





고분자의 Rheological Property 측정방법

i) Rotational type viscometer 종류

- RMS (Rheometrics Mechanical Spectrometer)
- RDS (Rheometrics Dynamic Spectrometer)
- RSR (Rheometrics Stress Rheometer)
- ARES (Advanced Rheometric Expansion System)
- Weissenberg Rheogoniometer, etc

측정가능한 물성

- Steady shear viscosity (η_0, η)
- Synamic viscosity(η^*)
- Storage modulus (G')
- Loss modulus(G")
- First normal stress difference $\frac{1}{2}$

(a) dynamic test(η^*) –

oscillatory shear, using the cone&plate fixtures, is recommended for materials which are very strain sensitive (i.e, exhibit linear visco-elastic behavior only for small deformations) since the strain is essentially constant throughout the sample volume,

- oscillatory parrel plate measurements ;

useful for materials in approximately the same range of modulus, also preferred when making measurements over a wide range of temp, since the plate separation may be varied and the use of a relatively wide plate separation minimizes errors due to thermal expansion of the fixture, 주로 temp sweep 때 사용함

(b) steady shear test (η) –

the most widely used fixture if the cone&plate, which has the advantage that each volume element of fluid within the sample experiences the same shear rate – This is especially important for fluids which are shear thinning

- steady shear viscosity(η) 와 first normal stress difference 측정가능
- viscosity 측정시 사용하는 transducer 가 10 gr-cm이면 torque 는 1dyne/cm²
 까지 측정가능, 이것은 약 10sec⁻¹ shear rate 에서 점도 10 poise 에 해당됨.

- 예로서(단위환산); poise ≡ dyne·sec/cm² = g/cm·s 1 Pa·sec = 10 poise = 10g/cm·sec 1 Pa = 10g/cm·sec² = 10 (g·cm/sec²)(1/cm²) = 10(dyne/cm²)

참고로 dyne = g·cm/sec², N = kg·m/sec², Pa = N/m²

- steady shear can also be performed between parallel plates if a sample is to be tested at a variety of temp.
- when fluids are manipulated in processes of interest such as extrusion, fiber spinning, etc., they are almost invariably subjected to a shear field involving continuous deformation.
- For this reason, it is often desirable to examine the behavior of fluids in steady shear rather than oscillatory shear

P 499 Chap 16. Rheolocical Properties of Polymer solutions

A Dilute Polymer solutions

$$[\eta] = \lim(c \to 0) \frac{\eta_{sp}}{c}$$

p 512 The glass transition temperature of polymer solutions

$$T_g = \frac{T_{gp} + (KT_{gs} - T_{gp})\theta_s}{1 + (K - 1)\theta_s}$$

k : constant
$$\approx \frac{\alpha_{ls} - \alpha_{gs}}{\alpha_{lp} - \alpha_{gp}}$$

 α_l : volume coefficient of expansion above T_g

 α_{g} : volume coefficient of expansion below T_g

$$\frac{T_{gp} - T_g}{T_{gp} - T_{gs}} = \frac{1 - \phi_p}{1 - \phi_p (1 - \frac{1}{K})}$$
(16.24)

 ϕ_p : volume fraction of polymer

p 515 (Ex 16.2) Estimate the T_g for a solution of PS in benzyl alcohol with $\phi_p = 0.85$

(sol.) According to Fig. 16.5 at $\phi_p = 0.85$ and K=2.5 (from page 513, bottom)

$$\frac{T_{gp} - T_g}{T_{gp} - T_{gs}} = 0.29 \qquad (16.24)$$

PS 의 $T_g = 373K$ Benzyl alcohol 의 $T_g = T_m \circ = \neq = f$ estimation (From Table 16.2) $\frac{T_{gs}}{T_{ms}} = \frac{2}{3}$ $\therefore T_{gs} = 2/3 \times (258K) = 172K$ 식 (16.24) 에 대입, $T_{g.est} = 315K$, $T_{g.exp} = 324K$

