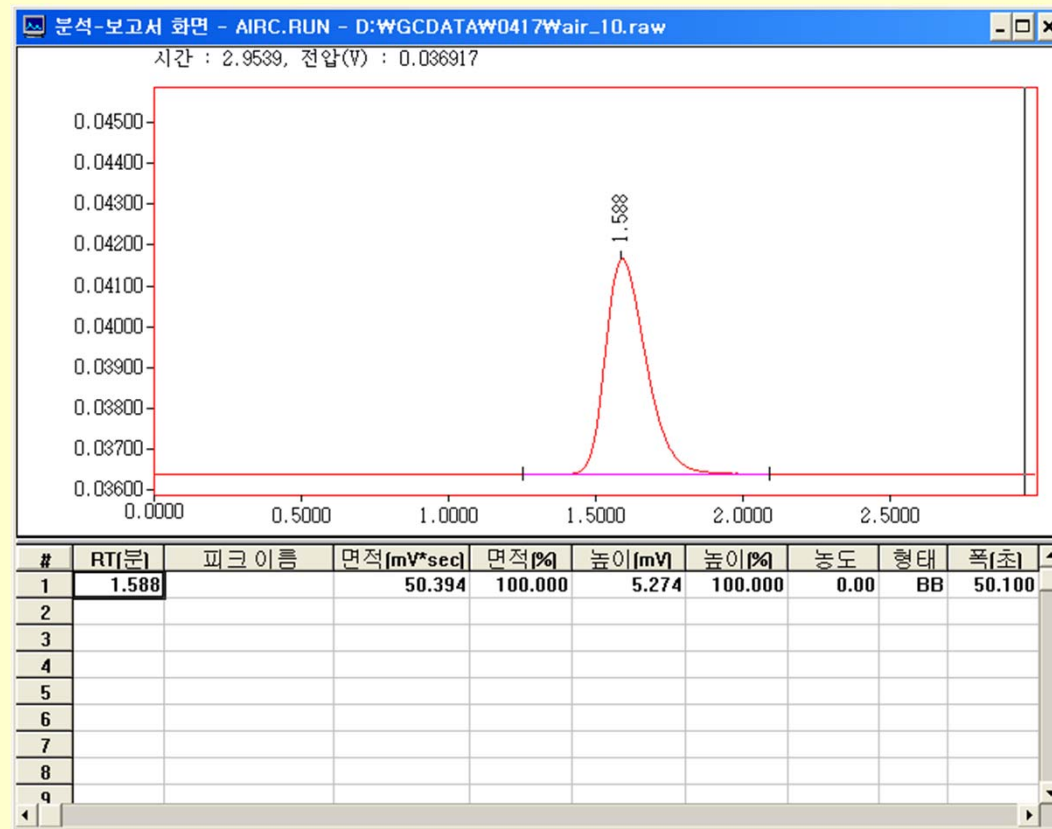


Fig.3-7 The diagram of analysis for air with GC

Results

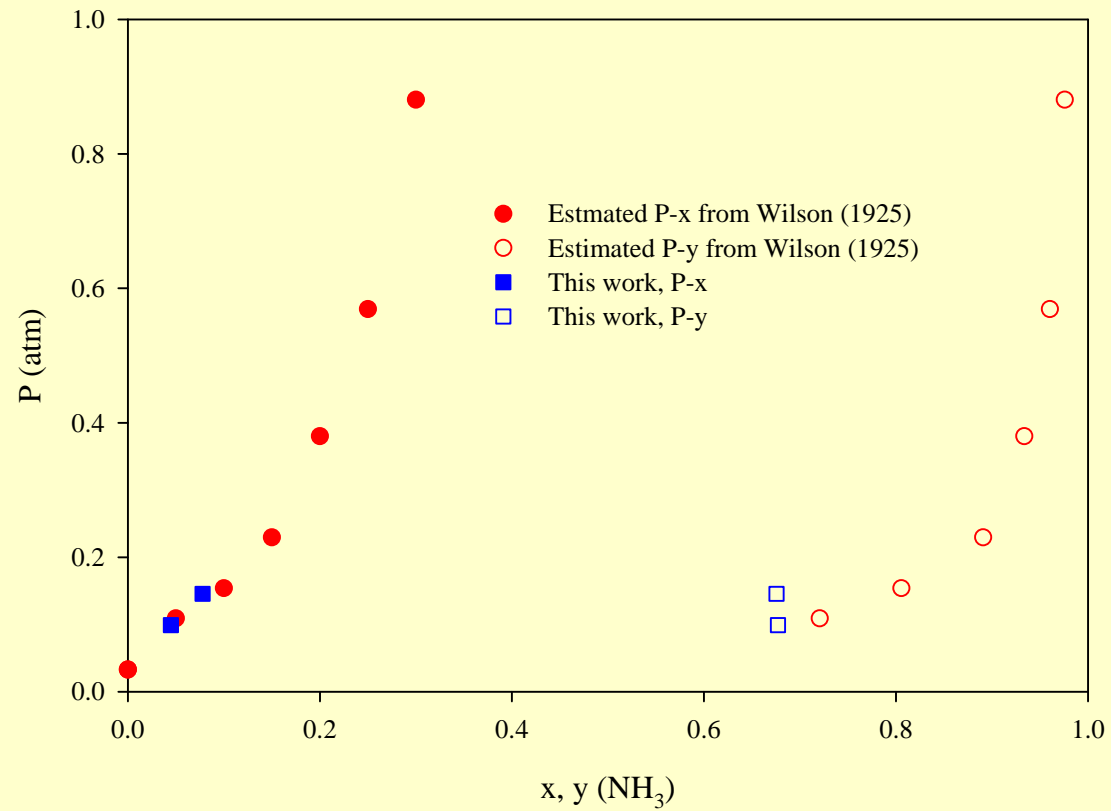


Fig.3-5 Comparison of interpolated data from Wilson (1925) with this work for ammonia-water vapor-liquid equilibria at 298.15K

Results

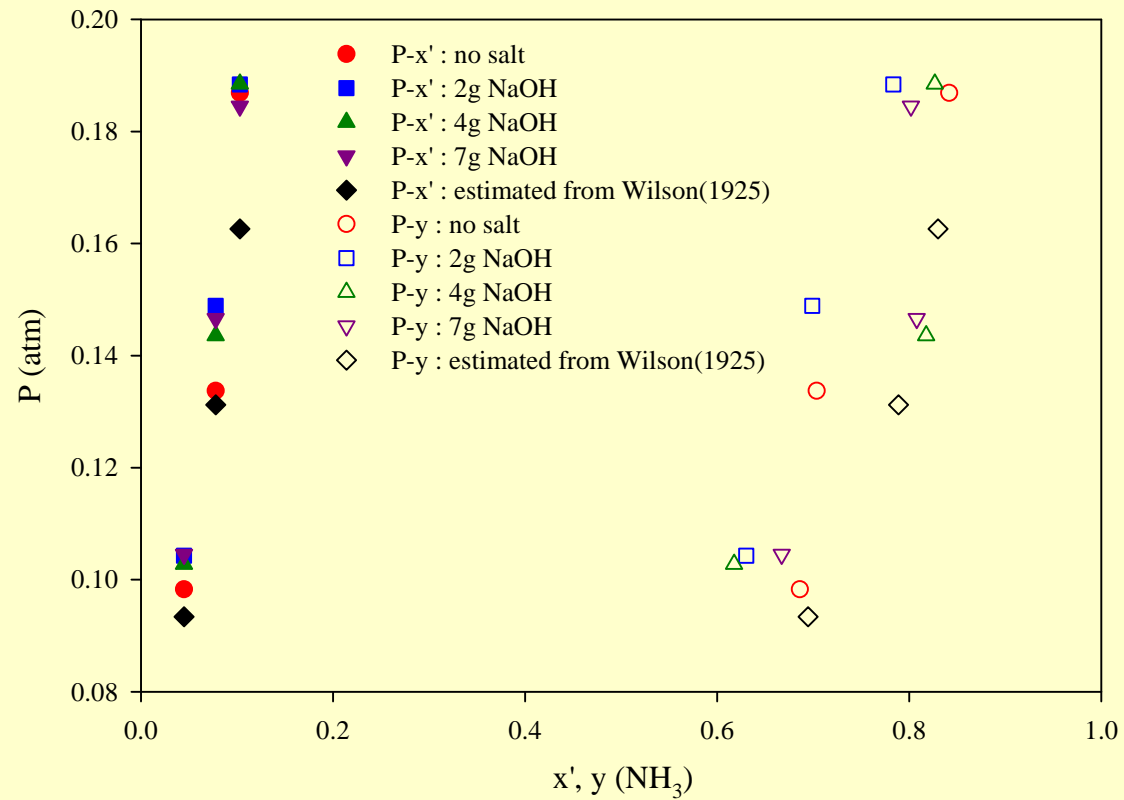


Fig.3-8 P-x'-y diagram for $\text{NH}_3(1)\text{-H}_2\text{O}(2)\text{-NaOH}(3)$ VLE at 298.15K.

Results

Table 3-1. Henry's constants of ammonia in NH₃-H₂O-NaOH systems at 298.15K

Weight of NaOH (g)	Henry's constant
-	1.040 x10 ⁻³
2	1.077 x10 ⁻³
4	9.909 x10 ⁻⁴
7	1.217 x10 ⁻³

cf) $H_i=8.903 \times 10^{-4}$ at 298.15K : estimated from NH₃-H₂O VLE at several temperatures

Correlations for mass transfer coeff.

- Mass transfer

- ▶ mass transfer of liquid in shell side
- ▶ mass transfer of vapor in membrane pore
- ▶ mass transfer of vapor in tube side

- Overall mass transfer coefficient

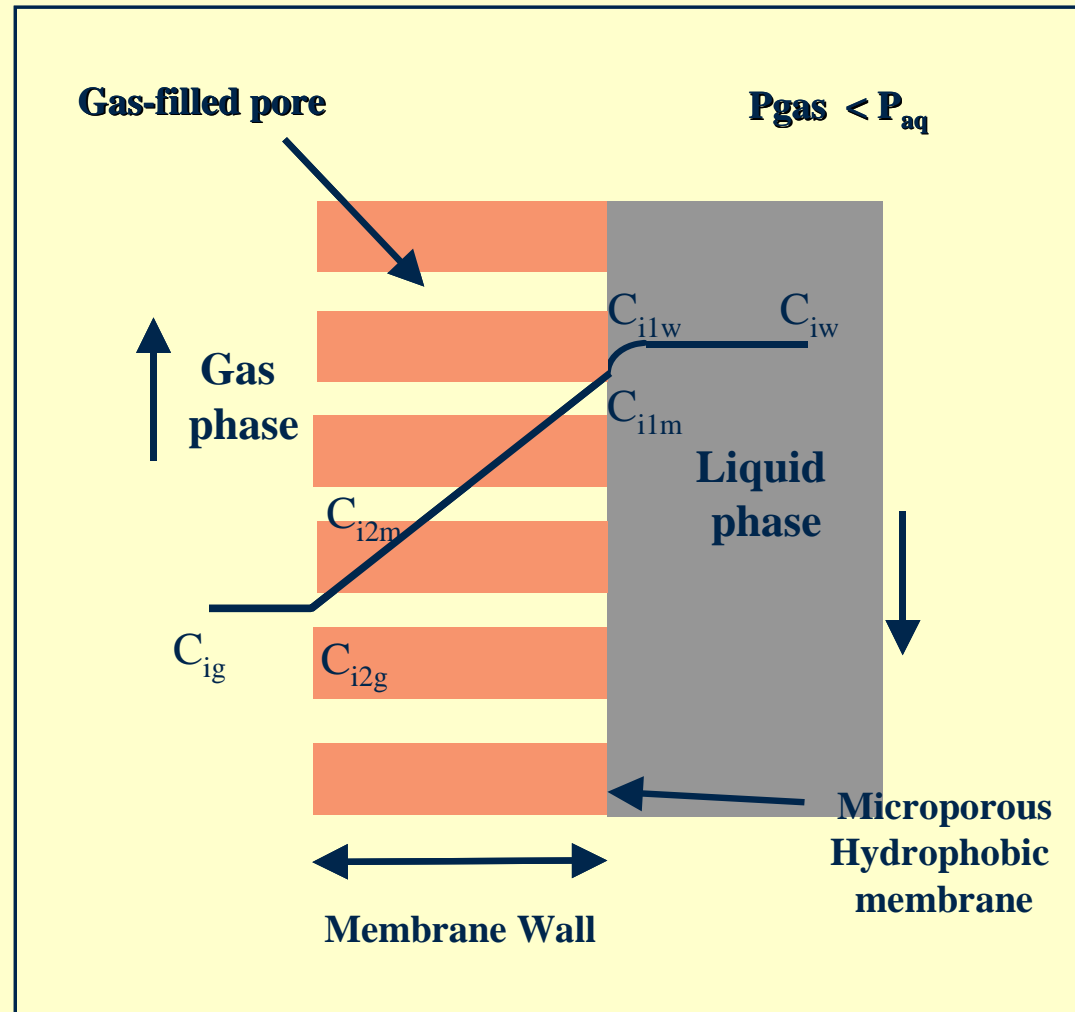
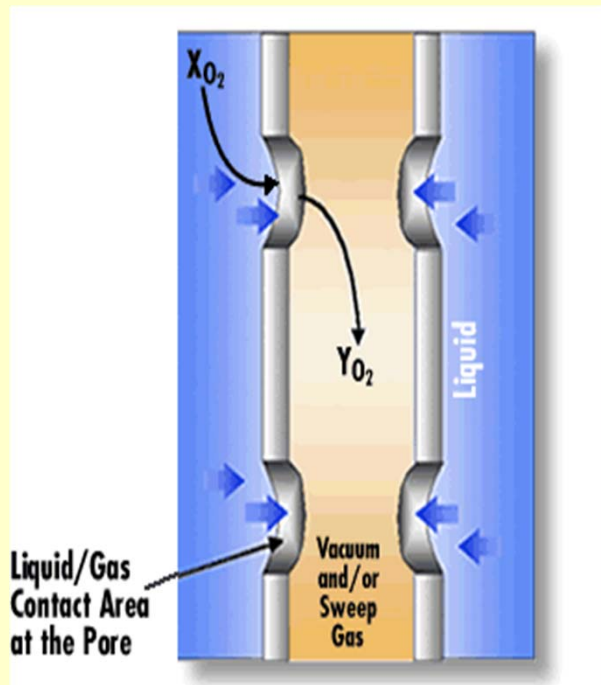
$$\frac{1}{K_{il}} = \frac{1}{k_{il}^l} + \frac{1}{k_{ig}^p H_i} + \frac{1}{k_{ig}^g H_i}$$

$$k_{ig}^g = 1.62 \frac{D_{ig}}{d} \left(\frac{d^2 v_g}{LD_{ig}} \right)^{1/3} \quad k_{ig}^p = \frac{2r_p}{3} \left(\frac{8RT}{\pi M_i} \right)^{1/2} \frac{\varepsilon}{l\tau} \quad \left(\frac{k_{il}^l d_e}{D_{il}} \right) = a \left(\frac{d_e v_l}{v_l} \right)^b \left(\frac{v_l}{D_{il}} \right)^c$$

- ▶ Yang and Cussler (1986), Sengupta et al.(1998)

$$K_{il} \approx k_{il}^l \quad \left(\because k_{il}^l \leq k_{ig}^p, k_{ig}^g \right)$$

Hollow Fiber Membrane contactor?



Results

Table 4-2. Comparison with individual mass transfer coefficients in 4"x28" module

Q_g (dm ³ /min)	Individual mass transfer coefficients (cm/sec)	Q_l (ml/min)			
		100	150	200	250
100	k_{il}	9.11x10 ⁻⁶	1.05x10 ⁻⁵	1.38x10 ⁻⁵	1.54x10 ⁻⁵
	$k_{ig}^p H_i$	1.34x10 ⁻³	1.34x10 ⁻³	1.34x10 ⁻³	1.34x10 ⁻³
	$k_{ig}^g H_i$	9.33x10 ⁻³	9.33x10 ⁻³	9.33x10 ⁻³	9.33x10 ⁻³
150	k_{il}	9.90x10 ⁻⁶	1.29x10 ⁻⁵	1.54x10 ⁻⁵	1.53x10 ⁻⁵
	$k_{ig}^p H_i$	1.34x10 ⁻³	1.34x10 ⁻³	1.34x10 ⁻³	1.34x10 ⁻³
	$k_{ig}^g H_i$	1.18x10 ⁻²	1.18x10 ⁻²	1.18x10 ⁻²	1.18x10 ⁻²
200	k_{il}	1.06x10 ⁻⁵	1.44x10 ⁻⁵	1.61x10 ⁻⁵	1.82x10 ⁻⁵
	$k_{ig}^p H_i$	1.34x10 ⁻³	1.34x10 ⁻³	1.34x10 ⁻³	1.34x10 ⁻³
	$k_{ig}^g H_i$	1.35x10 ⁻²	1.35x10 ⁻²	1.35x10 ⁻²	1.35x10 ⁻²

Results

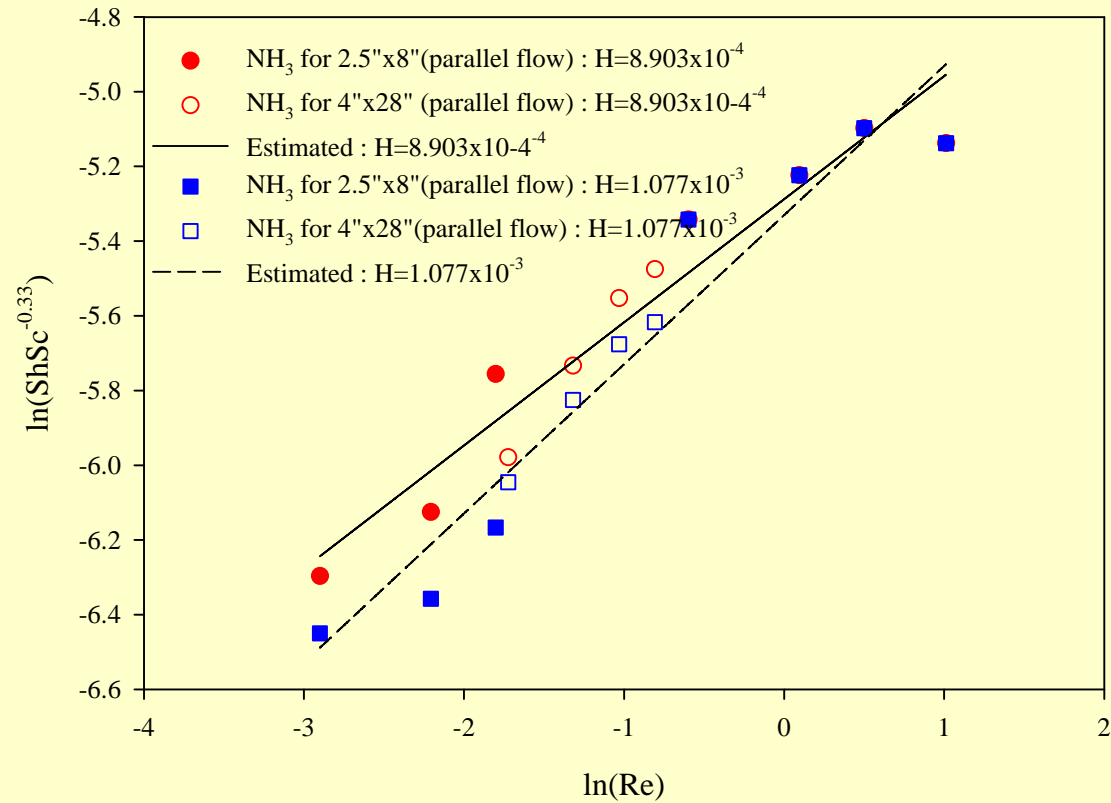


Fig.4-4 The correlation of shell side mass transfer coefficient of NH_3 with 2.5"x8" and 4"x28" membrane contactor modules

