8. Characteristics of continuous and batch crystallizers

8.1 Continuous MSMPR crystallizer

- What change of crystal size is expected if the mean residence time is varied? Assemble the characteristic equations representing some properties.

$$
L_D = 3G\tau
$$

$$
M_T = 6\rho_{cry}\alpha BG^3\tau^4
$$

$$
B = K_R M_T G^i
$$

where

$$
B = k_b M_T \Delta C^b
$$

$$
G = k_g \Delta C^g
$$

$$
K_R = k_b / k_g{}^i
$$

$$
i = b / g
$$

From assembly of above equations,

$$
\tau = \frac{\overline{L}_D}{3} \left[\frac{2\rho_{cry} \alpha K_R \overline{L}_D^4}{27} \right]^{1/(i-1)}
$$

That is,

$$
\tau \propto \overline{L}_D{}^{(i+3)/(i-1)} \qquad \text{if } i \neq 1
$$

$$
\overline{L}_D = \left[\frac{27}{2\rho_{cry}\alpha K_R} \right]^{1/4}
$$
 if $i = 1$

8.2 Size-dependent removal rates

Mean residence time of crystals depending on their size.

- Fine removal

Producing the same production rate with the fewer crystals of larger average size.

The mean residence time of fines (τ_F) and of the product (τ_P)

$$
\tau_F = \frac{v}{Q_F + Q_P} \qquad (L < L_F)
$$

$$
\tau_P = \frac{V}{Q_P} \tag{L>L_F}
$$

Then, the population density distribution of crystals

$$
n = n^0 \exp(-\frac{L}{G \tau_F}) \quad \text{for} \quad L < L_F
$$

$$
n = n^{0} \exp(-\frac{L_{F}}{G\tau_{F}}) \exp(-\frac{L}{G\tau_{P}})
$$
 for L> L_F if $L_{F} \ll \overline{L_{D}}$

Thereby, the effective birth rate can be defined as

$$
B_{\text{eff}} = G n^0 \exp(-\frac{L_F}{G \tau_F})
$$

As analogously in Eq. (8.1),

$$
\tau = \frac{f\overline{L}_D}{3} \left[\frac{2\rho_{cry}\alpha K_R \overline{L}_D{}^4}{27} \right]^{1/(i-1)}
$$

where

$$
f = \left[\exp\left[-\frac{3L_F \tau_P}{\overline{L}_D \tau_F} \right] \right]^{1/(i-1)}
$$

Typical parameter values for the fine removal system are $\tau_P / \tau_F = 10$, $L_F / L_D = 0.1$, $i = 3$, then $f = 0.22$

Advantage of the system

- greater operating flexibility

Disadvantage of the system

- greater encrustation on the crystallizer wall
- higher possibility of instability
- more energy cost for find dissolution

- Classified product removal

Case I

- smaller mean crystal size than one in normal crystallizer
- narrow crystal size distribution
- low number of crystals in product
- high population of small crystals in crystallizer
- low supersaturation level in crystallizer \rightarrow low growth rate *combining with fine removal system*

Case II

- larger mean crystal size than one in normal crystallizer
- wide crystal size distribution
- leading to unstable operating conditions.

8.3 Other factors influencing crystal size distribution

- Size-dependent growth rate

The small crystals have the lower growth rate than the large crystals.

$$
G = G_0[1 + \gamma L]^b \qquad \text{for } b < 1
$$

Dimensionless size, L/G0τ

- Agglomeration and breakage

In general, the agglomeration is occurring in the smaller size range whereas the breakage does in the larger size range.

Dimensionless size, $L/G^0\tau$

8.4 Dynamics and stability of continuous crystallizer

- unsteady state MSMPR crystallizer

$$
\frac{\partial n}{\partial t} + G \frac{\partial n}{\partial L} = -\frac{n}{\tau}
$$

Instability is originated from interaction between the inherent kinetics of crystallizing system and the residence time distribution function.

Typical cases of instability

- when the nucleation mechanism is changed from secondary to primary in either way.
- low frequency cycling combined with a fine removal system.