- P 515 A new method for estimating the viscosity of concentrated polymer solutions
- P 516 (Ex 16.3) For concentrated solutions of polyisobutylene in decalin($\phi_p > 0.1$), estimate the viscosity as a function of the volume fraction of polymer at a temp of 20°C. The viscosity of the bulk polymer at this temp is $\eta_p = 6.5 \times 10^9 (N \cdot S / m^2)$

(sol) (1)
$$T_{g,p}=198K$$
, $T_{g,s}=2/3T_{m,s}=2/3(230K)=150K$
From K=2.5, $\frac{T_{gp}-T_g}{T_{gp}-T_{gs}}=\frac{1-\phi_p}{1-\phi_p+\frac{\phi_p}{K}}$ 로부터 T_g 를 계산할 수 있습

(2) 그림(15.4)와 $\eta_p / \eta_p (1.2T_g)$ vs Tg/T

PIB
$$\[Pi]$$
 A = 12.5 (P 469 Table)
 $\frac{T_g}{T} = \frac{198}{293} = 0.676$
 $\log(\eta_p * / \eta_p (1.2T_g)) = -3.5$
 $\log \eta *_p = 9.8, \quad \therefore \log \eta_p (1.2T_g) = 9.8 + 3.5 = 13.3$

(3) From Eq.(16.26)

$$\eta = \eta *_p$$
 at $\phi_p = 1.0$
 $\log \eta = \log \eta *_p + 5 \log \phi_p$ (16.26)
여기서 $\log \eta = 구할 수 있슴$ (see Table 16.3)
(η 의 unit 은 N·S/m²)

여기서 η = viscosity of diluted polymer η * = viscosity of undiluted polymer

Chap 17. Transport of Thermal Energy

- P 530 (Ex 17.1) Estimate the Heat conductivity of amorphous PMMA, (a) at room temp (b) at 200°C
 - (Sol) From Eq(17.4), with Cp= $1380(J/kg\cdot K)$

$$\frac{\lambda}{C_p \cdot \rho} = L(\frac{U_R}{V})^3 [\frac{3(1-\upsilon)}{1+\upsilon}]^{1/2}$$

여기서 λ : heat conductivity

Cp : specific heat capacity

- ρ : density
- L : distance between the molecules in "adjacent isothermal layers"
- U: velocity of elastic wave(sound velocity)

$$U_{\rm R} = V \cdot U_L^{1/3} [\frac{1+V}{3(1-V)}]^{1/6}$$
 (P. 443)

 \checkmark Molar Sound velocity function or Rao function

$$U_{\log} = \left(\frac{U_R}{V}\right)^3 \left(\frac{3(1-v)}{1+v}\right)^{1/2}$$
(17.3)

P 525 $\lambda \approx C_p \rho uL$ (17.2)

 λ : heat conductivity

$$U_{\text{long}} = \left(\frac{U_R}{V}\right)^3 \left[\frac{3(1-\nu)}{1+\nu}\right]^{1/2}$$
(7.3)

v: poisson ratio (p374) chap 13

- 먼저 chap 14 (p 447 Table 14.2) 로부터 Rao function 을 구한다.

So U_R / V =
$$\frac{U_R}{\frac{M}{\rho}} = \frac{4945}{101.1/1.17} = 5.8(m/s)$$

(U_R / V)³ = 1.97×10³ (m/sec)

P 531 According to eq.(17.4)

$$\frac{\lambda}{C_p \cdot \rho} = L(\frac{U_R}{V})^3 [\frac{3(1-\nu)}{1+\nu}]^{1/2}$$

=>
$$C_p = 1380(J/kg\cdot K)$$
 (From P.112)
 $\rho = 1170(Kg/m^3)$
 $L = 5 \times 10^{-11}$ (m) (From Table 17.1)
 $(U_R / V)^3 = 1.97 \times 10^3$ (m/sec)
 $\nu = 0.40$