Results

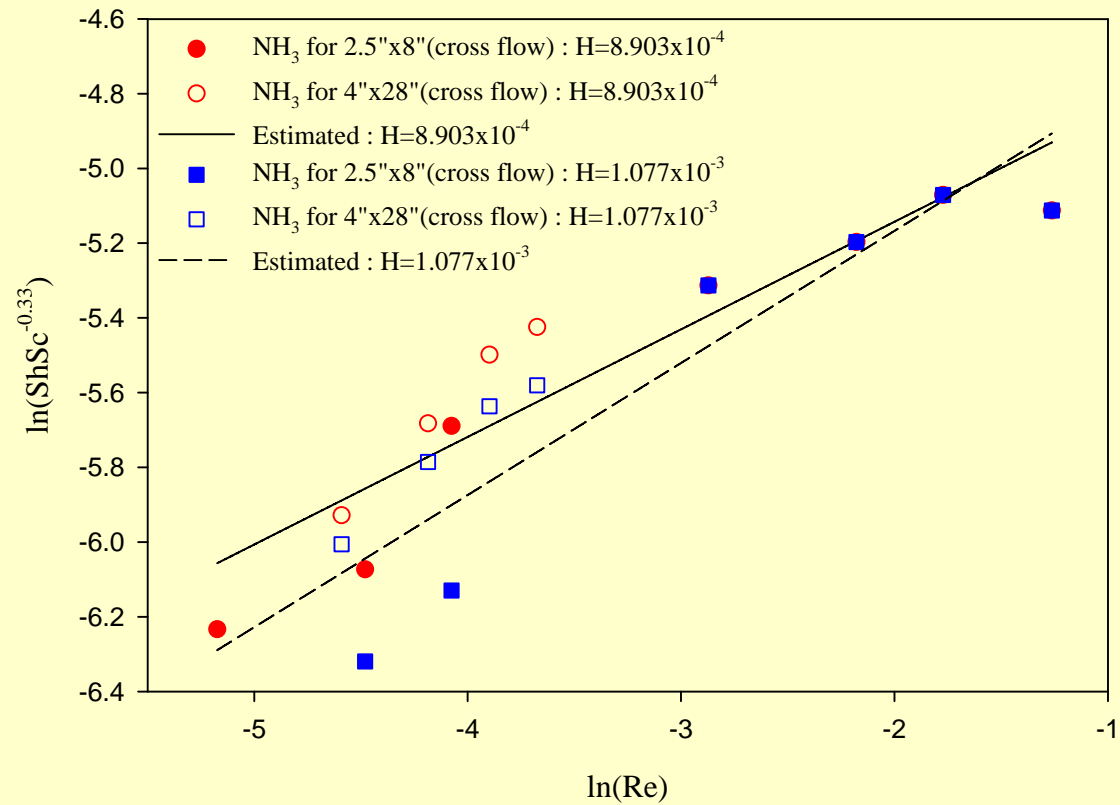


Fig.4-5 The correlation of shell side mass transfer coefficient of NH₃ with 2.5"x8" and 4"x28" membrane contactor modules

Results

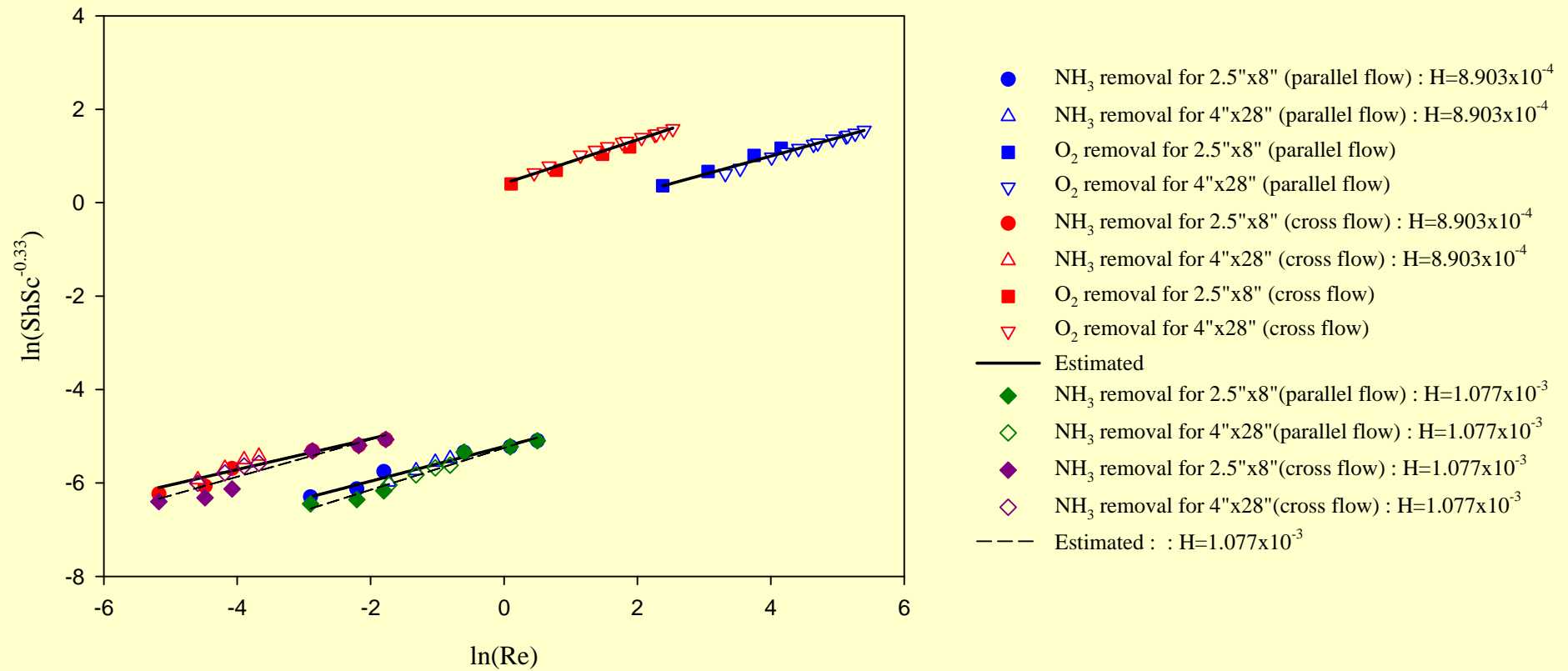


Fig.4-6 The comparison of mass transfer coefficients for ammonia removal and oxygen removal.

Results

Table 4-3. The fitted parameter a and b for the correlation of mass transfer coefficients

	Parallel flow		Cross flow	
	a	b	a	b
NH ₃ ¹⁾	0.0055	0.37	0.012	0.33
NH ₃ ²⁾	0.0052	0.45	0.014	0.40
O ₂	0.57	0.39	1.51	0.47

$${}^1)H_i=8.903 \times 10^{-4}$$

$${}^2)H_i=1.077 \times 10^{-3}$$

Application to $\text{NH}_3\text{-H}_2\text{O}$ VLE

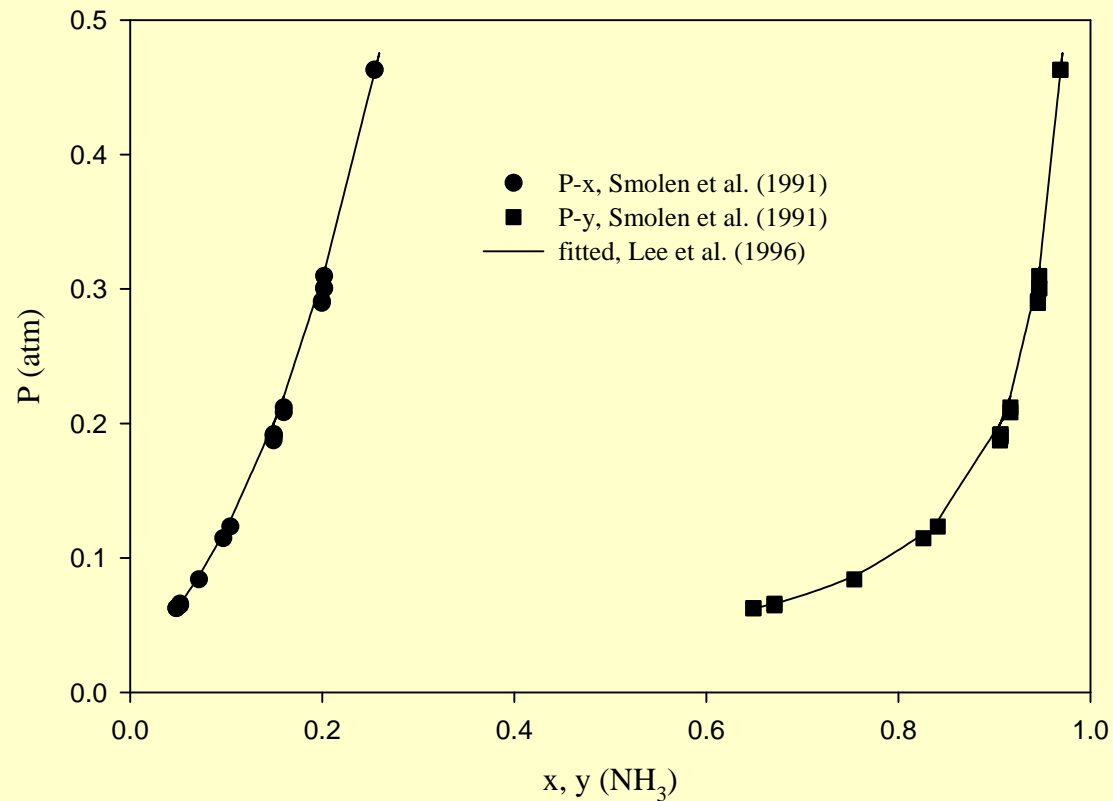


Fig.5-1 P-x, P-y diagram of ammonia-water vapor-liquid equilibrium at 293.15K

Application to $\text{NH}_3\text{-H}_2\text{O}$ VLE

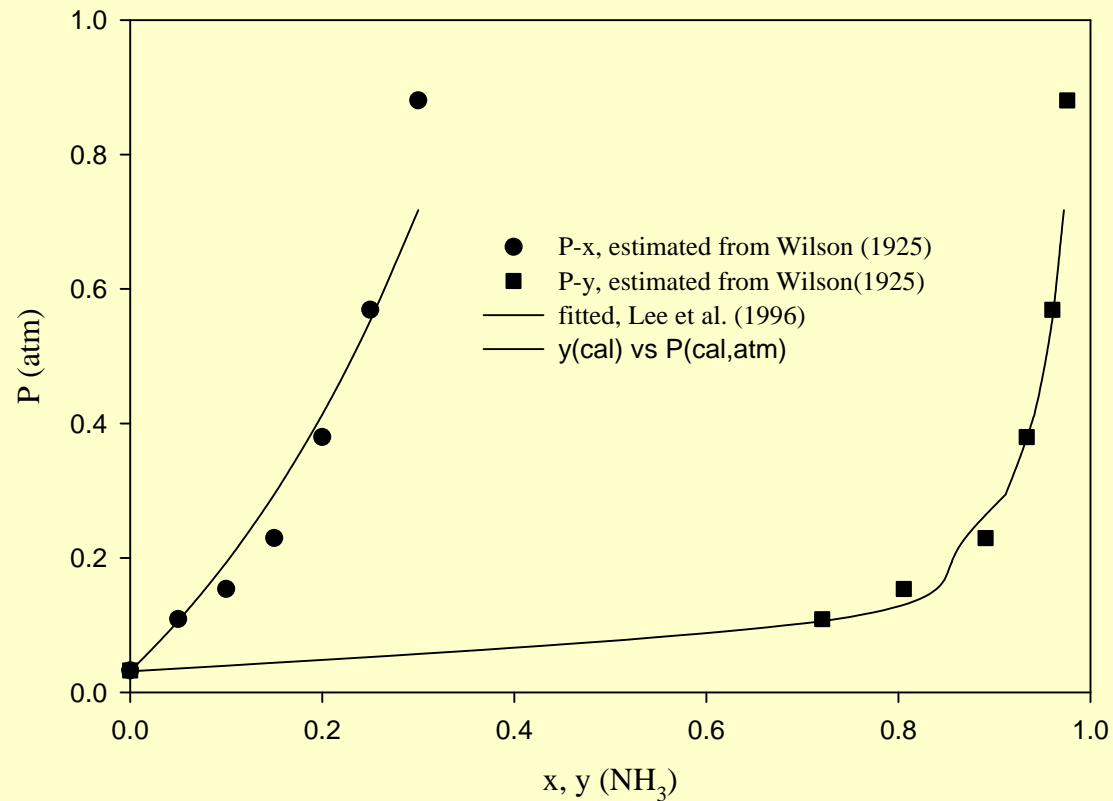


Fig.5-2 P-x-y diagram of ammonia-water vapor-liquid equilibria at 298.15K

Application to $\text{NH}_3\text{-H}_2\text{O-NaOH}$ VLE

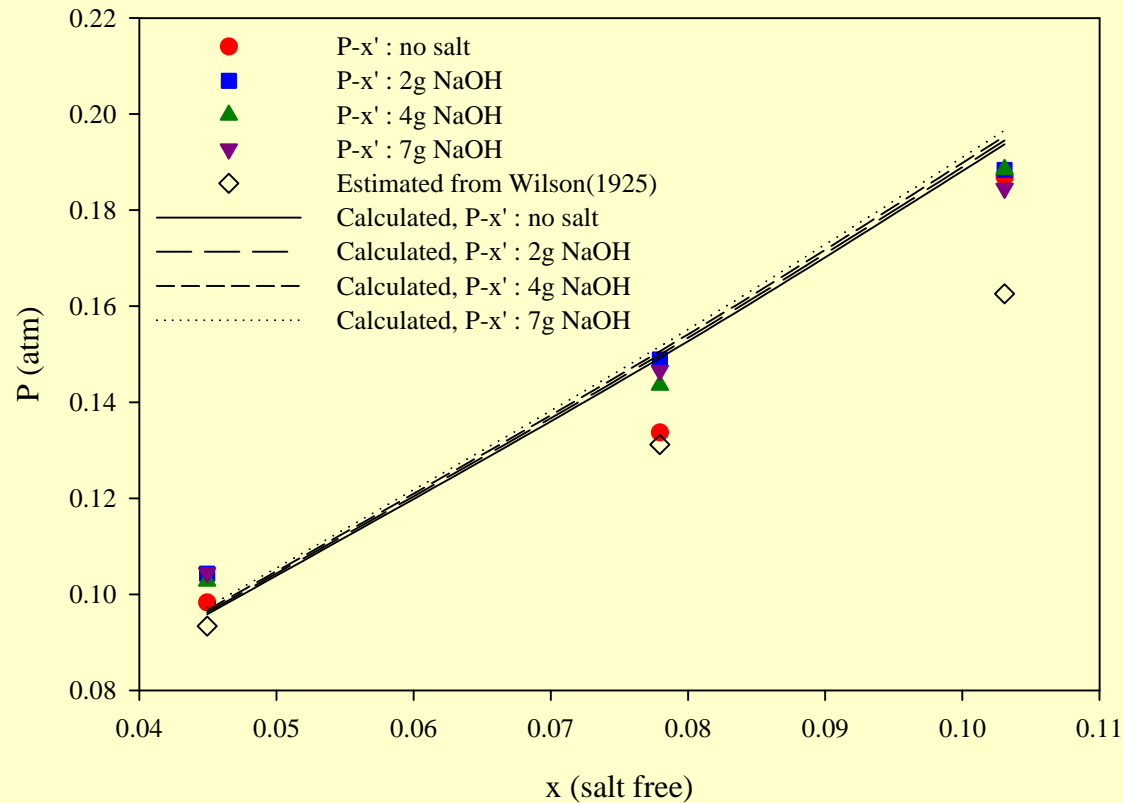


Fig.5-3 P-x' diagram of $\text{NH}_3(1)\text{-H}_2\text{O}(2)\text{-NaOH}(3)$ at 298.15K .

Application to $\text{NH}_3\text{-H}_2\text{O-NaOH}$ VLE

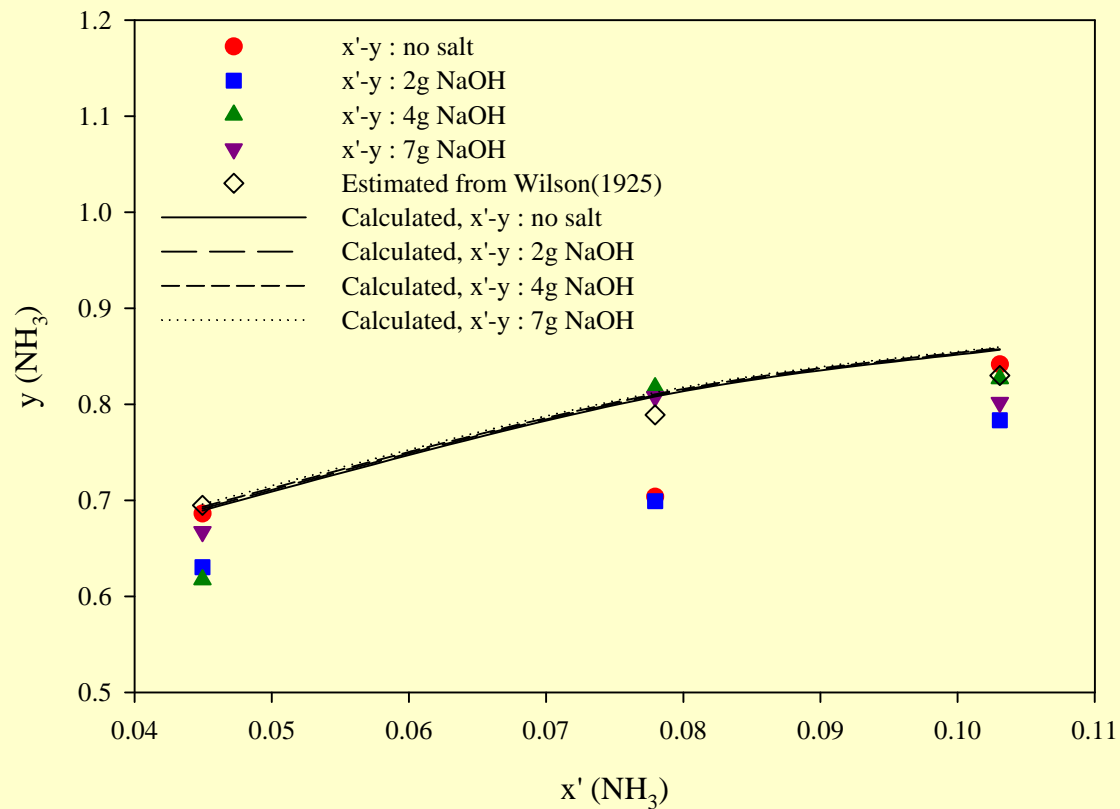


Fig.5-4 $x\text{'-}y$ diagram of $\text{NH}_3(1)\text{-H}_2\text{O}(2)\text{-NaOH}(3)$ at 298.15K

Mixed Solvent Systems

- **Increasing interest in the effects of salts on the VLE of solvent mixtures.**
 - ▶ **A wide variety of important chemical processes**
 - **Wastewater treatment, extractive distillation, solution crystallization, desalination, gas scrubbing etc.**
- **The effect of salt out and salt in : shifting and eliminating azeotrope of solvent mixtures**
- **Little is known about the effect of electrolyte on VLE of alcohol-water-systems because of complex interaction between mixed solvents**