8.5 Batch crystallizer

- for low production rate of specialty, agro- and pharmaceutical chemicals
- simple and flexible system
- low capital investment
- multi-purpose process (reactor, crystallizer, mixer, blender handling many products)

Typical type of crystallization

- cooling crystallization
- evaporation crystallization
- drowning-out (salting-out) crystallization
- reaction crystallization

Operation variables

- batch time
- supersaturation rate
- addition of seed crystals
- agitation type and level
- feeding mode and rate etc.

- The mass balance

$$
\frac{dM}{dt} + \frac{dVc}{dt} = 0
$$

where M is the amount of crystals in suspension, V is the solution volume and c is the concentration of solute in solution.

(1) In cooling crystallization with assumption of c approximately equal to c_{eq} , the mass balance is rearranged as,

$$
\frac{dM}{dt} + V\left(\frac{dc_{eq}}{d\theta}\frac{d\theta}{dt}\right) = 0
$$

where

$$
\frac{dc_{eq}}{d\theta} = \text{slope of solubility curve}
$$

$$
\frac{d\theta}{dt} = \text{cooling rate}
$$

(2) In evaporation crystallization with assumption of c approximately equal to c_{eq} , the mass balance is rearranged as,

$$
\frac{dM}{dt} + c_{eq} \frac{dV}{dt} = 0
$$

where

$$
\frac{dV}{dt} = \text{evaporation rate}
$$

$$
\frac{L_p}{L_s} = \left[\frac{M_p}{M_s}\right]^{1/3}
$$

 L_s and L_p : crystals sizes of seed and product, respectively M_s and M_p : masses of seed and product, respectively

- Cooling crystallization

Natural cooling : constant temperature and constant flow rate of cooling water.

$$
\frac{\theta - \theta_0}{\theta_i - \theta_0} = \exp(-t/\tau_B)
$$

where θ_i and θ_0 are the initial and final temperatures, respectively, and τ_B is the batch time constant defined as,

$$
\tau_B = \frac{M_S C_P}{U A_B}
$$

where *U* is overall heat transfer coefficient, A_B is the heat transfer area, M_S is the mass of solution and C_P is the heat capacity of the solution.

Controlled cooling : for constant supersaturation

$$
\frac{\theta_i - \theta}{\theta_i - \theta_0} = (t/t_B)^4
$$
 for unseeded system

$$
\frac{\theta_i - \theta}{\theta_i - \theta_0} = (t/t_B)3
$$
 for seeded system

- Other crystallization method

Similarly, in evaporation crystallization the evaporation rate should be very low at the first of the batch and gradually increase as a greater crystal surface is developed.

Also, in drowning-out crystallization the anti-solvent should be slowly added and gradually increase in the course of the batch.

- The population balance for batch crystallization

$$
\frac{\partial n}{\partial t} + \frac{\partial nG}{\partial L} = 0
$$

Kinetic data are required to solve the balance equation.

- Practical operating factors in batch crystallization

Minimum stirring speed (*Njs*) to suspend the crystals of specific size *L*.

$$
N_{js} = S[v^{0.1}L^{0.2}X^{0.15}D^{-0.85}(g\Delta\rho/\rho_l)^{0.45}]
$$

 ν is the kinetic viscosity of the solution, *X* is the fraction of solid in the vessel, *D* is the stirrer diameter, *g* is the gravity, ρ_l is the liquid density and $\Delta \rho$ is the density difference between crystal and solution. *S* is the dimensionless constant depending on the vessel geometry.

9. Crystals in formulated products

9.1 Crystals as active products

Pharmaceutical drug of active ingredients :

$$
\frac{dm}{dt} = \frac{DA}{h}(c_{eq} - c)
$$

 where *dm/dt* is the dissolution rate, *D* is the diffusivity, *A* is the surface area, *h* is the diffusion layer thickness, and *ceq* and *c* are the solute concentration at equilibrium and bulk, respectively.

High dissolution

Slow dissolution

9.2 Crystals as property controllers

Margarine and chocolate : triglyceride crystal

Ice cream : water ice crystals

9.3 Crystals causing problems

Ostwald ripening : Crystal size increase, surface area decrease

Phase transformation : Ammonium nitrate

9.4 Crystallization controllers as products

Crystallization inhibitor to paraffins in middle distillate fuels: copolymer of ethylene and vinylacetate.

Scale inhibitor : organic phosphate and carboxylate