:.
$$\lambda = 1380 \times 1170 \times 5 \times 10 - 11 \times 1.97 \times 103 \times 1.13 = 0.180(J/s \cdot m \cdot K)$$

P 527의 Table 17.1과 비교
 $\lambda_{exp} = 0.193 (J/s \cdot m \cdot K)$

(b) at 200°C

먼저 25°C에서, T/T_g = 298/387 = 0.77 from fig. 17.2 λ (T)/ λ (T_g) = 0.96 λ (T_g) = $\frac{1}{0.96}$ (0.180) = 0.188

p 531 at
$$T = 200 + 273 = 473K$$

 $\frac{T}{T_g} = \frac{473}{387} = 1.22$
From Fig 17.2
 $\frac{\lambda(473)}{\lambda(T_g)} = 0.95$
 $\therefore \lambda(473) = 0.188(0.95) = 0.178(J/s \cdot m \cdot K)$

P 532 (Ex 17.2)
Calculate the
$$\lambda$$
 of PET at 40% crystallinity
 $\Rightarrow \lambda$ (at roomp) = 0.218 ($J/s \cdot m \cdot K$)
(Sol.) $\rho_c = 1.465$, $\rho_a = 1..335$
Eq.(17.7) $\notearget \notearget$
 $\frac{\lambda_c}{\lambda} - 1 = 5.8(\frac{\rho_c}{\rho_a} - 1)$
 $\lambda_c = 0.218(1 + 5.8(\frac{1.465}{1.335} - 1)) = 0.218 \times 1.56 = 0.340$
 $earget \notearget$
 $earget \notearget$
(see Fig.17.4 in P.531)
 $\frac{\lambda - \lambda_a}{\lambda_c - \lambda_a} \approx 0.36$ or (From P.531 Fig 17.4)

$$\frac{\lambda - 0.218}{0.340 - 0.218} = 0.36$$
$$\lambda = 0.044 + 0.218 = 0.262 \quad (J/s \cdot m \cdot K)$$
$$\lambda_{exp} = 0.272 \quad (J/s \cdot m \cdot K)$$

Chap.18

Properties Determining Mass Transfer in Polymeric Systems

A. Permeation of simple Gases.

P: (permeability)

S: (solubility)

D : (diffusivity)

 $P = S \times D$

- P 536 permeation is a sequential process, starting with solution of the gas on the outer surface of the polymer, followed by slow inward diffusion
- P 542 Ex 18.1) Estimate the solubility and the heat of solution (sorption) of oxygen in PET, both in the quenched amorphous glassy state and semi-crystalline state ($X_c = 0.45$).

Sol) i) $T_g(PET) = 345K$, For O_2 , $\epsilon/k=107$ From Eq.(18.7b) ϵ (potential energy constant) k(Boltzman const.) $\log S(298) = -7.4 + 0.010\epsilon/k \pm 0.6$ $= -6.33 \pm 0.6$ $\therefore S = 5.6 \times 10^{-7}$ $S_{Exp} = 9.9 \times 10^{-7}$

ii) For semicrystalline state ;

$$\begin{split} S_{sc}(298) &= S_a(298)(1\text{-}X_c) \\ &= 5.6 \times 10^{-7}(0.55) = 3.1 \times 10^{-7} \\ S_{sc}(\text{Exp}) &= 7.4 \times 10^{-7} \end{split}$$

- P 552 (Ex 18.2) Estimate the diffusivity at 298K and the activation energy of diffusion for oxygen in PET, both in the glassy and in the semicrystalline state.
 - (sol.) For the derivation of E_D (activation energy of diffusion) we use Fig. 18.3 $T_g = 345K$, $P = 6.75 \pm 1.5$

(from Eq.18.12b p 552)

 $\frac{E_D}{R} \cdot 10^{-3} = (\frac{6O_2}{6N_2})^2 \cdot P = (\frac{347}{38})^2 \cdot (6.75 \pm 1.5) = 0.83(6.75 \pm 1.5) = 5.6 \pm 1.25 \text{ (KJ/mol)}$ 10⁻³ × E_D = {(8.3)5.6 ± (8.3)1.25} = 46.5 ± 10.5 \text{ (KJ/mol)} E_{D,Exp} = 46.1 ~ 48.5