Mixed Solvent Systems

- **Mock et al. (1986)**
 - ▶ Extended Chen's NRTL model to mixed solvent solution
 - ▶ Ignore long-range interaction term
- **Sander et al. (1986)**
 - ▶ Extended UNIQUAC equation for the representation of salt effect on VLE
 - ▶ Concentration-dependent interaction parameter
- **Macedo et al. (1990)**
 - ▶ Modified Debye-Hückel term from Cardoso and O'Connell (1987)
- **Li et al. (1994), Polka et al. (1994)**
 - ▶ 4 ion-ion parameters
 - ▶ 2 solvent-solvent parameters
 - ▶ Applicable up to high concentration

Mixed Solvent Systems

- **Excess Gibbs Energy : Lee et al. (1996)**

- ▶ **Long-range + Physical** $G^E = G_{DH}^E + G_A^E + G_R^E$

- ▶ **Debye-Hückel term**

$$G_{DH}^{E*} = -\frac{RTV}{4\pi a^3 N_a} \left[\ln(1+aK) - aK + \frac{(aK)^2}{2} \right] \quad K = \left(\frac{8\pi e^2 N_a I}{D_s kT} \right)^{1/2}$$

- ▶ **In high pressure limit, holes are vanished**

$$A^E(T, P = \infty, x_i) = A^E(T, low P, x_i) = G^E(T, low P, x_i)$$

- ▶ **Physical interaction : Athermal + Residual**

$$\beta G_A^E = \sum N_i \ln \frac{\theta_i}{x_i} + \left(1 - \frac{z}{2}\right) \sum N_i q_i \ln \frac{q_M r_i}{r_M q_i} \quad \beta G_R^E = -\frac{zN_q}{2} \sum \theta_i \ln \left(\sum \theta_j \tau_{ji} \right)$$

Mixed Solvent Systems

- For solvent activity coefficient

$$\ln \gamma_j = \ln \gamma_{DH,j} + \ln \gamma_{A,j} + \ln \gamma_{R,j}$$

- For solute activity coefficient

$$\ln \gamma_j^* = \ln \gamma_j - \lim_{x_i \rightarrow 0} \ln \gamma_j$$

$$\ln \gamma_{\pm j}^* = \ln \gamma_{DH,\pm j}^* + \ln \gamma_{A,\pm j}^* + \ln \gamma_{R,\pm j}^*$$

- Interaction between ion

$$\epsilon_{ij} = \epsilon_{ij}^{(e)} + \epsilon_{ij}^{(n)}$$

- Interaction with uncharged species

$$\epsilon_{ij} = \epsilon_{ij}^{(n)}$$

- Interaction between unlike species

$$\epsilon_{ij}^{(n)} = (\epsilon_{ii}^{(n)} \epsilon_{jj}^{(n)})^{1/2} (1 - k_{ij})$$

Parameters for Mixed Solvent Systems

- **Parameters for Salt & Water**

- ▶ From Lee et al. (1996)

- **Only parameters for pure solvent & parameters for solvent-water interaction**

$$r_i, \epsilon_{ii}, k_{ij}$$

- **Determination**

- ▶ Data for alcohol-water VLE (Gmehling et al., 1977)

- ▶ Data for alcohol-water mixture volume and dielectric constant (Sandler, 1989; Conway, 1952)

Temperature-dependent parameters

$$r_i = r_a + r_b (T_0 / T) + r_c \ln(T_0 / T)$$

$$\varepsilon_{ii} = \varepsilon_a + \varepsilon_b (T_0 / T) + \varepsilon_c \ln(T_0 / T)$$

$$k_{ij} = k_a + k_b (T_0 / T) + k_c \ln(T_0 / T)$$

$$T_0 = 298.15 K$$

Results

Table 5-1. Temperature coefficients of eqns (5-16) and (5-17) for methanol, ethanol, 1-propanol and 2-propanol

	r_a	r_b	r_c	ϵ_a	ϵ_b	ϵ_c
Methanol	281.80	-270.03	251.12	86.42	-85.13	76.65
Ethanol	16.50	-11.25	8.82	40.88	-40.00	33.16
1-Propanol	-15.20	22.05	-16.21	114.46	-113.83	98.34
2-Propanol	141.49	-136.40	117.42	-4.94	6.11	-9.30

Results

Table 5-2. Temperature coefficients of eqns (5-18) for methanol-, ethanol-, 1-propanol- and 2-propanol-water

	k_a	k_b	k_c
Methanol-water	281.80	-270.03	251.12
Ethanol-water	16.50	-11.25	8.82
1-Propanol-water	-15.20	22.05	-16.21
2-Propanol-water	141.49	-136.40	117.42

Results : Isothermal VLE

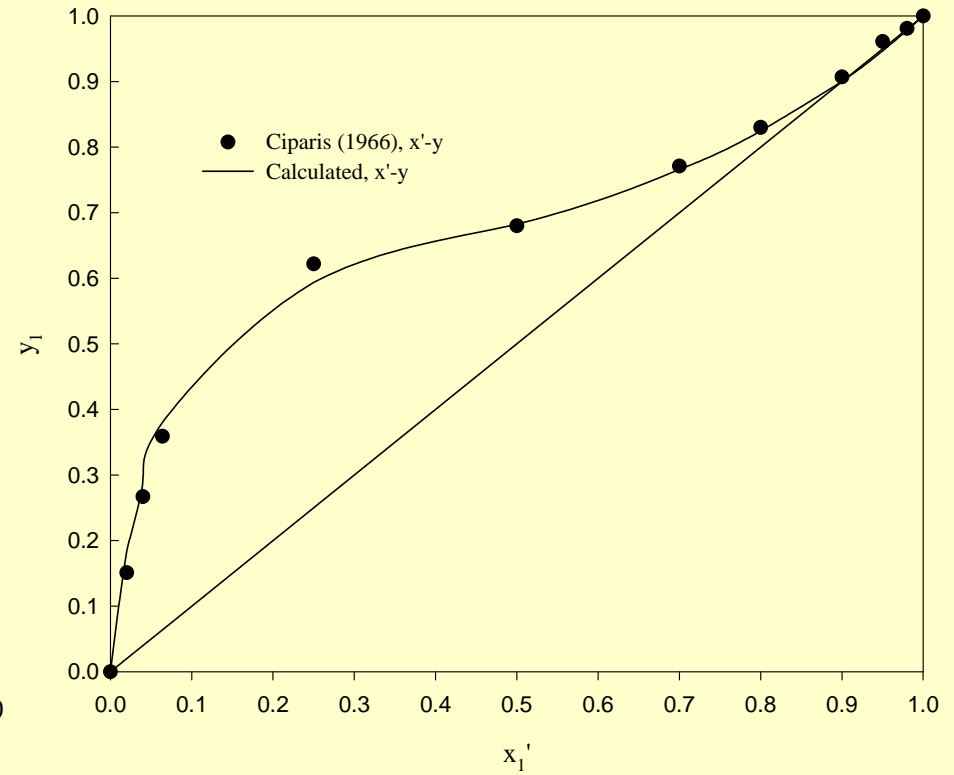
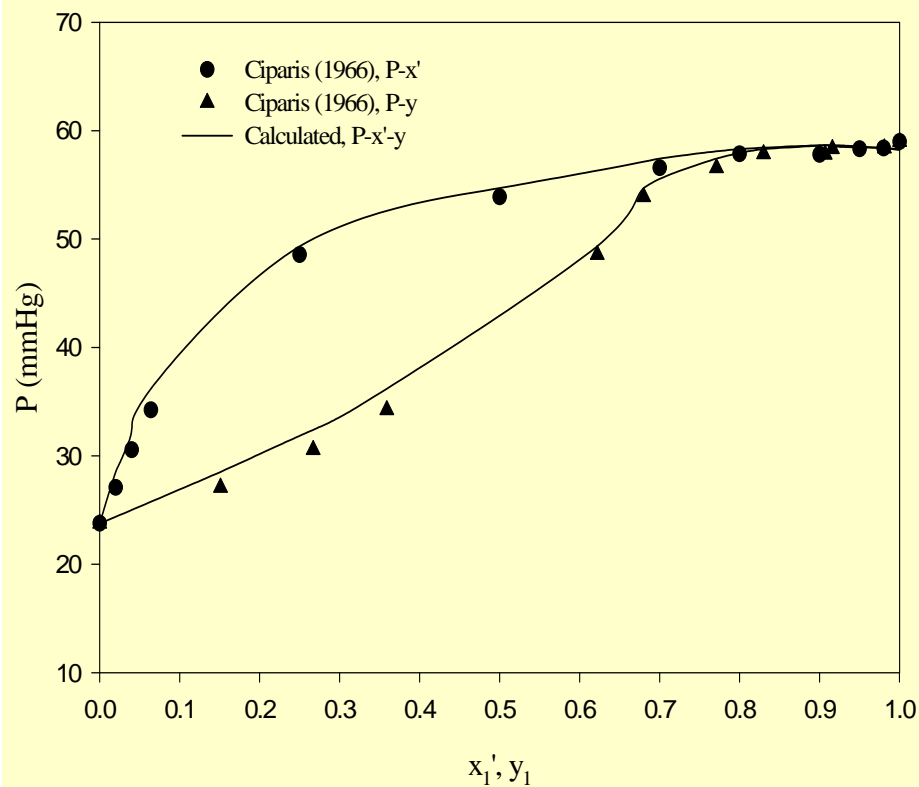


Fig.5-5 P-x'-y for EtOH(1)-H₂O(2)-LiCl(3) VLE at 298.15K.
m(LiCl)=0.0 mol/kg.

Results : Isothermal VLE

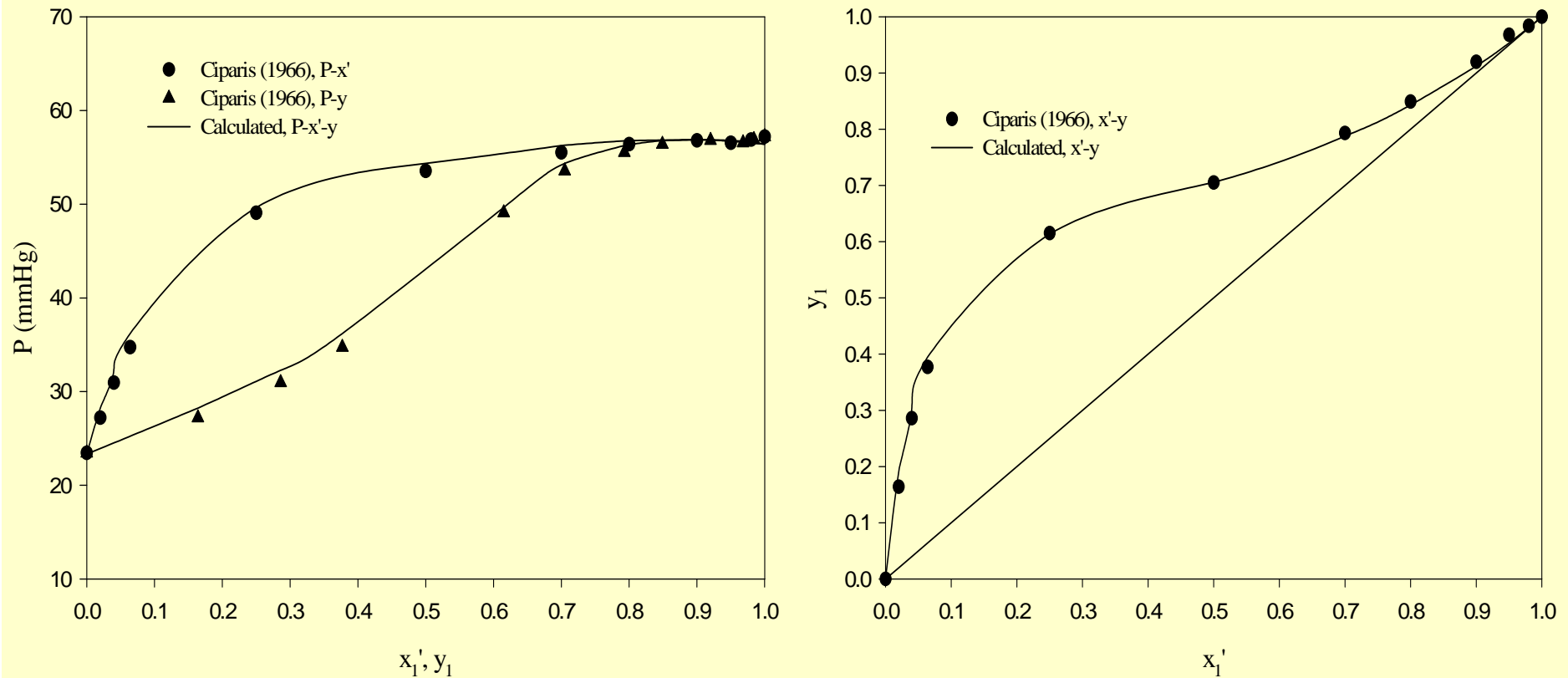


Fig.5-6 $P-x'-y$ for EtOH(1)-H₂O(2)-LiCl(3) VLE at 298.15K.
 $m(\text{LiCl})=0.5 \text{ mol/kg}$.

Results : Isothermal VLE

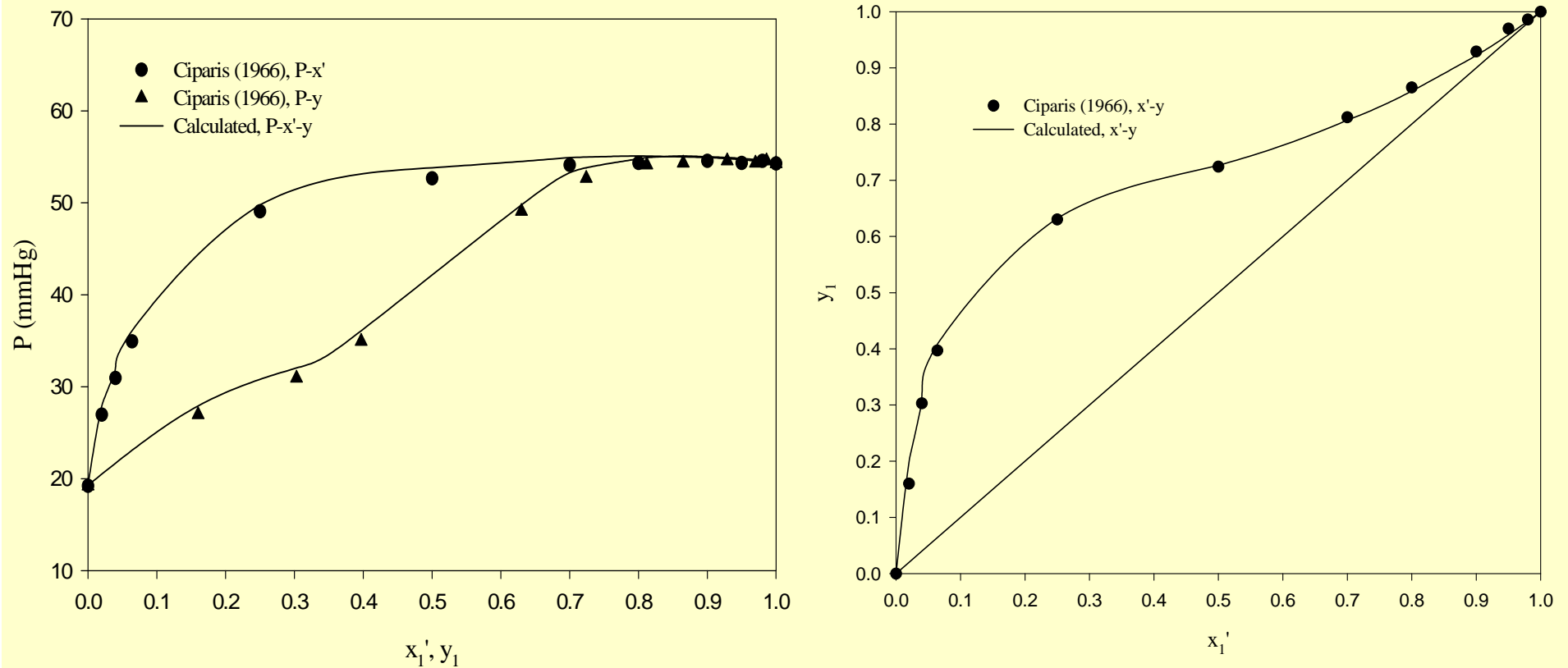


Fig.5-7 $P-x'-y$ for EtOH(1)-H₂O(2)-LiCl(3) VLE at 298.15K.
 $m(\text{LiCl})=1.0 \text{ mol/kg}$.

Results : Isothermal VLE

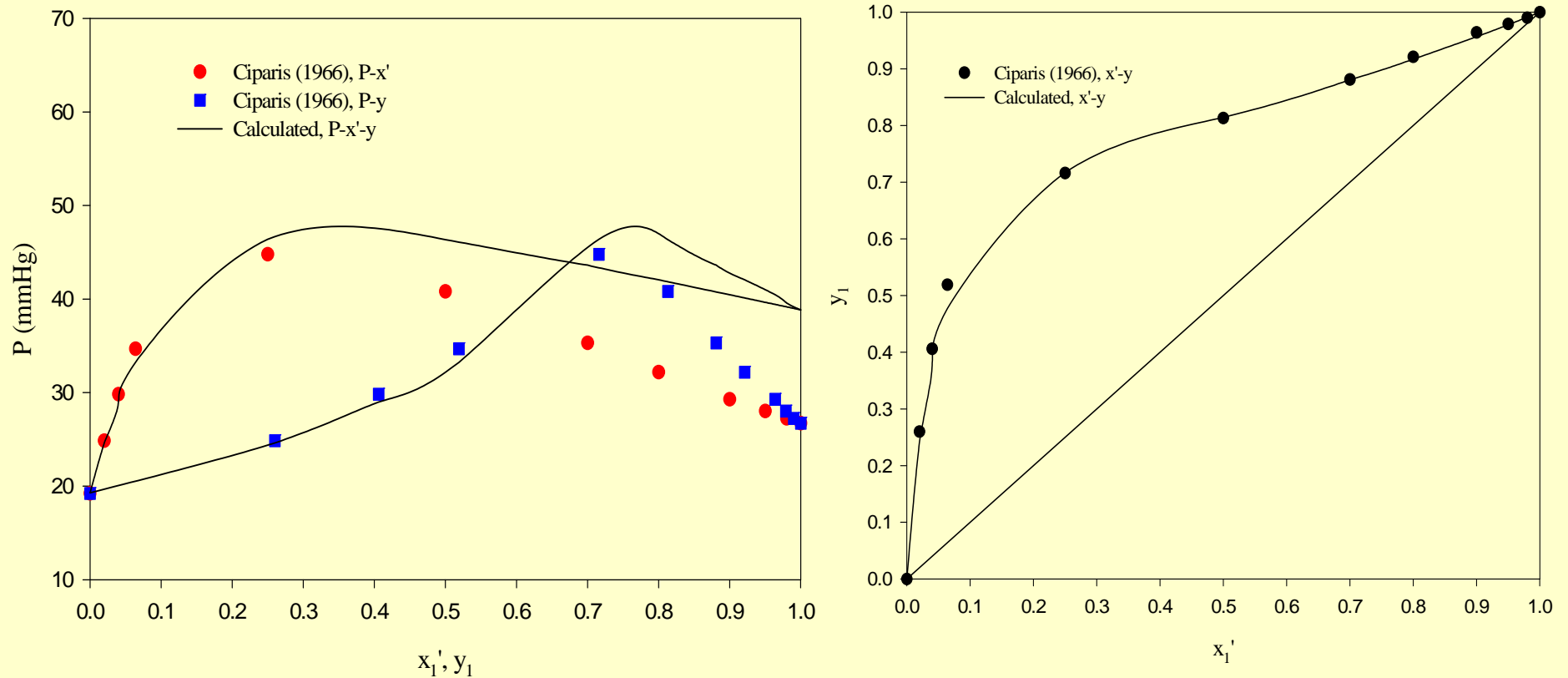


Fig.5-8 $P-x'-y$ for EtOH(1)-H₂O(2)-LiCl(3) VLE at 298.15K.
 $m(\text{LiCl})=4.0 \text{ mol/kg}$

