2. Phase Equilibria and crystallization technique

2.1 Phase rule

- Solubility product K_{sp}

Degree of freedom (F)
P + F = C + 2
where
P : number of phases
C : number of components

Ex) NaCl + water

Phase = 3 (solid, liquid, vapor) Component = 2 (NaCl, water)

F = 2 + 2 - 3 = 1

Transition point : NaCl, NaCl-2H₂O Phase = 4 (2 solids, liquid, vapor) Component = 2 (NaCl, water)

F=2+2-4=0

Addition of an extra-component = drowning-out

-Eutectic system (selective crystallization)

line BC : pure B-crystal + A/B mixture-liquid line AC : pure A-crystal + A/B mixture-liquid Pure separation is possible by single step of crystallization.

Ex) gold/thallium, naphthalene/benzene, m-/p-nitrochlorobenzene, KCl/H2O

- Compound and solid solutions (co-crystallization)

ex) NaCl/NaBr, naphthalene/beta-naphthol

Multi-step crystallization is required to purify a specified component.

2.3 The Driving force for crystallization

- Under-saturated
- Saturated
- Supersaturated = metastable, labile

- Supersaturation

$$\sigma = (\mu_{ss} - \mu_{eq})/kT$$

 $\mu_i = \mu^0 + kT lna_i$ (Gibbs-Duhem equation)

- Concentration driving force : $\Delta C = C_{\rm ss} - C_{\rm eq}$

2.4 Crystallization technique

- Suspension process

crystallization in solution depending on solubility change

ex) cooling crystallization

drowning-out crystallization evaporation crystallization salting-out crystallization reaction crystallization particulate materials :

crystal size, distribution, shape, structure, purity

- Solidification process

solidification of liquid phase below melting point

ex) melt crystallization

- purification by single step crystallization in eutectic system

- purification by multi-step crystallization (fractional crystallization)

spray drying (no purification)

- Continuous process commodity materials produced in high tonnage

ex) slat, paraxylene, ammonium nitrate, urea, adipic acid etc

- Batch-wise process specialty chemicals produced in low tonnage