From Eq.(18.13b) (p.552) $\log D_0 = 10^{-3} E_D / R - 5.0 \pm 0.8 = 0.6 \pm 0.8$

From Eq(18.15) log D(298) = log D₀ - $1.46 \times 10^{-3} E_D/R = 7.6 \pm 0.8$ \therefore D_a(298) = 2.5×10^{-8} (cm²/sec) P 560 Ex 18.3 Estimate the permeability P(298) for oxygen of two polymer films : one a neoprene rubber film and the other a PVC film.

P 571 Ex 18.4 Estimate the moisture content of nylon-6 at 25°C and a relative humidity of 0.7. The crystallinity is 70%.

 $\begin{array}{ll} P \ 581 & \text{Ex 18.5} & \text{Estimate the rate of dissolution of PS in toluene at } 35^{\circ}\text{C}(308\text{K}) \\ (a) \ at \ a \ very \ low \ Reynolds \ number \ (N_{Re} \approx 0 \) \\ (b) \ at \ a \ Reynolds \ number \ of \ 100D \\ PS(M_w) = 150000 \quad , \quad D = toluene \ in \ PS \ at \ 35^{\circ}\text{C} \ is \ 1.5 \times 10^{-6} \\ \end{array}$

Chap. 19 Crystallization and Recrystallization

A1. Crystallinity :

- the change from a random liquid structure to a well ordered, periodic crystalline structure can occur, this transformation is called crystallization : the reverse is called melting.
- Many polymeric solids consistlargely of folded chain lamellae.

A₂. Nucleation and Growth.

P 586 - the theory is based on the assumption that in supercooled melts there occur fluctuations leading to the formation of a new phase.
 The phase transformation begins with the appearance of a number of very small particles of the new phase (nucleation)

(Ex 19.1) Estimate for isotactic PS.

- a. the temperature of maximum crystallization velocity
- b. the linear growth rate at this temp.
- c. the probable(maximum) degree of crystallization
- a) Two methods of estimation are available
 - : eq(19.8) and Fig(19.6b)

i) From eq(19.8)

$$T_k \cong 0.5 (T_m + T_g)$$

= 0.5 (513 + 373) = 443 K

- ii) using Fig(19.6b) with $T_g/T_m = 373/513 = 0.7$
 - $rightarrow [7] \lambda = 0.86$, so $T_{x,max} = 441 \text{K}$, $T_{exp} = 449 \text{ K}$

b) applying Eq(19.16), with $T=T_{x,max}=442K$

i)
$$\log \frac{v}{v_0} \approx -2.3 \frac{T_m}{T} \left\{ \frac{T_m}{T_m - T_g} + \frac{50}{T_m - T} \right\}$$
 (19.16)
 $\approx 7 \lambda^2 \quad v_0 = 10^{12} \text{ (nm/sec)}$ (universal const. For crystalline polymer)

P 661
$$\log v = 12 - 2.3 \frac{513}{442} \left(\frac{513}{513 - 373} + \frac{50}{71} \right) = 12 - 4.7 = 0.3$$
, $v_{\text{max}} = 2.0$

ii) From Fig 19.6-a, $T_g/T_m = 0.725$ 그림으로부터 $\log v_{max} = 0.5$ the average $\log v_{max} = \frac{0.3 + 0.5}{2} = 0.4$

:.
$$v_{\text{max}} = 10^{0.4} = 2.5 (\text{nm/sec})$$
, $v_{\text{max,exp}} = 4.2 (\text{nm/sec})$

c) Maximum degree of crystallinity; Applying Fig 19.6c, $T_g/T_m = 0.725$ { Xc,max = 0.3 , Xc,max,exp = 0.34 } in good agreement.