Results : Isothermal VLE

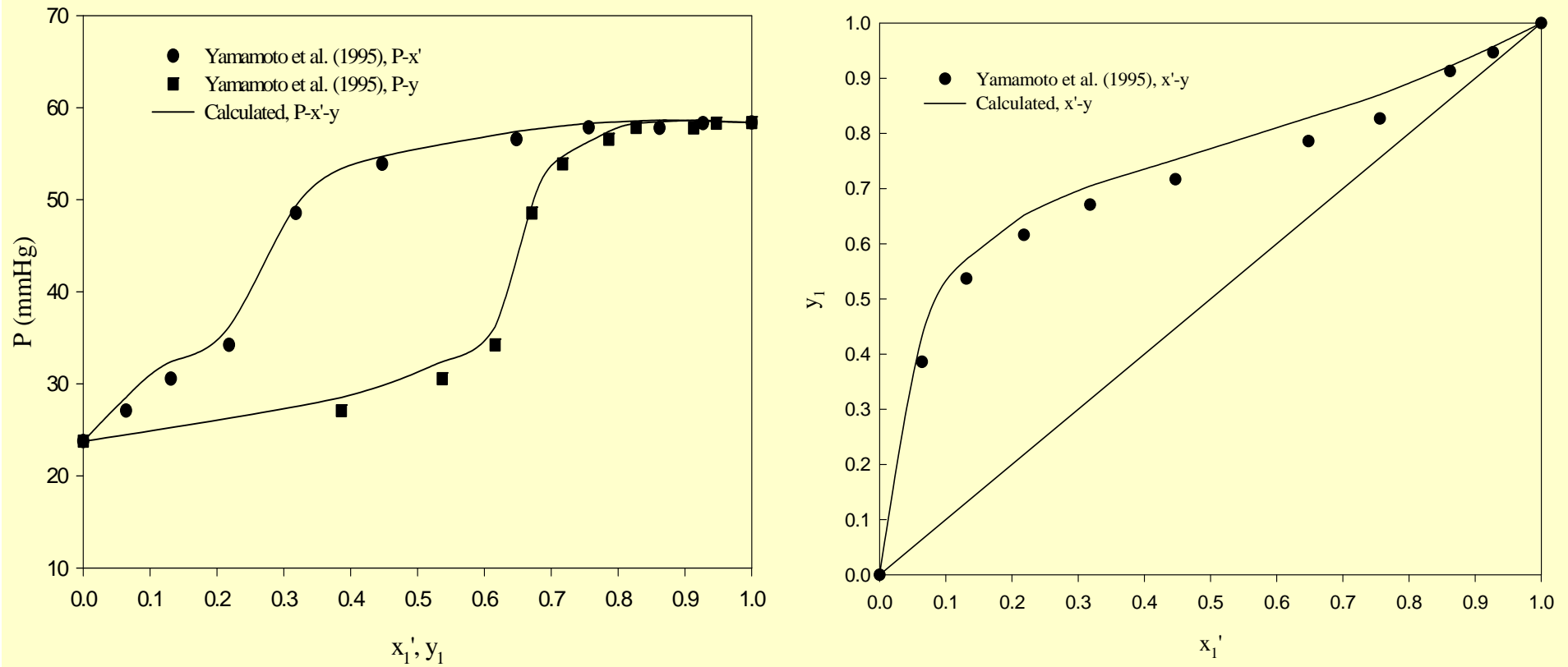


Fig.5-9 P- x' - y for EtOH(1)-H₂O(2)-CaCl₂(3) VLE at 298.15K.

Results : Isothermal VLE

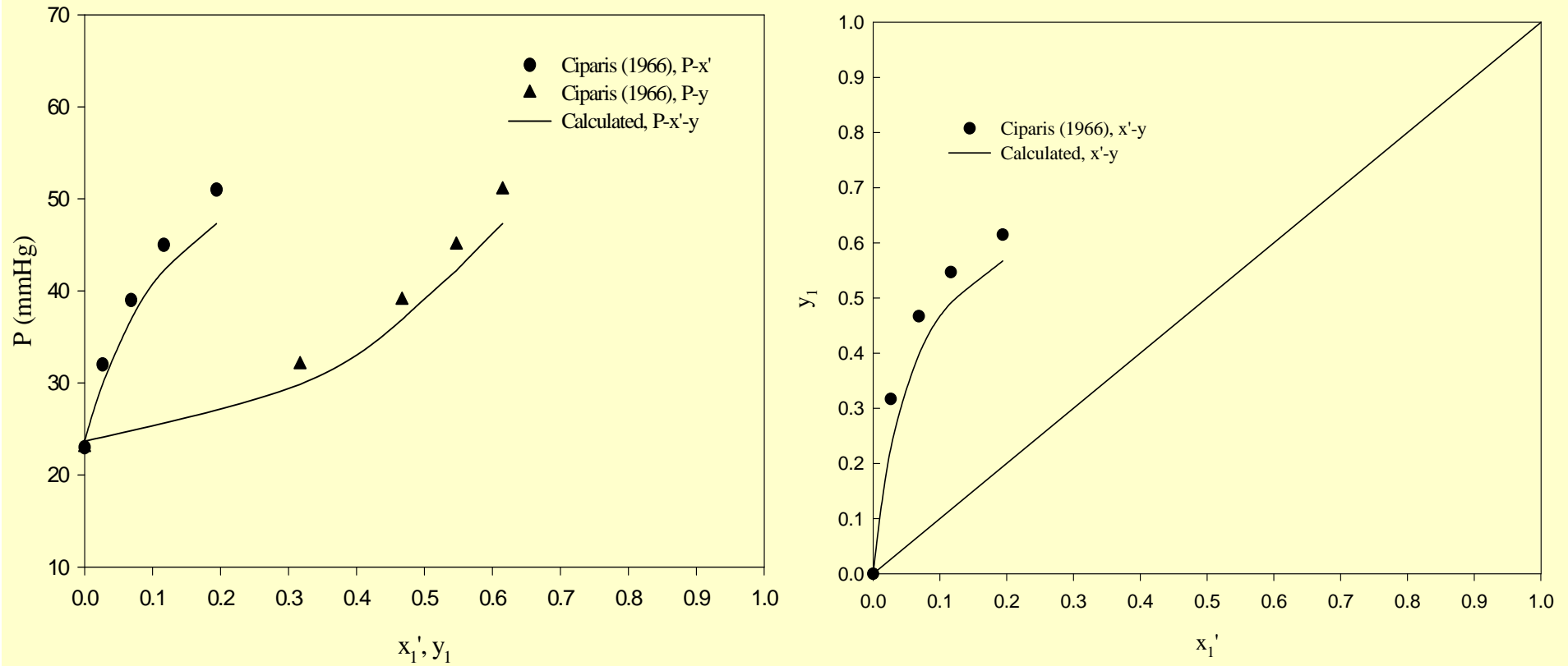


Fig.5-10 P- x_1' - y_1 for EtOH(1)-H₂O(2)-Na₂SO₄(3) VLE at 298.15K.

Results : Isothermal VLE

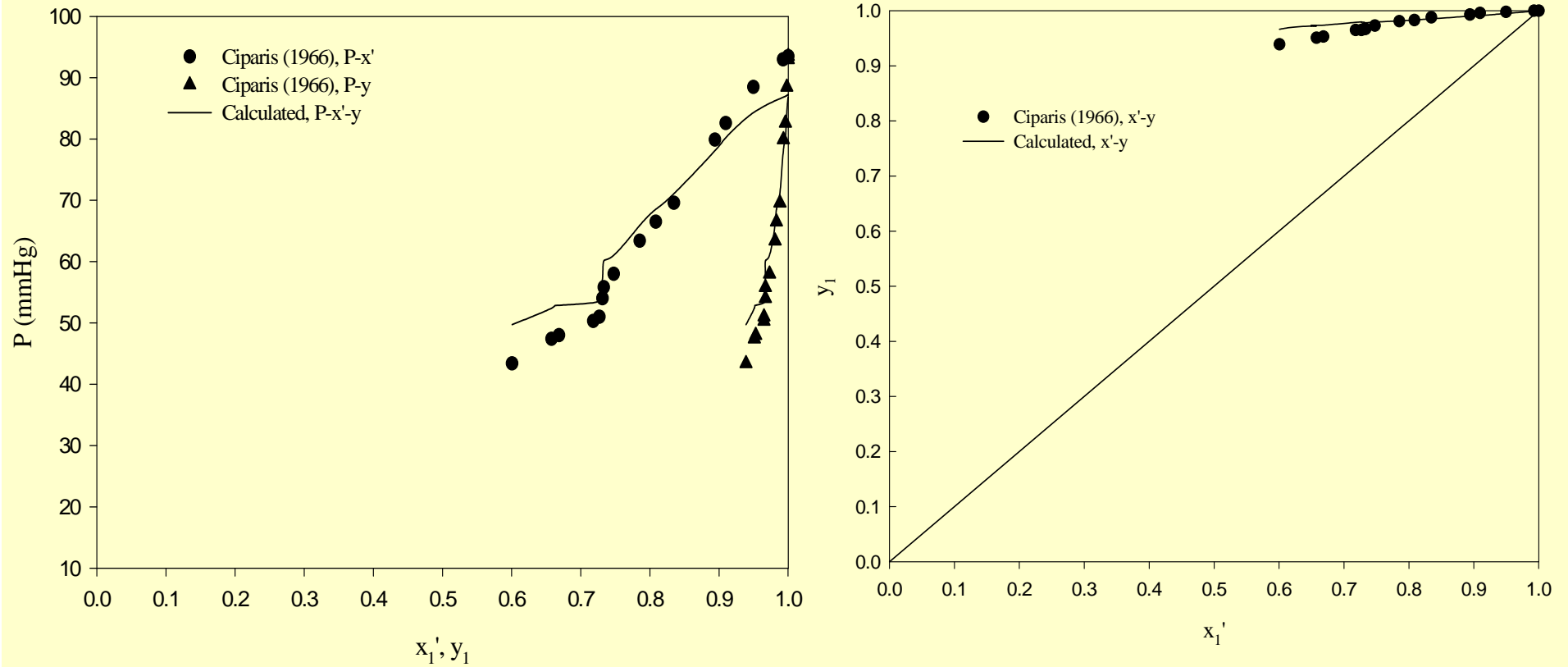


Fig.5-11 P - x' - y for MeOH(1)-H₂O(2)-CaCl₂(3) VLE at 298.15K.

Results : Isothermal VLE

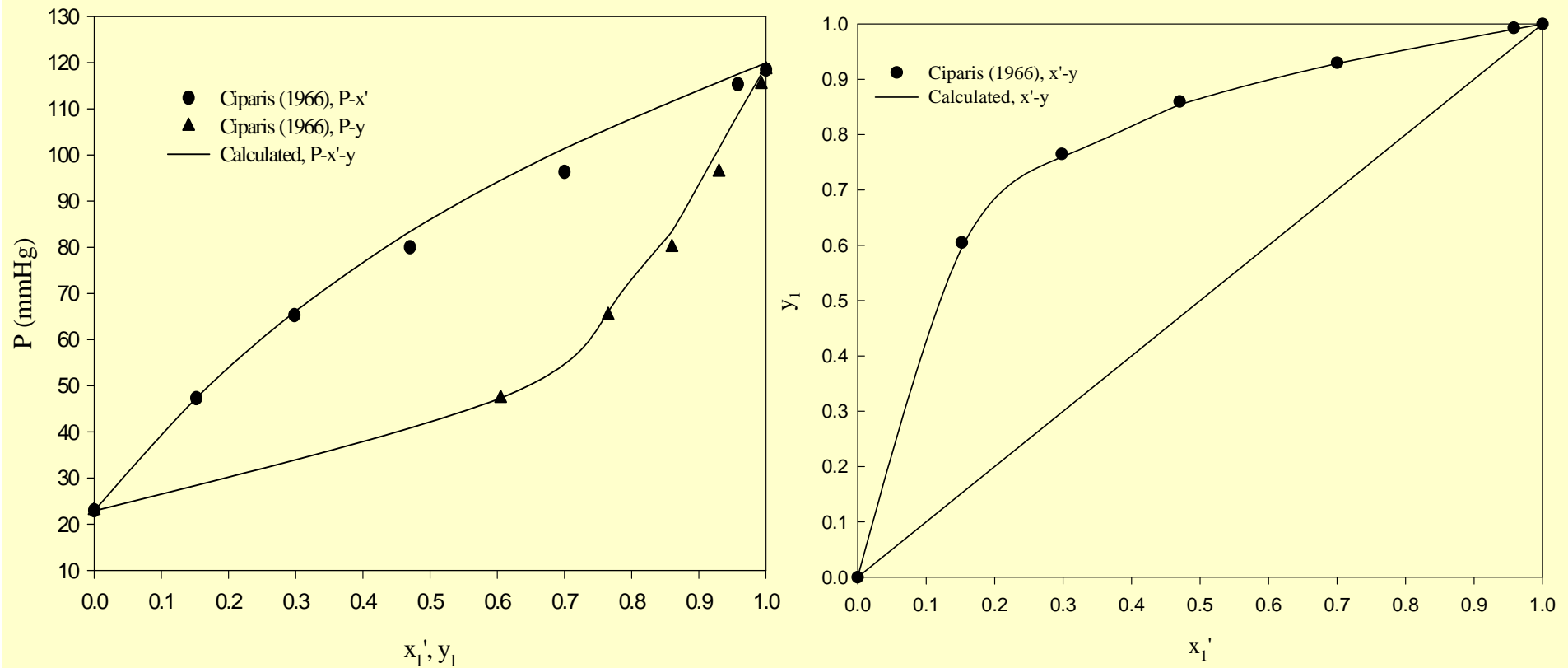


Fig.5-12 $P-x'-y$ for MeOH(1)-H₂O(2)-LiCl(3) VLE at 298.15K.
 $m(\text{LiCl})=1.0 \text{ mol/kg}$

Results : Isothermal VLE

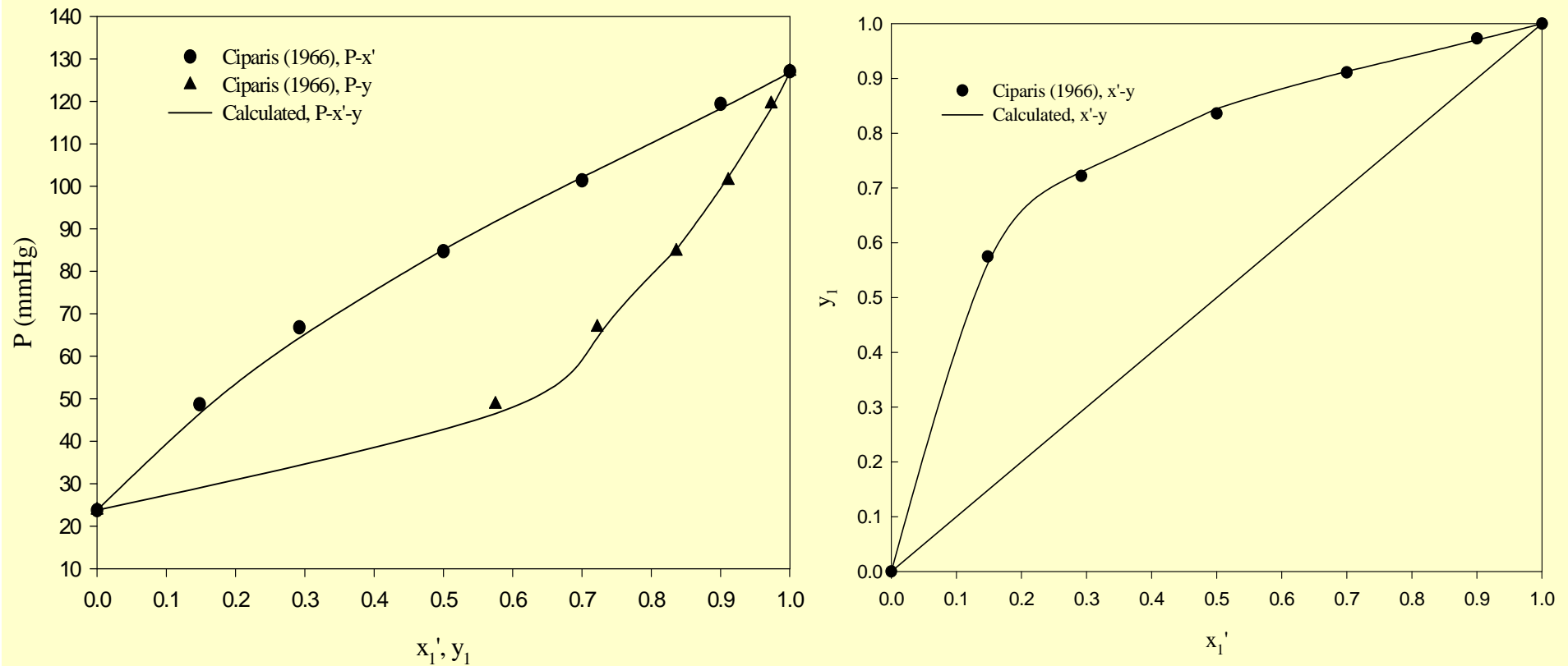


Fig.5-13 $P-x'-y$ for MeOH(1)-H₂O(2)-NaBr(3) VLE at 298.15K.
 $m(\text{LiCl})=0.0$ mol/kg.

Results : Isothermal VLE

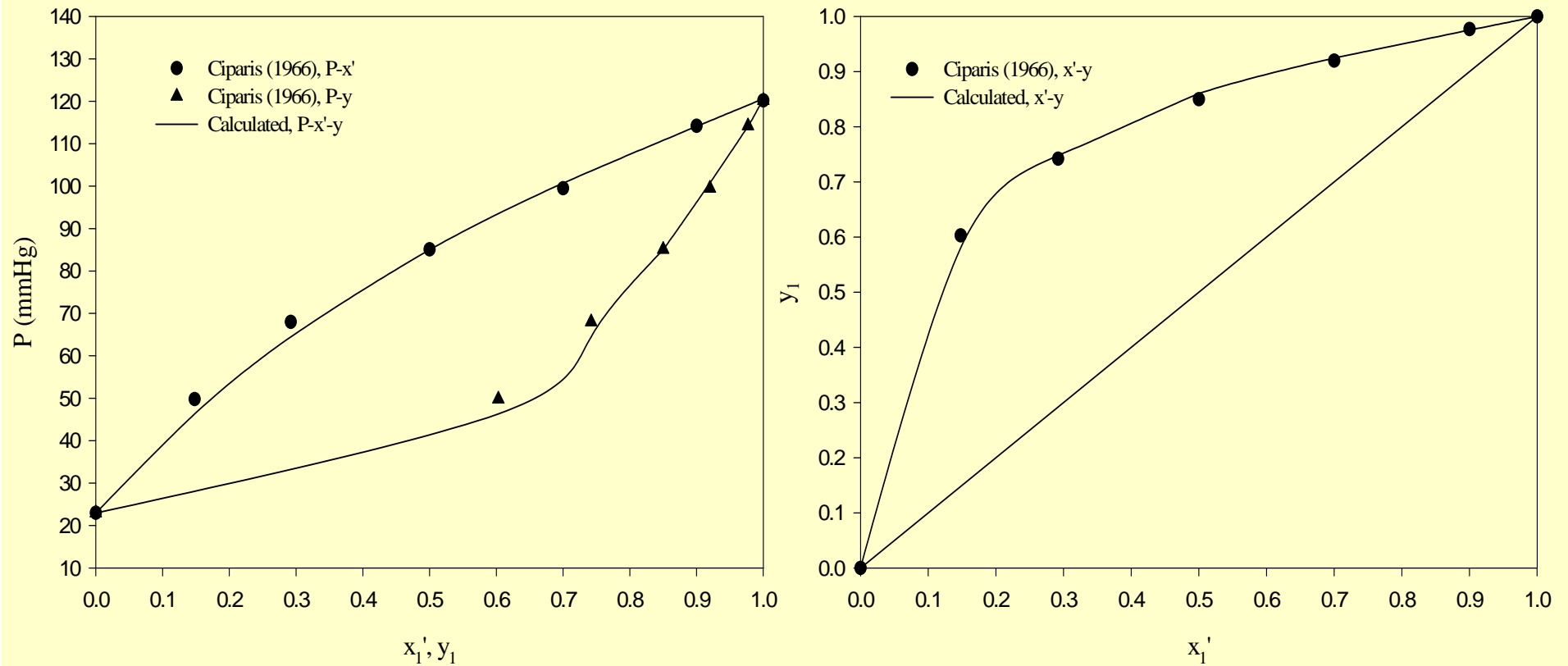


Fig.5-14 $P-x'-y$ for MeOH(1)-H₂O(2)-NaBr(3) VLE at 298.15K.
 $m(\text{LiCl})=1.0 \text{ mol/kg}$.

Results : Isothermal VLE

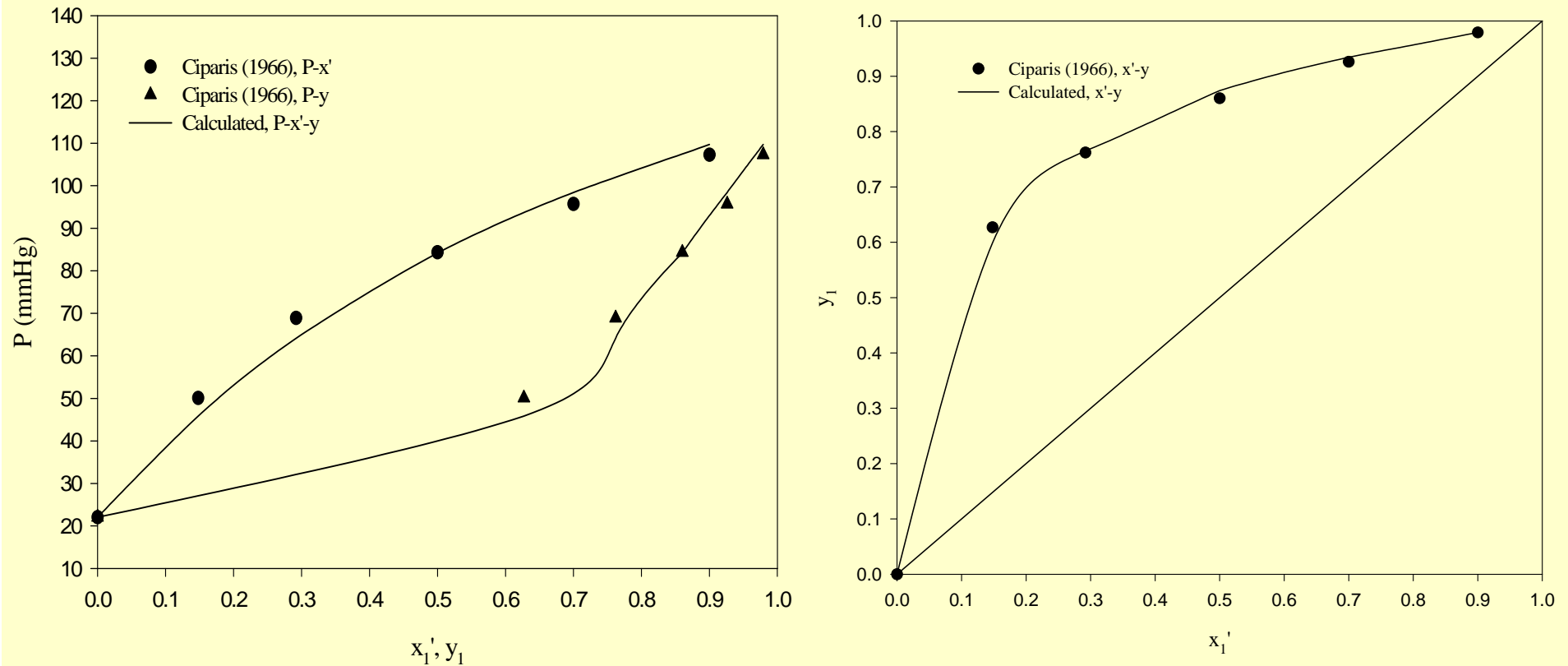


Fig.5-15 P - x' - y for MeOH(1)-H₂O(2)-NaBr(3) VLE at 298.15K.
 $m(\text{LiCl})=2.0$ mol/kg.

Results : Isothermal VLE

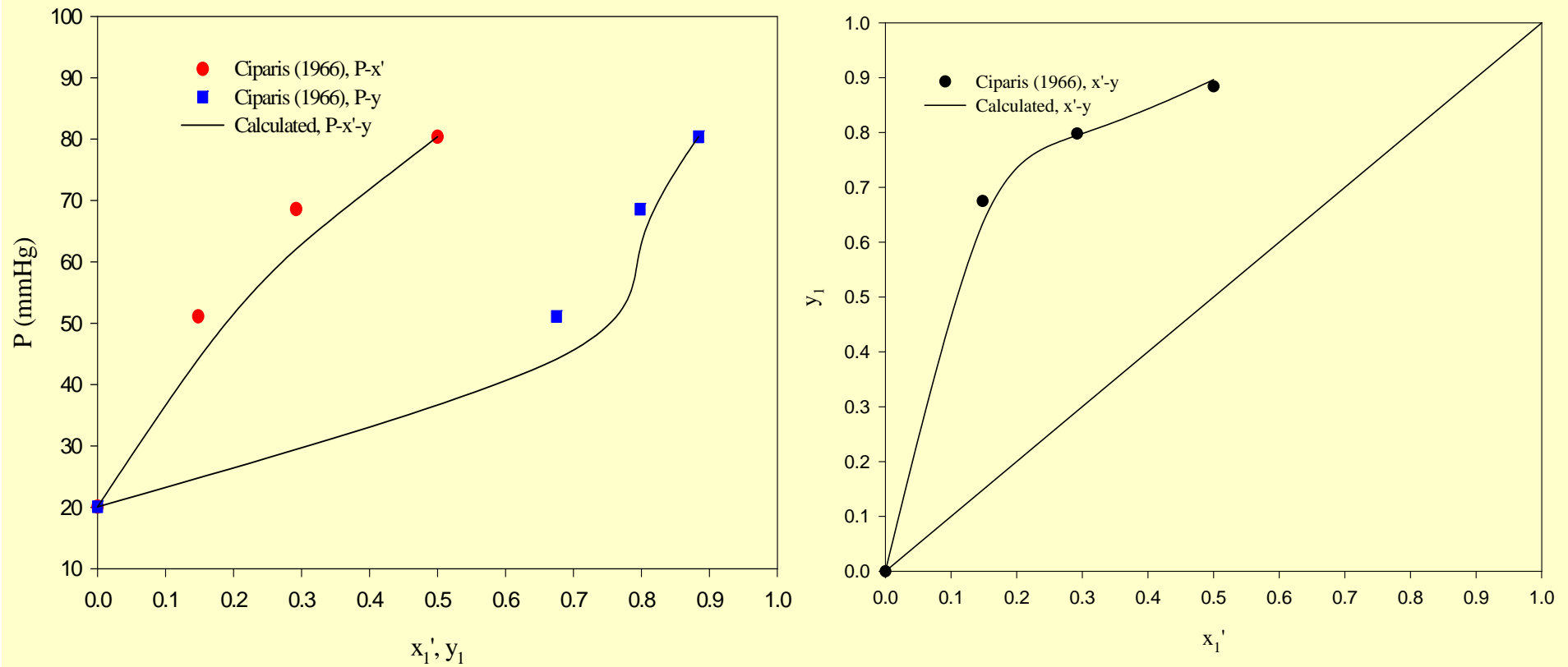


Fig.5-16 P-x'-y for MeOH(1)-H₂O(2)-NaBr(3) VLE at 298.15K.
m(LiCl)=4.0 mol/kg

Results : Isothermal VLE

Table 5-3. Comparison of RMS errors of Isothermal VLE for Ethanol(1)-Water(2)-Electrolyte(3) systems

	σ_y	σ_p/mmHg
CaCl ₂	0.03	2.8
(m=0.0)	0.01	0.8
(m=0.5)	0.01	0.7
LiCl	0.01	0.3
(m=1.0)	0.01	0.3
(m=4.0)	0.01	6.2
MgSO ₄	0.02	1.4
Na ₂ SO ₄	0.08	3.4
Average	0.02	2.2

Results : Isothermal VLE

Table 5-4. Comparison of RMS errors of Isothermal VLE for Methanol(1)-Water(2)-Electrolyte(3) systems

	σ_y	σ_p/mmHg
CaCl ₂	0.01	3.7
LiCl	0.003	1.8
(m=0.0)	0.005	1.0
(m=1.0)	0.006	1.3
NaBr	0.009	2.4
(m=4.0)	0.14	3.4
Average	0.03	2.3

Results : Isobaric VLE

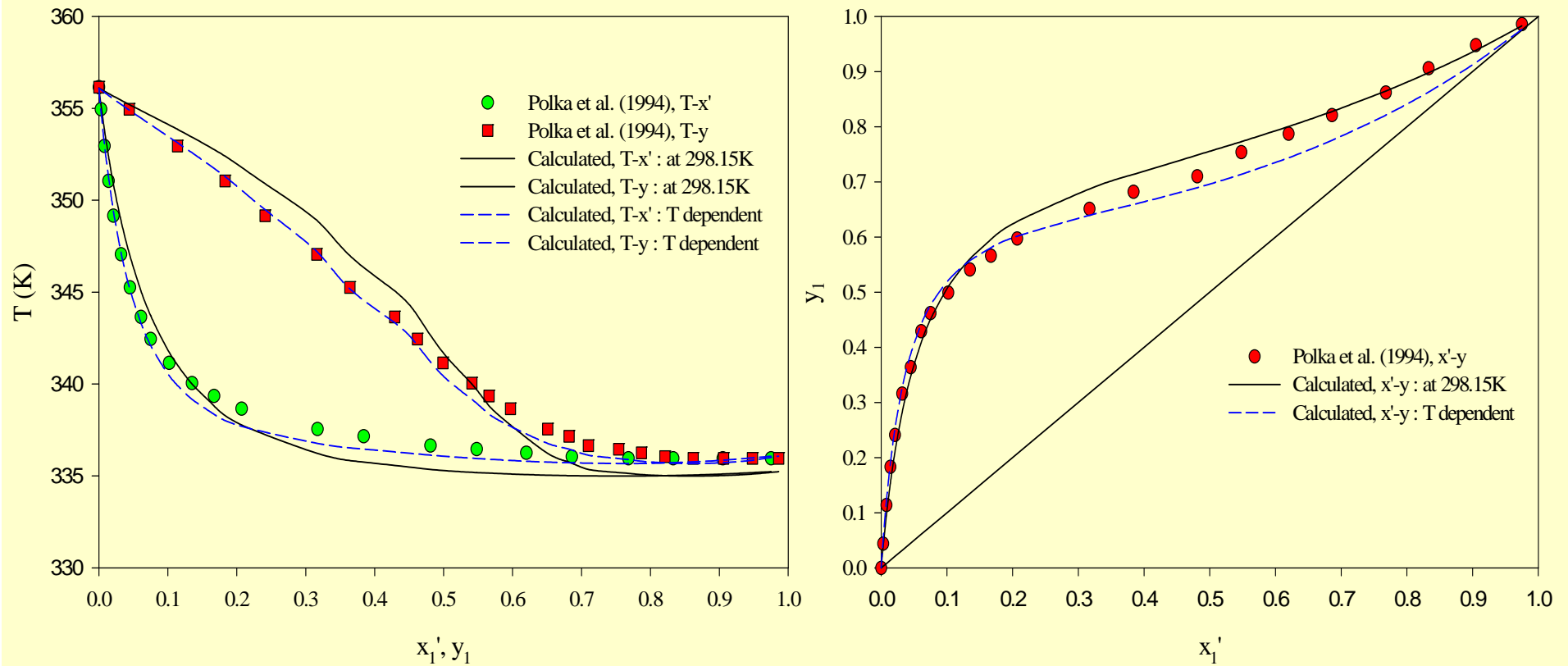


Fig.5-21 T-x'-y for EtOH(1)-H₂O(2)-Ca(NO₃)₂(3) VLE at 50.66kPa.
 $m(\text{Ca}(\text{NO}_3)_2)=1.038 \text{ mol/kg}$

Results : Isobaric VLE

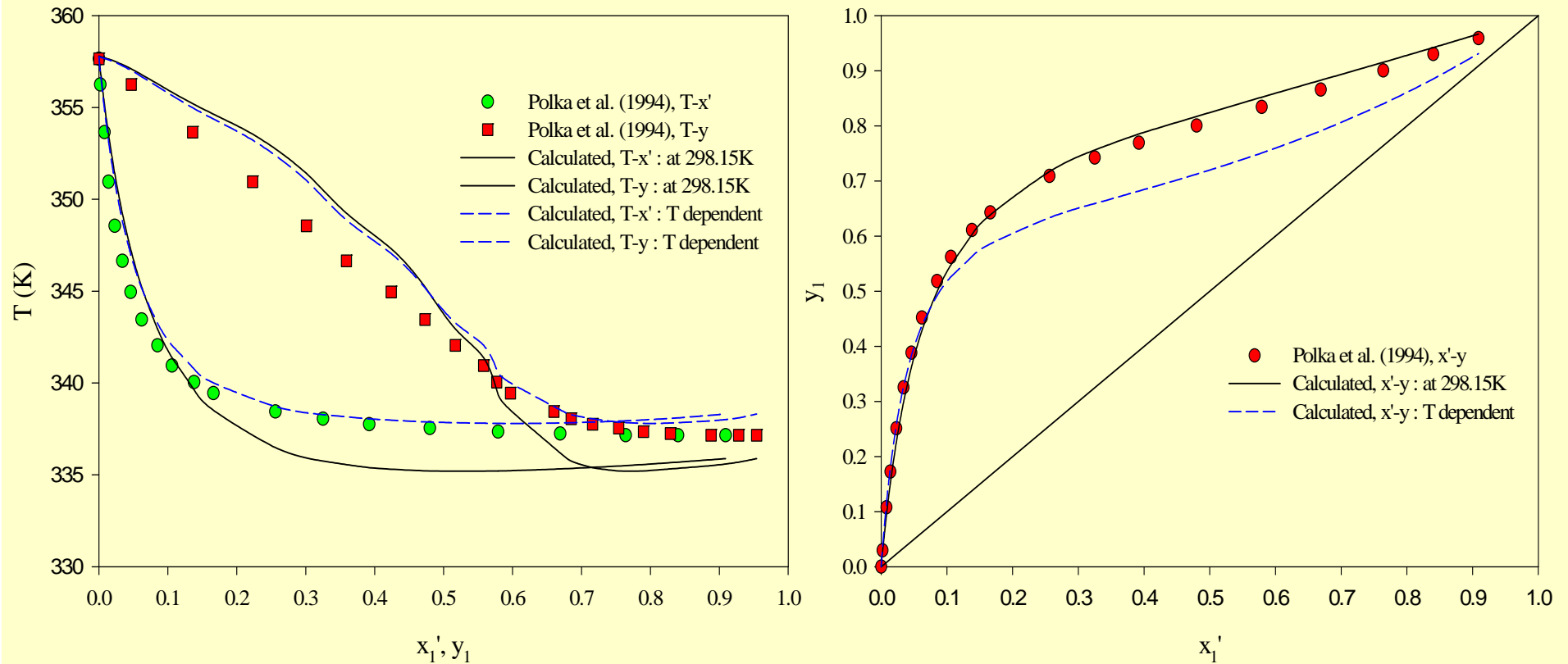


Fig.5-22 T-x'-y for EtOH(1)-H₂O(2)-Ca(NO₃)₂(3) VLE at 50.66kPa.
 $m(\text{Ca}(\text{NO}_3)_2)=2.049 \text{ mol/kg}$

Results : Isobaric VLE

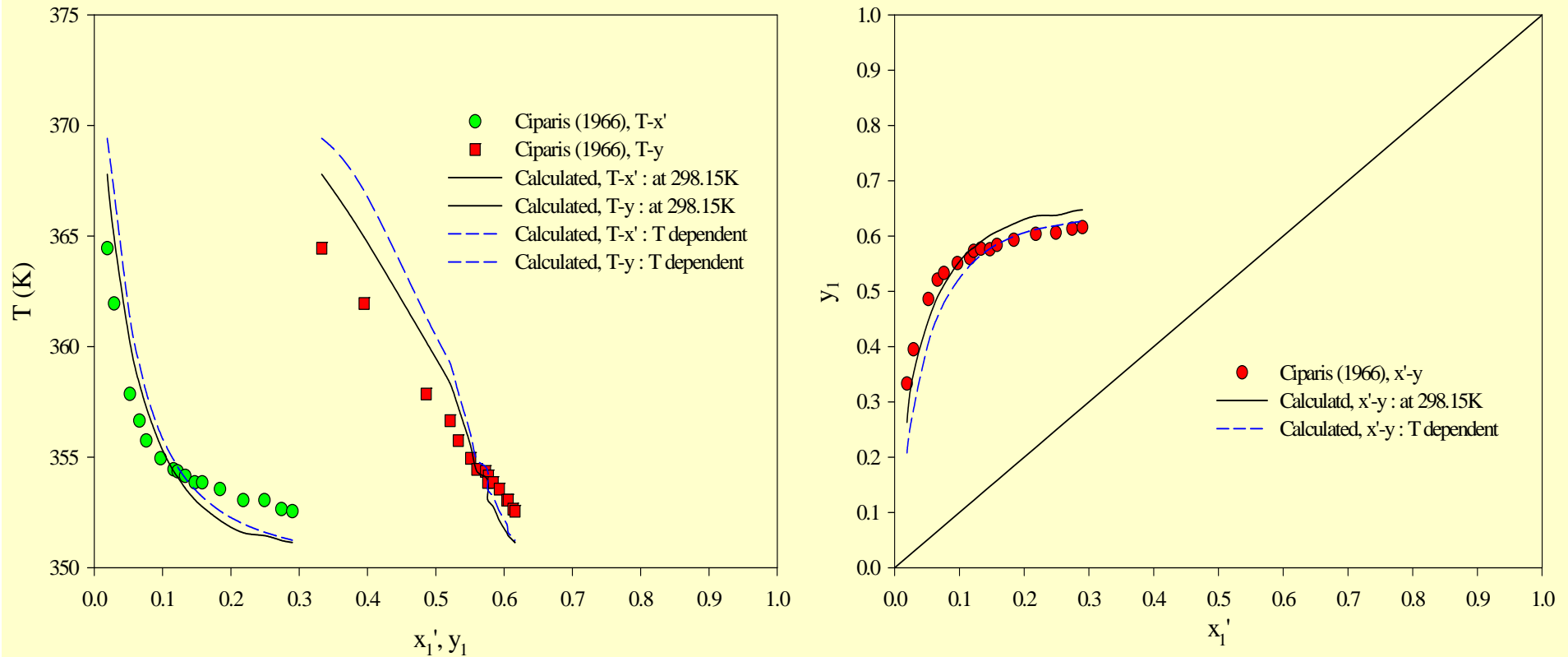


Fig.5-17 EtOH(1)-H₂O(2)-BaCl₂(3) VLE at 700mmHg.

Results : Isobaric VLE

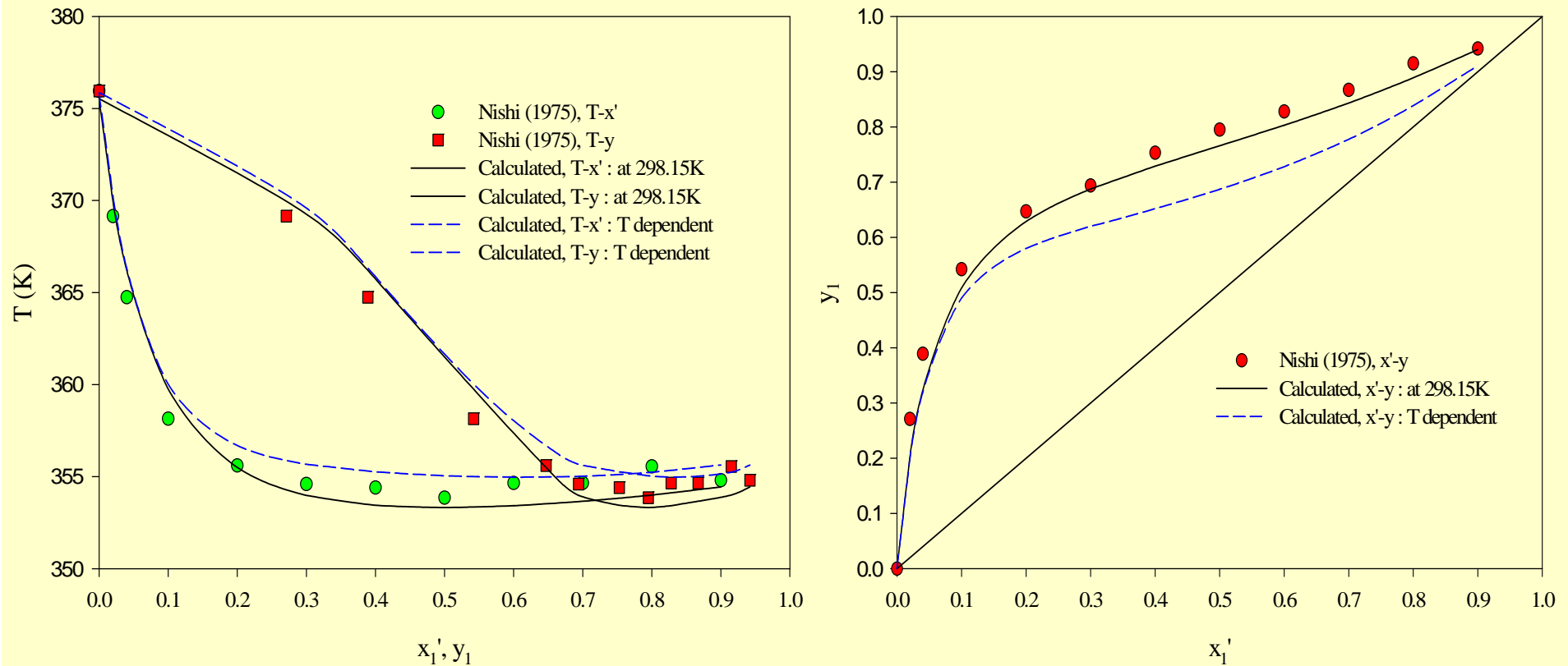


Fig.5-18 T-x'-y for EtOH(1)-H₂O(2)-CaCl₂(3) VLE at 1 atm.
 $m(\text{CaCl}_2)=1.505 \text{ mol/kg}$

Results : Isobaric VLE

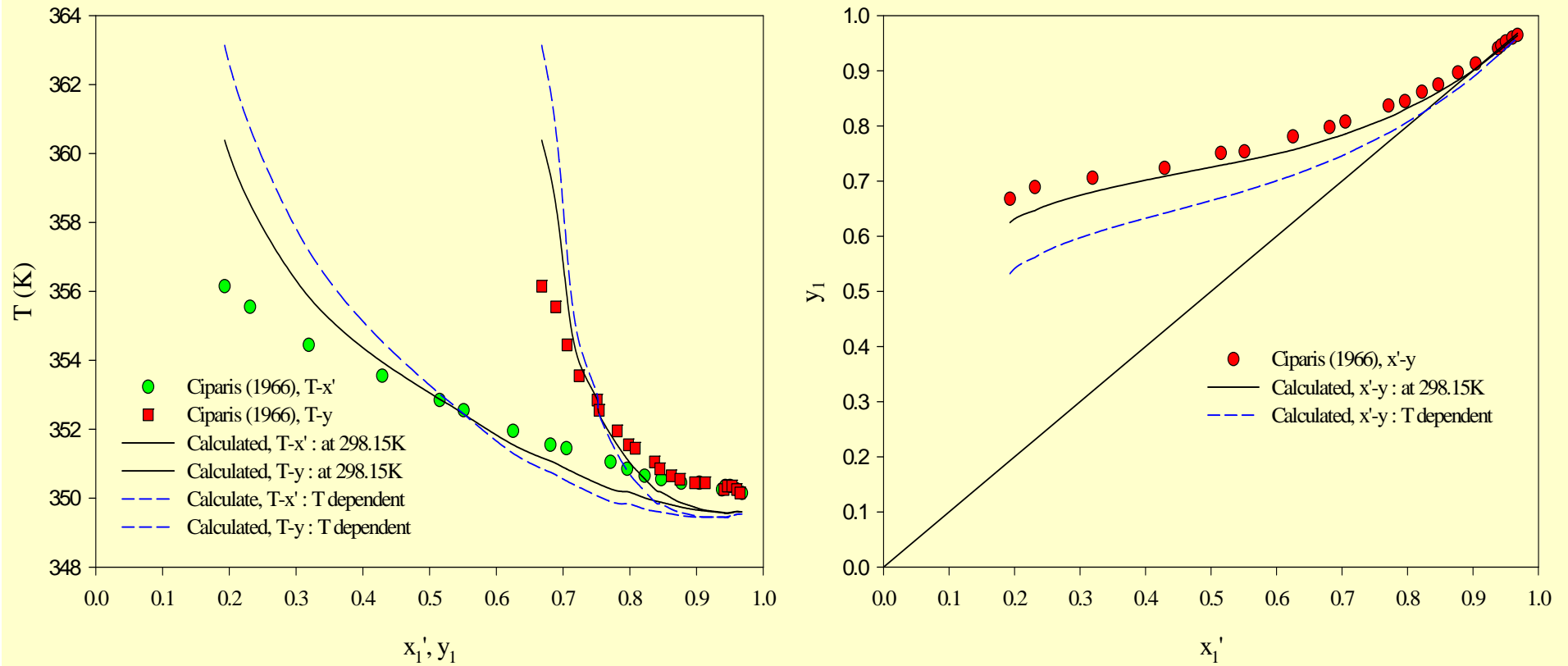


Fig.5-19 T - x' - y for EtOH(1)-H₂O(2)-KI(3) VLE at 700mmHg.

Results : Isobaric VLE

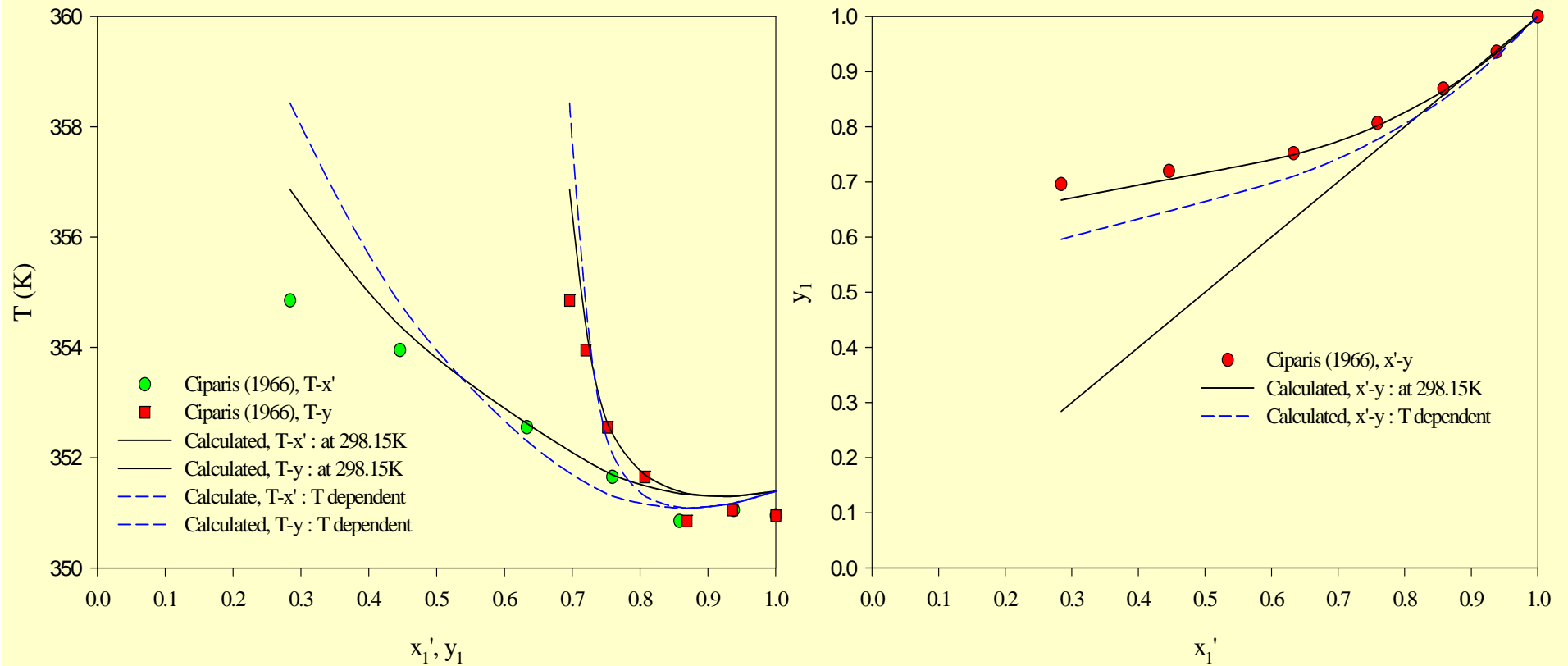


Fig.5-20 T-x'-y for EtOH(1)-H₂O(2)-NH₄Cl(3) VLE at 754mmHg.

Results : Isobaric VLE

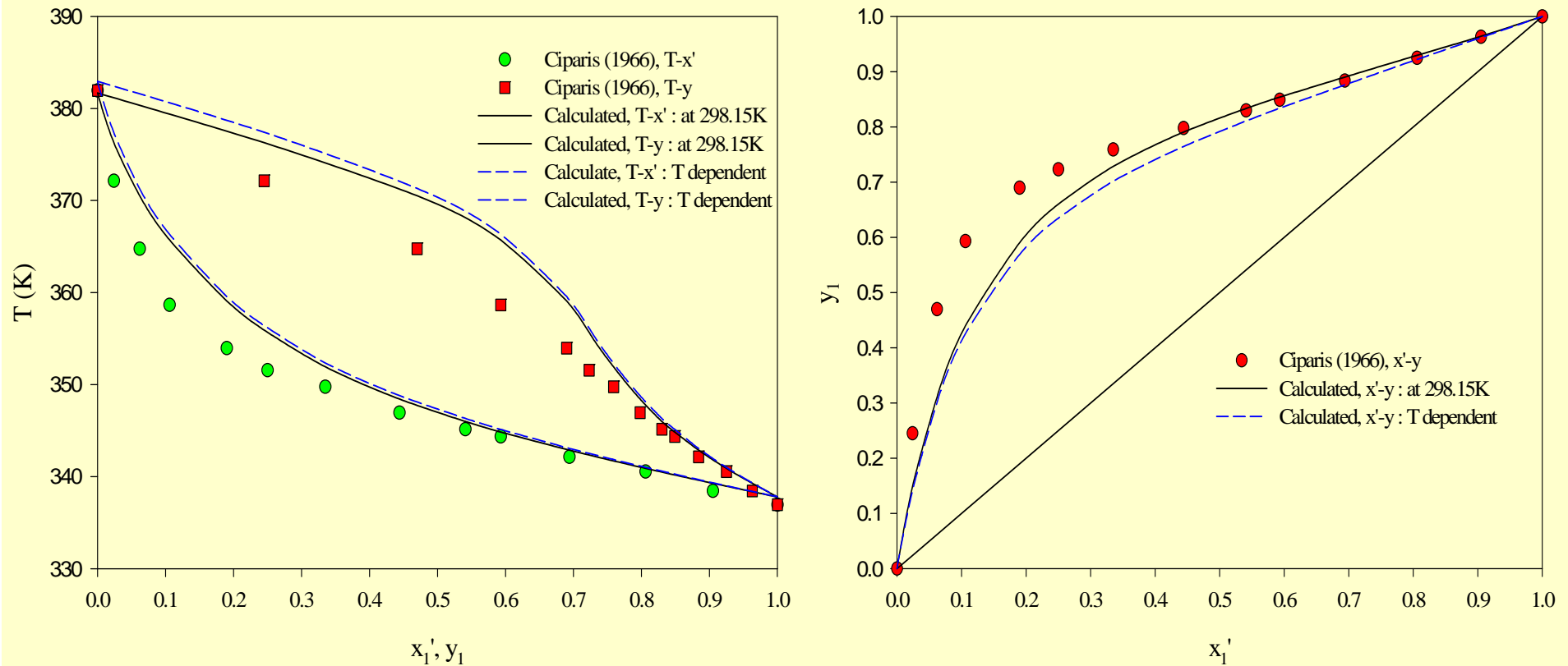


Fig.5-23 T-x'-y for MeOH(1)-H₂O(2)-KCl(3) VLE at 760mmHg.

Results : Isobaric VLE

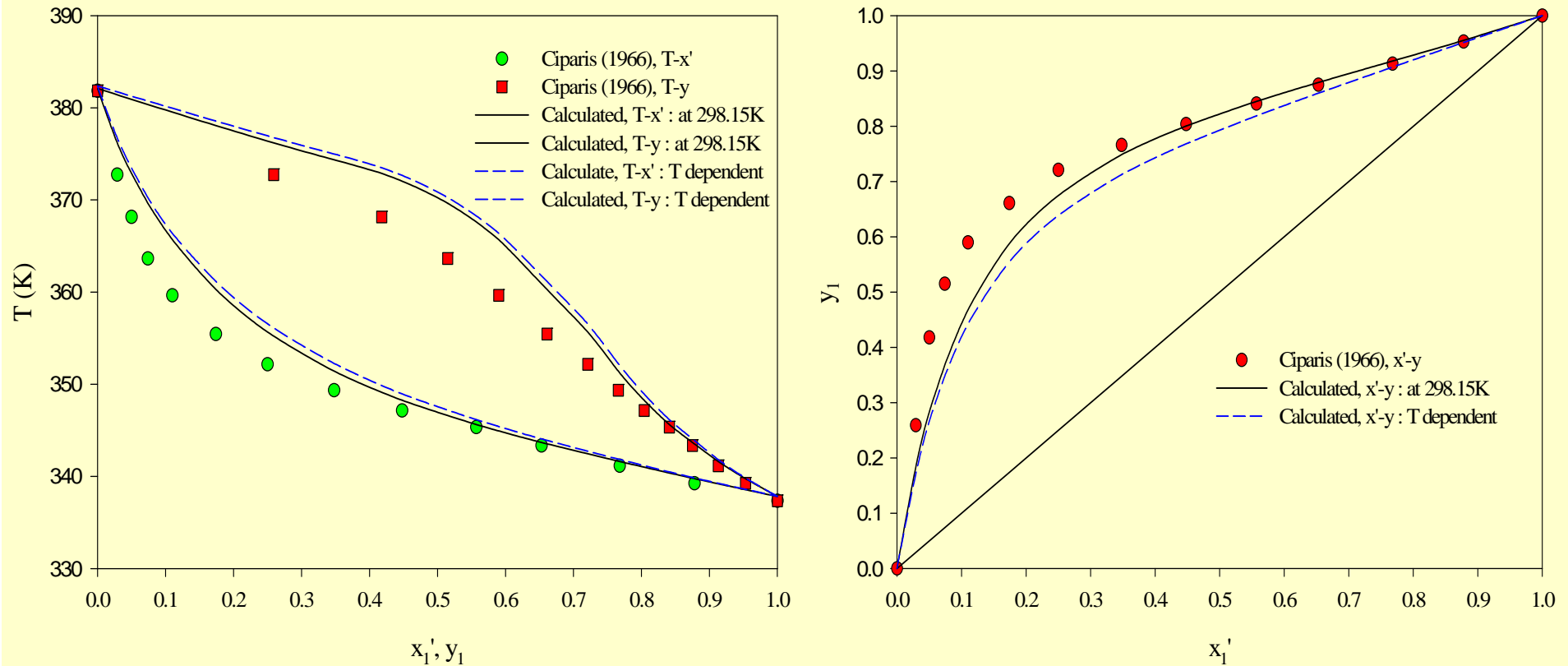


Fig.5-24 T-x'-y for MeOH(1)-H₂O(2)-NaCl(3) VLE at 762mmHg.

Results : Isobaric VLE

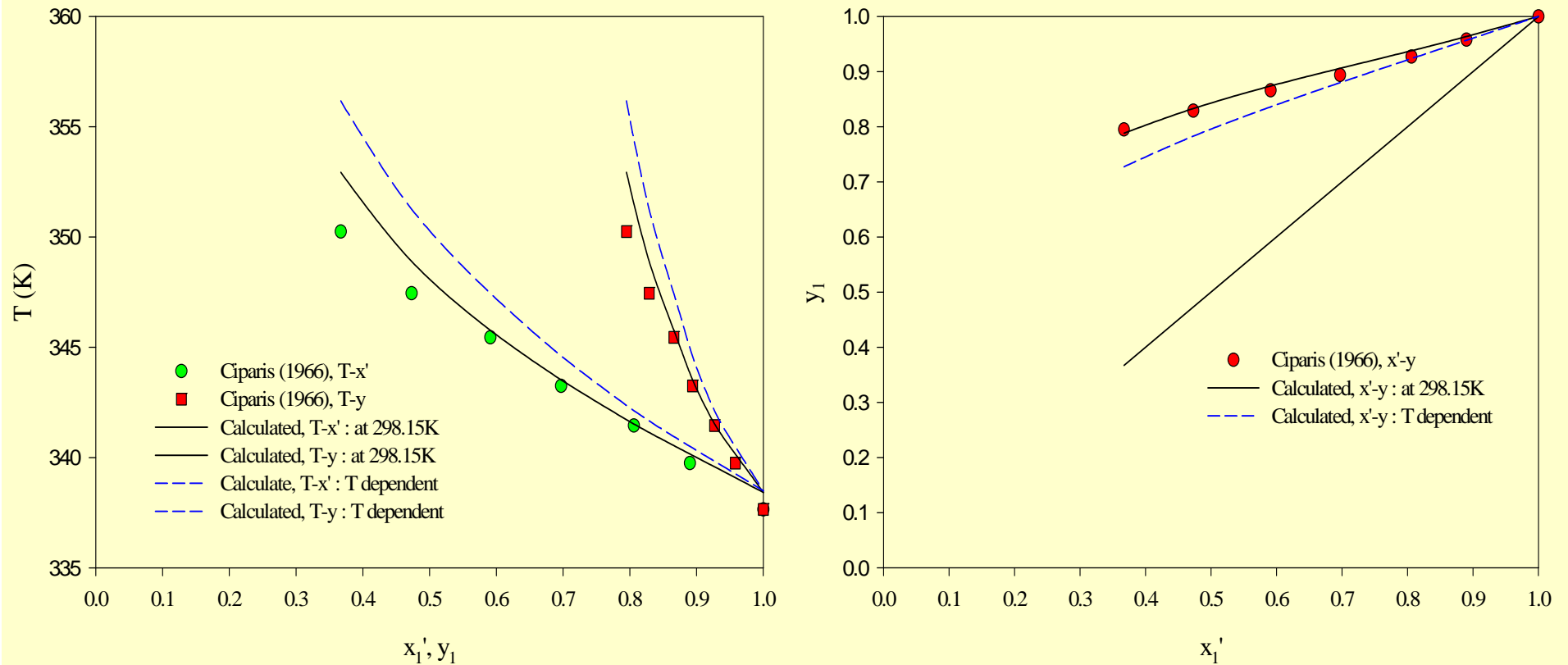


Fig.5-25 T-x'-y for MeOH(1)-H₂O(2)-NH₄Cl(3) VLE at 755mmHg.

Results : Isobaric VLE

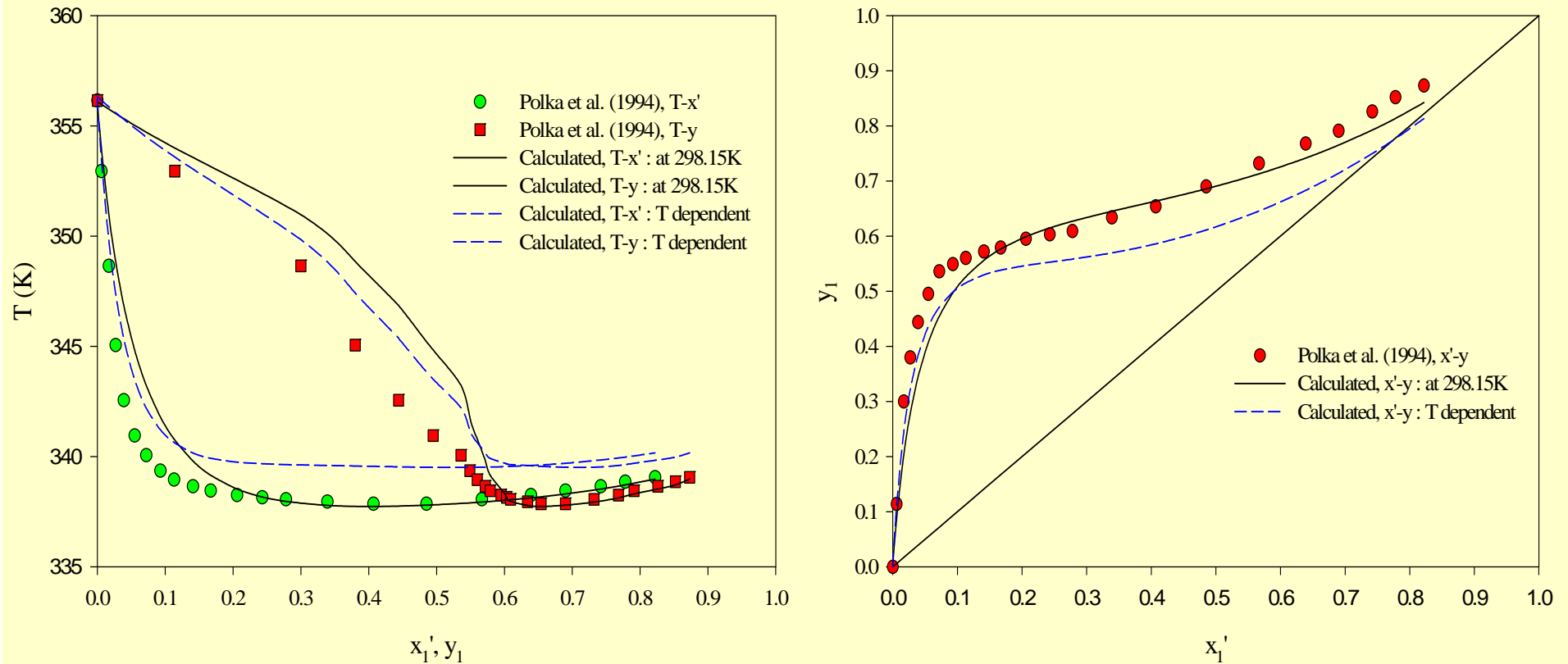


Fig.5-26 T-x'-y for Pr-2-OH(1)-H₂O(2)-Ca(NO₃)₂(3) VLE at 50.66kPa.
 $m(\text{Ca}(\text{NO}_3)_2)=1.038 \text{ mol/kg}$

Results : Isobaric VLE

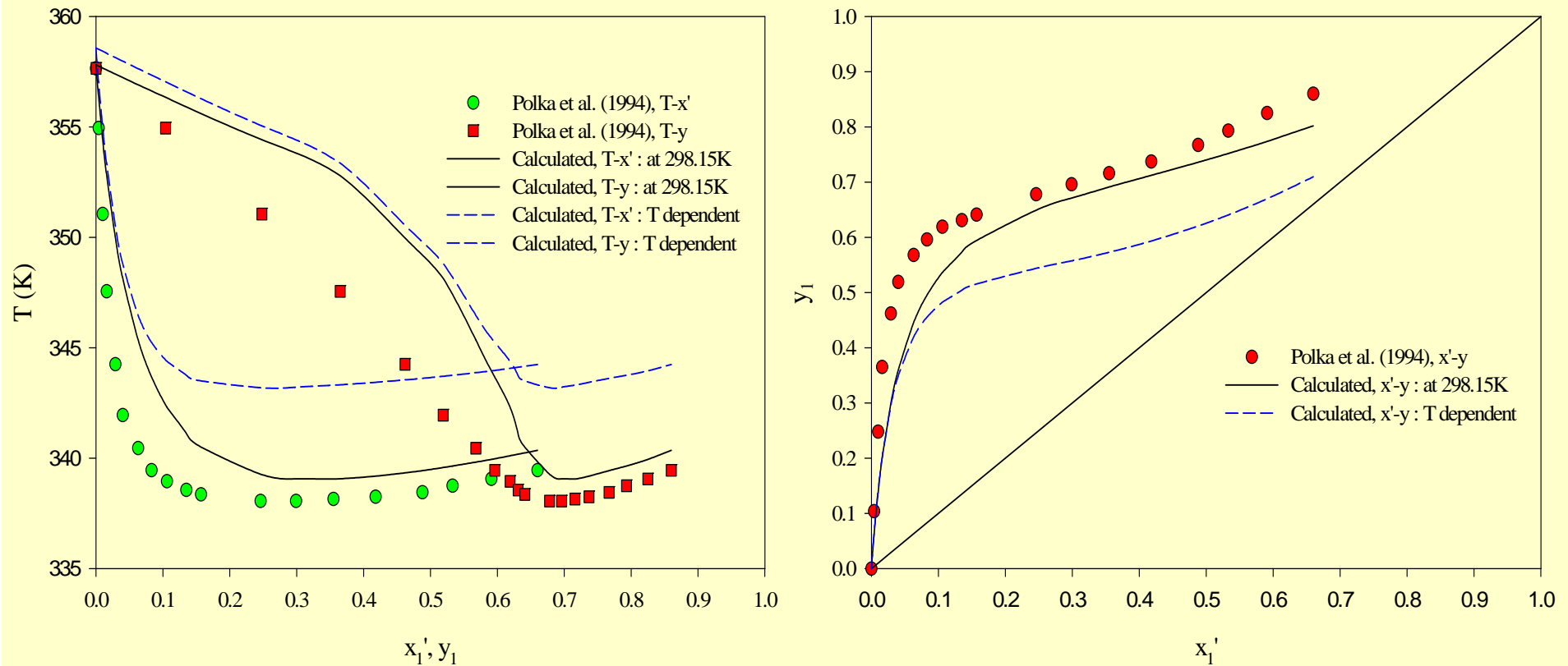


Fig.5-27 T-x'-y for Pr-2-OH(1)-H₂O(2)-Ca(NO₃)₂(3) VLE at 50.66kPa.
 $m(\text{Ca}(\text{NO}_3)_2)=2.073 \text{ mol/kg}$

Results : Isobaric VLE

Table 5-5. Comparison of RMS errors of Isobaric VLE for Ethanol(1)-Water(2)-Electrolyte(3) systems

	Fixed		T dependent	
	σ_y	σ_T/K	σ_y	σ_T/K
BaCl ₂	0.07	1.9	0.06	1.9
CaCl ₂	0.03	0.9	0.07	0.9
Ca(NO ₃) ₂ (m=1.308)	0.02	1.0	0.02	0.4
Ca(NO ₃) ₂ (m=2.049)	0.03	1.7	0.03	1.0
KCl (1)	0.06	2.5	0.07	2.6
KCl (2)	0.07	3.4	0.08	3.4
KI	0.02	0.9	0.05	1.4
KNO ₃	0.14	5.9	0.16	5.5
NaCl (1)	0.06	2.7	0.08	3.1
NaCl (2)	0.06	2.9	0.08	3.4
NaI	0.02	0.5	0.06	0.6
NaNO ₃	0.04	1.3	0.05	1.6
NH ₄ Cl	0.008	0.5	0.04	0.8
SrBr ₂	0.02	0.8	0.05	0.8
SrCl ₂	0.03	1.3	0.06	1.6
Sr(NO ₃) ₂	0.05	1.6	0.03	1.2
Average	0.04	1.9	0.06	1.9

Results : Isobaric VLE

Table 5-6. Comparison of RMS errors of Isobaric VLE for Methanol(1)-Water(2)-Electrolyte(3) systems

	Fixed		T dependent	
	σ_y	σ_T/K	σ_y	σ_T/K
KCl	0.05	2.7	0.06	3.1
NaCl	0.05	2.6	0.07	3.1
NH ₄ Cl	0.01	1.1	0.02	2.4
Average	0.04	2.1	0.05	2.9

Results : Isobaric VLE

Table 5-7. Comparison of RMS errors of Isobaric VLE for 1-Propanol(1)-Water(2)-Electrolyte(3) systems

	Fixed		T dependent	
	σ_y	σ_T/K	σ_y	σ_T/K
(x3=0.02)	0.03	0.8	0.07	1.3
(x3=0.04)	0.03	0.8	0.11	2.5
Ca(NO ₃) ₂ (x3=0.06)	0.02	0.3	0.08	1.8
(x3=0.08)	0.02	0.3	0.06	2.3
(x3=0.10)	0.01	0.5	0.01	1.2
KBr	0.03	2.3	0.10	4.4
KCl	0.03	0.9	0.07	2.2
NaBr	0.06	2.4	0.15	5.1
NaCl (1)	0.02	1.0	0.06	2.7
NaCl (2)	0.03	1.9	0.09	4.0
Average	0.03	1.1	0.08	2.8

Results : Isobaric VLE

Table 5-9. Comparison of RMS errors of Isobaric VLE for 2-Propanol(1)-Water(2)-Electrolyte(3) systems

		Fixed		T dependent	
		σ_y	σ_T/K	σ_y	σ_T/K
Ca(NO ₃) ₂	(m=1.308)	0.04	1.1	0.06	1.5
	(m=2.073)	0.07	2.5	0.13	4.9
	LiBr (1)	0.04	2.2	0.09	3.6
	LiCl (2)	0.04	1.6	0.09	2.9
Average		0.05	1.9	0.09	3.2

Electrolyte Solution Based on Solvation

Previous Models

▶ G^E Model

- Debye-Hückel (1923), Bromley (1973), Pitzer (1973)

Meissner & Tester (1972), Chen et al. (1982)

▶ Primitive Model

- Waisman et al. (1972), Blum (1975), Harvey et al. (1989), Taghikhani et al. (2000)

▶ Nonprimitive Model

- Planche et al. (1981), Ball et al. (1985),
Fürst et al. (1993), Zuo et al. (1998)

▶ Acceptable accuracy up to $I=6.0$ or less

Hydration Theory

G^E model

- Ghosh and Patwardhan (1990)

- ▶ Based on lithium chloride as a reference electrolyte
- ▶ Hydration energy, function of the total moles of water hydrated per kg of solution
 - Fitted with experimental ϕ , γ
- ▶ Up to $I=24$ for 150 electrolyte solutions

- Schoenert (1990, 1991, 1993, 1994)

- ▶ Modified hydration model of Robinson and Stokes
- ▶ Hydration of ions : ligand-binding equilibria
 - Transfer of water to the hydration spheres of ions
- ▶ Up to $m=1$ for HCl, LiCl, NaCl, KCl, CsCl, NH₄Cl, NaBr

Hydration Model

SAFT Approach

- **Gil-Villegas et al. (2001)**
 - ▶ Ionic contribution : MSA
 - ▶ Monomer : perturbation expansion
 - ▶ Association : Solvent-solvent, solvent-ion, ion-ion pairing
 - ▶ Applied to the NaCl solution up to 10 m
- **Paricaud et al. (2001)**
 - ▶ Applied to the NaOH solution up to 22 m

In present work

- ▶ Solvation contribution from the Veytsman statistics
Explicitly added to Lee et al. model
- ▶ Application to LiCl, LiBr, LiI and LiClO₄ solutions

Excess Gibbs Function

- **Long-range + Physical + Solvation**

$$G^E = G_{DH}^E + G_A^E + G_R^E + G_{HB}^E$$

- ▶ **In high pressure limit, holes are vanished**

$$A^E(T, P = \infty, x_i) = A^E(T, low P, x_i) = G^E(T, low P, x_i)$$

- ▶ **Physical interaction : Athermal + Residual**
From Lee et al. model (1996)

- ▶ **Solvation interaction**
From a normalized Veytsman statistics
(Park et al., 2001)

Activity Coefficient

- For solvent in symmetric convention

$$\ln \gamma_j = \ln \gamma_{DH,j} + \ln \gamma_{A,j} + \ln \gamma_{R,j} + \ln \gamma_{HB,j}$$

- For solute in asymmetric convention

$$\ln \gamma_j^* = \ln \gamma_j - \lim_{x_i \rightarrow 0} \ln \gamma_j$$

$$\ln \gamma_{\pm i}^* = \ln \gamma_{DH,\pm i}^* + \ln \gamma_{A,\pm i}^* + \ln \gamma_{R,\pm i}^* + \ln \gamma_{HB,\pm i}^*$$

Solvation Contribution

- For solvent,

$$\ln \gamma_{HB,k} = -\sum_i^m d_k^i \ln \frac{N_{i0}^k N_{i0}^0}{N_{i0} N_{i0}^{k,0}} - \sum_j^n a_k^j \ln \frac{N_{0j}^k N_{0j}^0}{N_{0j} N_{0j}^{k,0}}$$

- For solute,

$$\ln \gamma_{HB,\pm k}^* = -\frac{v_{+k}}{v_{\pm k}} \sum_i^m d_k^i \ln \frac{N_{i0}^0 N_{i0}^\infty}{N_{i0} N_{i0}^{0,\infty}} - \frac{v_{-k}}{v_{\pm k}} \sum_j^n a_k^j \ln \frac{N_{0j}^0 N_{0j}^\infty}{N_{0j} N_{0j}^{0,\infty}}$$

$$N_{i0}^{HB} = N_d^i - \sum_j^n N_{ij}^{HB}, \quad N_{0j}^{HB} = N_a^j - \sum_i^m N_{ij}^{HB}$$

- ▶ N_{ij}^{HB} : the number of proton donor-acceptor pair for hydrogen bonding

$$N_{ij}^{HB} N_r = \left(N_d^i - \sum_{j=1}^n N_{ij}^{HB} \right) \left(N_a^j - \sum_i^m N_{ij}^{HB} \right) \exp(-\beta A_{ij}^{HB})$$

- ▶ N_{ij}^0 with $A_{ij}^{HB} = 0$

Parameters

- For physical interaction

- ▶ Size parameter of each ion and water, r_i

- ▶ Energy parameters

- Cation-water & anion-water, $\tau_{13}, \tau_{23}, \tau_{31}, \tau_{32}$

- For solvation

- ▶ Solvation number

- Cation : donor number, d

- Anion : acceptor number, a

- Water : donor & acceptor number ($d=2, a=1$)

- ▶ Solvation energy

- Cation-water & anion-water, A_{13}^{HB}, A_{32}^{HB}

Parameter Determinations

- **Size parameter**
 - ▶ Cation : from crystalline ionic volume
 - ▶ Water : from Lee et al. model (2.5)
- **Solvation number**
 - ▶ From coordination numbers in hydration shells of ions (Krestov et al., 1994)
- **Solvation energy of water : from Luck(1980)**
(-10.55 kJ/mol)
- **Data for solute activity coefficients**
 - ▶ Size parameter of each anion
 - ▶ Energy parameters for physical interaction
 - ▶ Solvation numbers & solvation energy parameters of cation- & anion-water

Results

Table 1. Parameters for Lithium ionic Electrolyte Systems

	r_i	τ_{13} (or τ_{23})	d_{ii} (or a_{ii})	A_{13} (or A_{32}) / kJ mol ⁻¹
Li ⁺	0.1229	0.156	6	-15.61
Cl ⁻	0.615	0.143	5	-4.75
Br ⁻	1.145	1.167	8	-4.70
I ⁻	1.756	1.350	8	-4.45
ClO ₄ ⁻	1.845	1.052	8	-3.85

Results

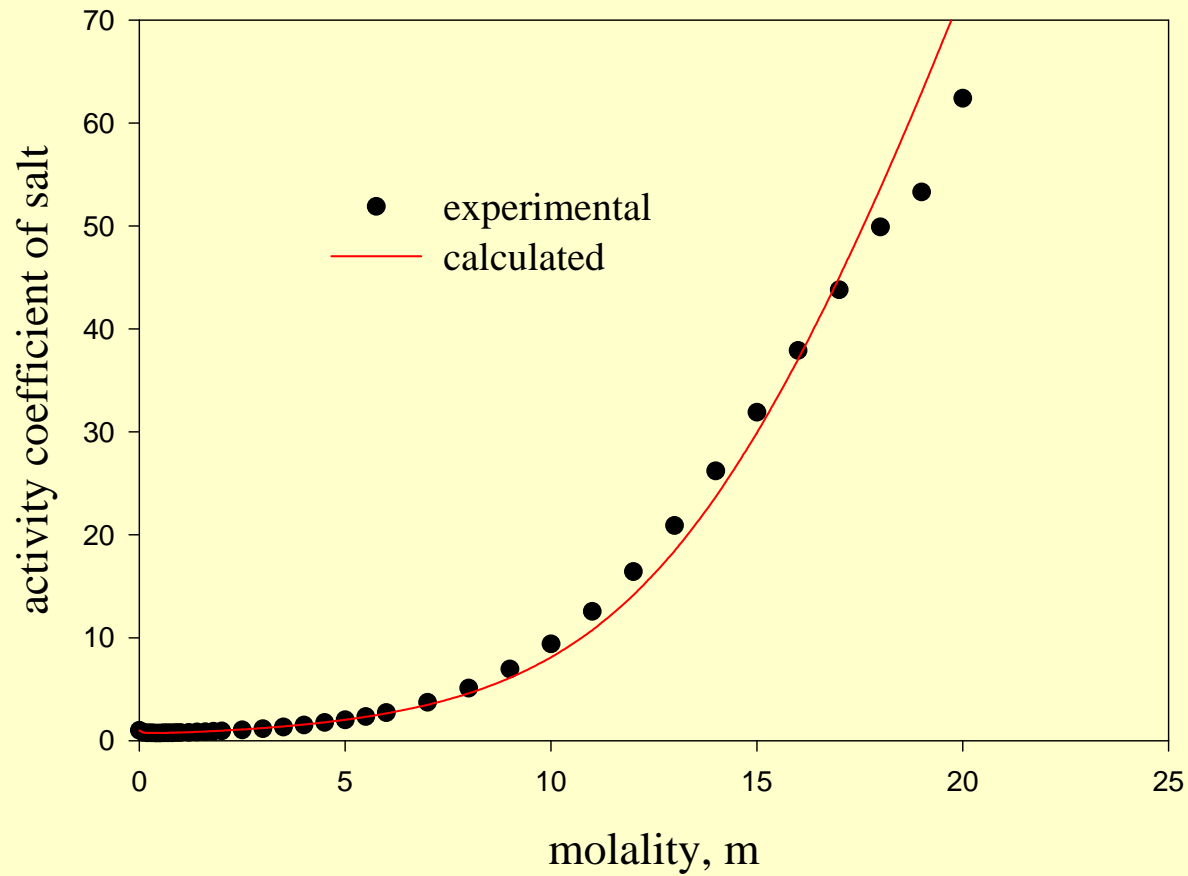


Fig.1 The activity coefficient of LiCl.

Results

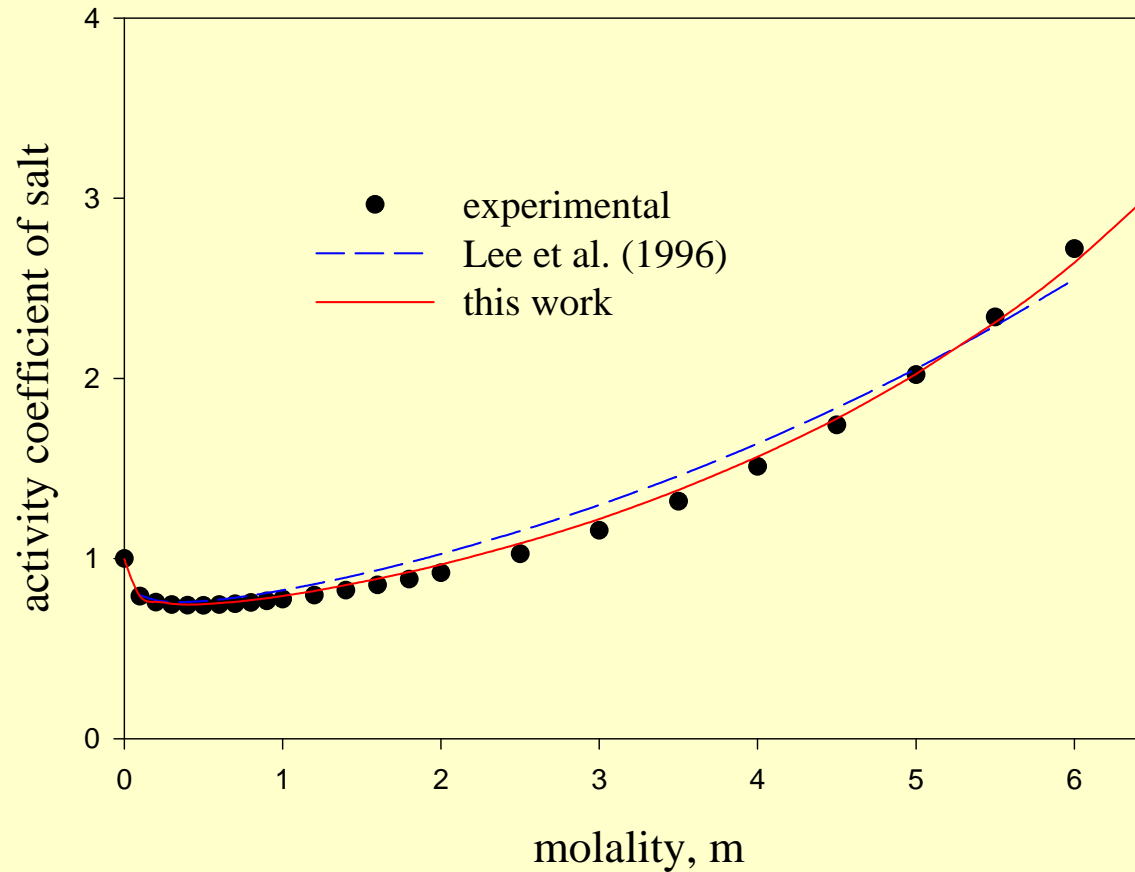


Fig.2 The activity coefficient of LiCl.

Results

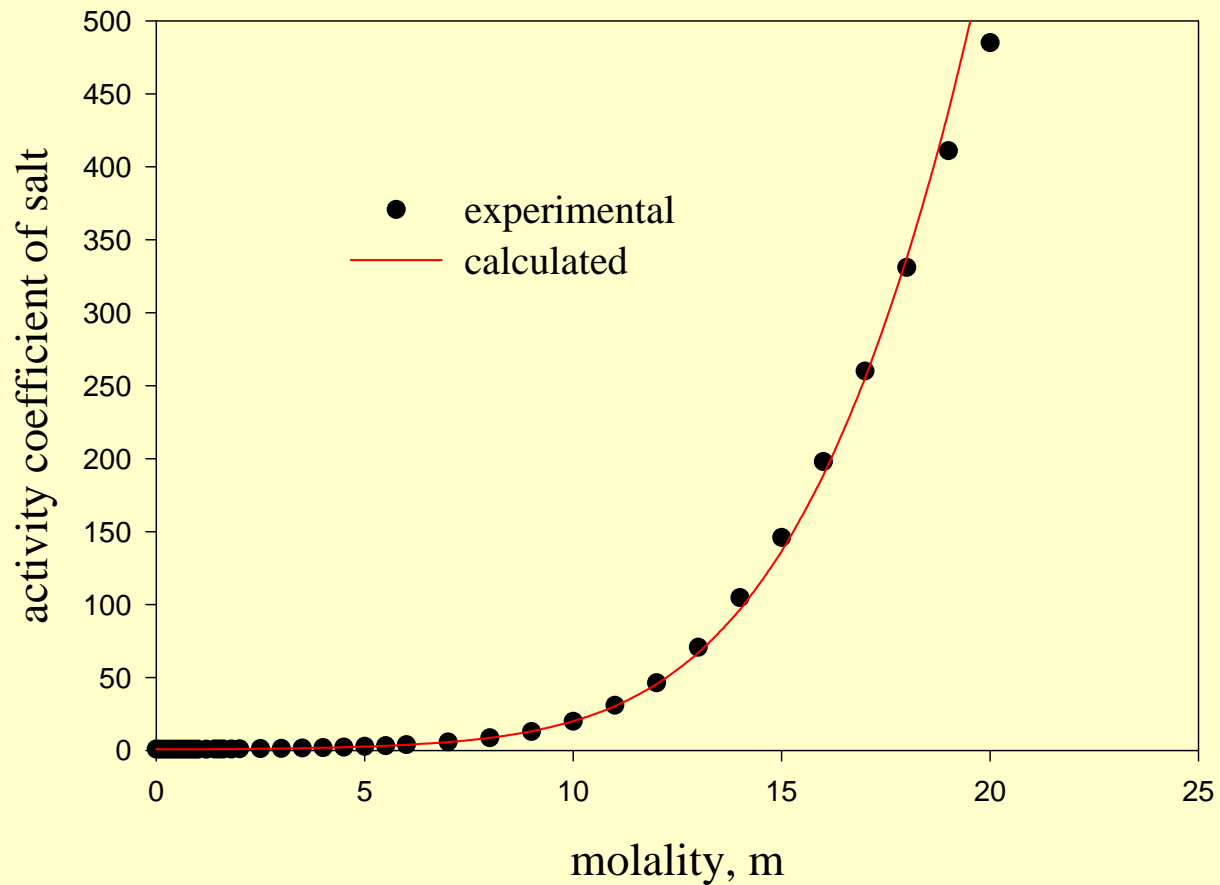


Fig.3 The activity coefficient of LiBr.

Results

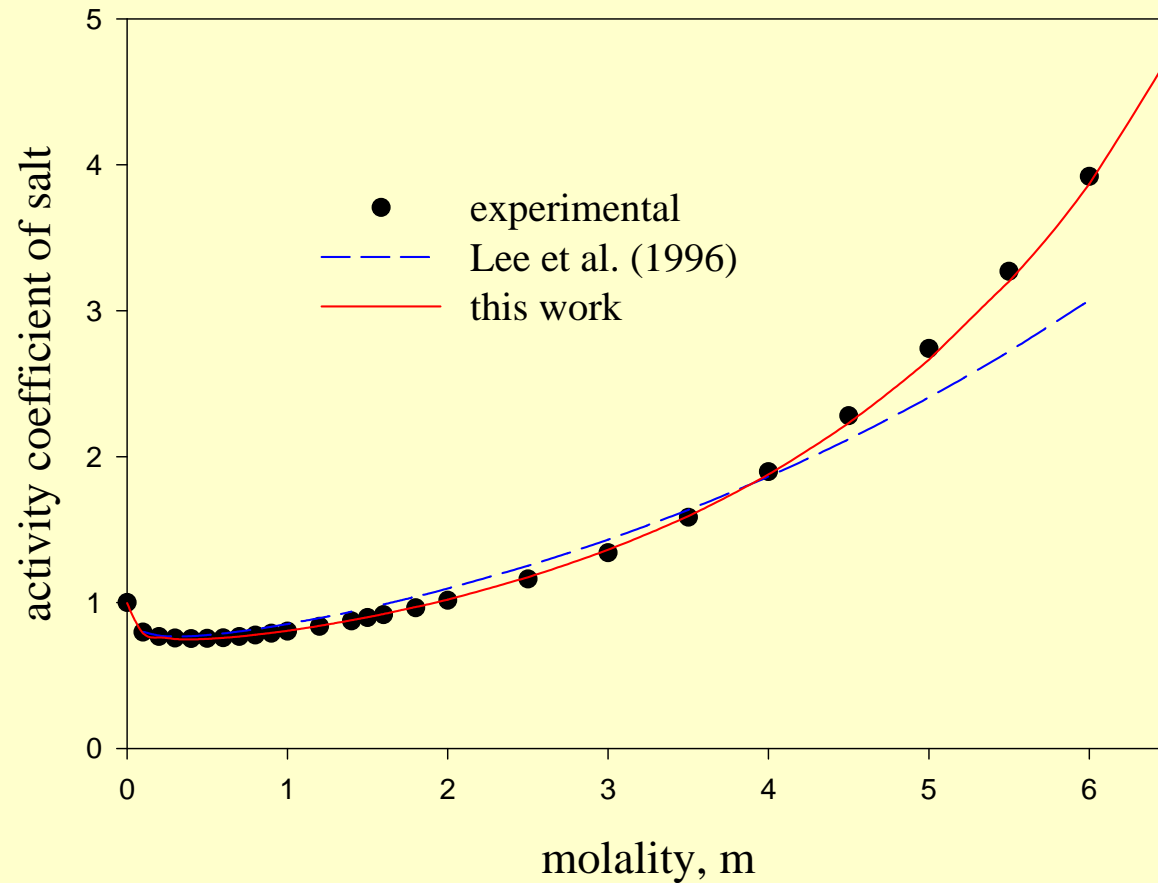


Fig.4 The activity coefficient of LiBr.

Results

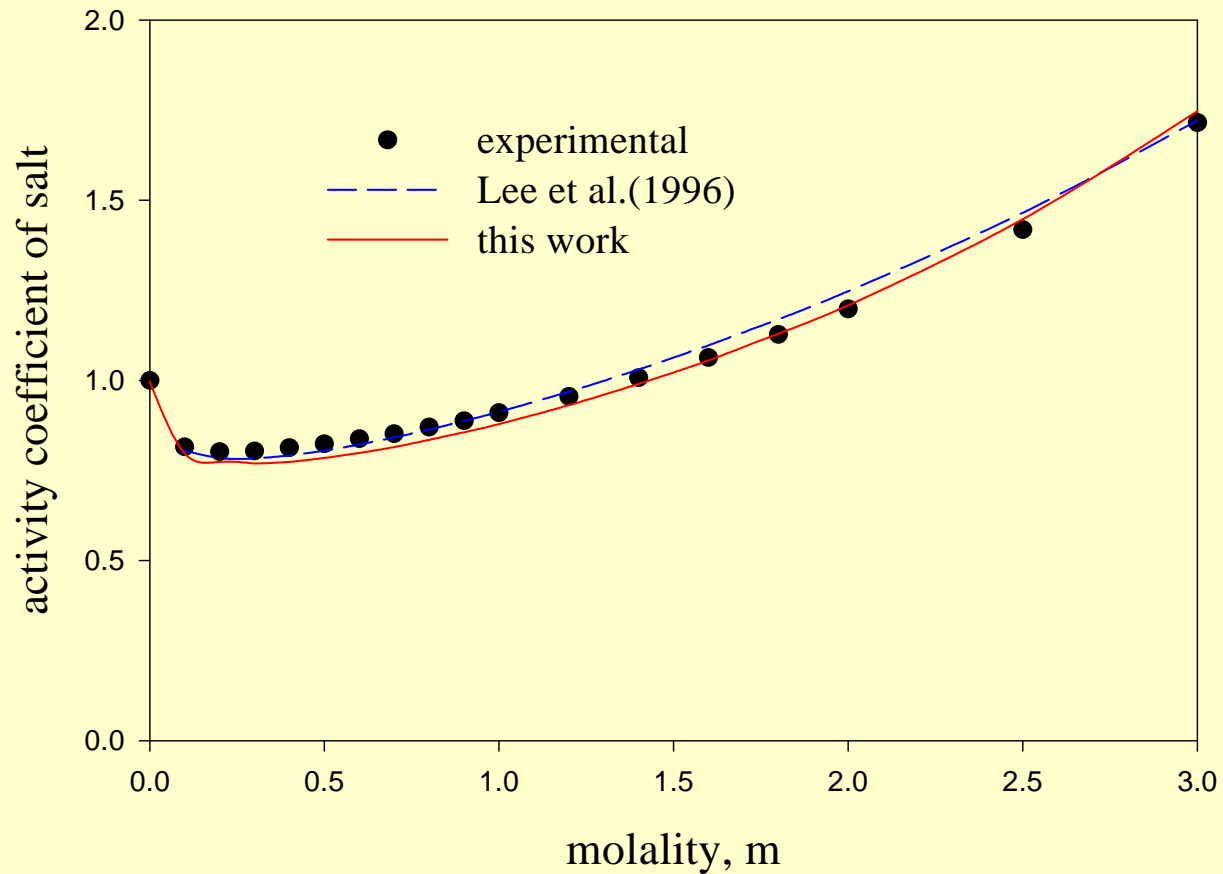


Fig.5 The activity coefficient of LiI.

Results

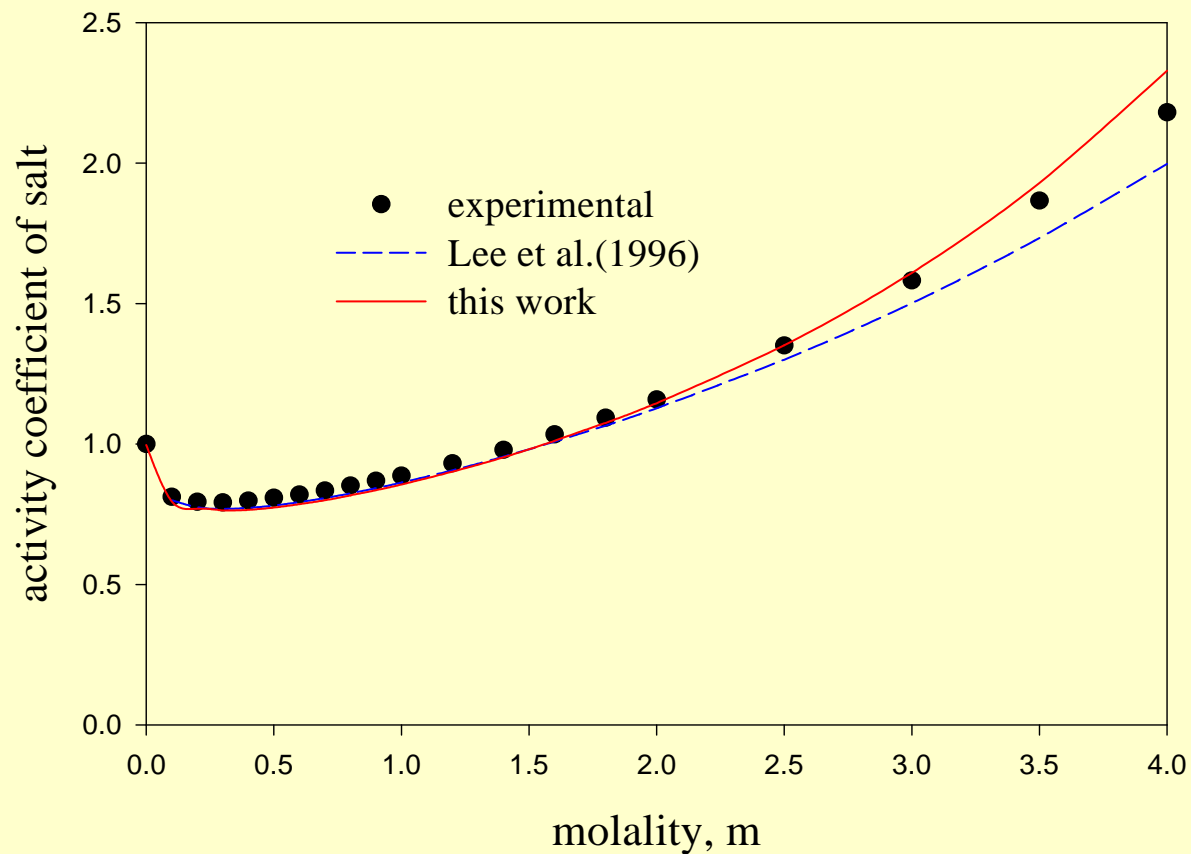


Fig.6 The activity coefficient of LiClO₄.

Conclusions

- Mass transfer mechanism in ammonia stripping process was analyzed for parallel and cross flow in shell side
- Measuring $\text{NH}_3\text{-H}_2\text{O-NaOH}$ VLE data with a modified static method, we estimated the Henry's constant of ammonia in aqueous solution.
 - ▶ Due to the presence of air and the uncertainty in the amount of water present in vapor phase, it is difficult to measure the equilibrium data.
- Mass transfer coefficients of ammonia removal were correlated with the Henry's constant, and compared with those of oxygen removal of Sengupta et al. (1998)
 - ▶ Fitted parameter a : dependent to the removed species.

Conclusions

- Lee et al. model was applied to the $\text{NH}_3\text{-H}_2\text{O-NaOH}$ VLE assuming ammonia to be a solvent species. The calculated results show similar trend with the experimental data.
- Lee et al. model also was applicable to the salt-mixed solvent VLE systems with only solvent parameters fitted from solvent-solvent VLE data.
- Lee et al. model was extended to the high concentrated electrolyte solutions, explicitly including solvation from a normalized Veytsman statistics. The fitted results give a good agreement with experimental activity coefficients of LiCl , LiBr , LiI and LiClO_4 up to 20 molal concentrations.