

## Chapter 4. Volumetric Properties

A. The volumetric properties are extremely important for nearly every phenomenon or process

- (1) Specific volume, molar volumes, densities in the glassy, rubbery, and crystalline state,
- (2) Specific and molar thermal expansivities
- (3) Specific and molar melt expansion for crystalline polymer.

- 위의 properties 들을 additive group contribution 법  
법을 이용하여 구할 수 있음

◦ Methods for expressing the additivity within structural units

- (1) use of “atomic” contributions
- (2) use of “group” contribution
- (3) use of “bond” contribution

$$◦ \text{density} = \frac{\text{molar mass}}{\text{molar volume}} = \frac{M}{V} \frac{(\text{g/mol})}{(\text{cm}^3/\text{mol})} = (\text{g/cm}^3)$$

◦ Van der Waals volume ( $V_w$ ) – defined as the space occupied by this molecule, and the Van der Waals volume is given by eq(4.1) (p. 73)  
(see Table 4.2 for  $V_w$ )

$$◦ V_c (0K) = V^\circ(0) \approx 1.30V_w \quad (4.2)$$

→ zero point molar volume

→ zero point volume at crystalline state

B. Standard molar volumes at room temp (298K)

(1) Table 4.2 Van der Waals volume을 나타냄

◦ Table 4.2A에는  $V^\circ (0)$ 에 대한 atomic and structural constants

를 나타냄

- Table 4.3에는  $\text{CH}_2$ 에 대한 molar volume을 나타냄
- Table 4.4에는 room temp.에서 organic liquid의 molar volume의 group contribution을 나타냄
- Table 4.5에는 25°C에서 amorphous polymer (무정형 고분자), (rubbery state)에 대한 molar volume을 나타냄.

$$V_r(298\text{K}) = \sum_i V_i(298k) \quad (4.3b)$$

- Table 4.4의 값을 이용하여 rubbery amorphous polymer의 molar volume의 값을 Table 4.5에 나타내었다.

$$V_r/V_w = 1.6 \pm 0.035 \text{ (cm}^3/\text{mol)} \quad (\text{p.81 figure 4.1참조})$$

- Molar volume of glassy amorphous polymer
  - 이 경우는  $T_g$  (유리전이온도 : glassy transition temperature)가 상온(25°C)보다 높은 고분자인 경우임  
Table 4.6에 glassy amorphous polymer의 molar volume을 나타내었음  $V_g/V_w = 1.6 \pm 0.045 \text{ (cm}^3/\text{mol)}$
- Molar volume of crystalline polymer at 25°C

- Table 4.7에 fully crystalline polymer의 molar volume을 나타내었다.

$$V_c(298\text{K})/V_w = 1.435 \pm 0.045 \text{ (cm}^3/\text{mol)}$$

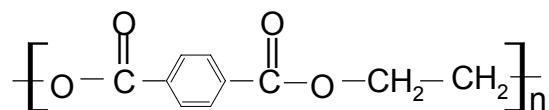
- Molar volume of semi crystalline polymers

$$V_{sc} = x_c V_c + (1-x_c) V_a$$

여기서  $x_c$  = degree of crystallinity

Table 4.8에서  $\rho_c/\rho \approx 1.13$

(ex 4.1) Estimate the densities of amorphous & crystalline PET(poly ethylene terephthalate))



에서

$M=192.2(\text{g/mol})$ , 상온에서 amorphous PET는 glassy state 이므로 (이유는 PET의  $T_g$ 가 약  $70^\circ\text{C}$ ),

Table 4.9에서

Group	$V_g(298\text{K})$	$V_c(298\text{K})$
	65.5 ( $\text{cm}^3/\text{mol}$ )	59.0
$-\text{COO}-$	$2 \times 23 = 46$	$221.5 = 43$
$-\text{CH}_2-$	$2 \times 16.37 = 32.7$ 144.2	$2 \times 14.68 = 29.4$ 131.4

$$\rho_g(298\text{K}) = \frac{M}{V} \frac{(\text{g/mol})}{(\text{cm}^3/\text{mol})} = \frac{192.2}{144.2} = 1.33 \text{ (g/cm}^3)$$

실험치는  $1.33 \text{ (g/cm}^3)$

$$\rho_c(298\text{K}) = \frac{192.2}{131.4} = 1.47 \text{ (g/cm}^3)$$

실험치는  $1.48 \text{ (g/cm}^3)$

### C. Thermal Expansion

1. The Specific thermal expansivity

$$\left( \frac{\partial v}{\partial T} \right)_p \equiv e \quad (\text{cm}^3/\text{g}\cdot\text{K})$$

2. The coefficient of thermal expansion

$$\frac{1}{v} \left( \frac{\partial v}{\partial T} \right)_p \equiv \alpha \quad (\text{K}^{-1})$$

3. The linear coefficient of thermal expansion

$$\frac{1}{L} \left( \frac{\partial L}{\partial T} \right)_p \equiv \beta \quad (\text{K}^{-1})$$

4. The molar thermal expansivity

$$\left(\frac{\partial V}{\partial T}\right)_p \equiv E \quad (\text{cm}^3/\text{mol}\cdot\text{K})$$

- Inferences from the thermal expansion model

### 1. Numerical values of the molar thermal expansivities

$$E_l = \frac{V_l(T) - V_l(0)}{T} = \frac{V_l(298) - V_c(0)}{298} \approx \frac{V_r(298) - V_c(0)}{298} = E_r \quad (4.12)$$

$$E_g = \frac{V_g(T) - V_g(0)}{T} \approx \frac{V_c(T) - V_c(0)}{T} = \frac{V_c(298) - V_c(0)}{298} = E_c \quad (4.13)$$

### 2. The excess volume of the glassy state

$\Delta V_g = V_g(T) - V_c(T)$  : the difference in molar volume of the two solid states of the polymer.

See Table 4.11 (p.92)

$$V_r(T) = V_l(T) = V_r(298) + E_l(T-298)$$

$$V_g(T) = V_g(298) + E_g(T-298) = V_g(298) + E_c(T-298)$$

$$V_c(T) = V_c(298) + E_c(T-298)$$

$E_c$ : molar thermal expansivity

(Ex 4.2) Estimate the expansion coefficient of the PET melt and its density at the extrusion temperature of 277°C(550K)

(sol) From eq(4.6)

$$e_l = E_l/M \quad e_g = E_g/M \quad \text{에서}$$

From eq(4.14) and (4.15) molar thermal expansivity는

$$E_g = E_c = 0.4510 \times 3V_w \quad (\text{Table 4.11}) \\ = 0.45 \times 10^{-3} \times 94.18 = 4.2 \times 10^{-2}$$

$$E_l = 10 \times 10^{-4} \times 94.18 = 9.4 \times 10^{-2}$$

$$T_g(\text{PET}) = 343\text{K}$$

$$\begin{aligned} V_l(550) &= V_g(298) + E_g(T_g - 298) + E_l(550 - T_g) \\ &= 143.2 + 4.2 \times 10^{-2}(343 - 298) + 9.4 \times 10^{-2}(550 - 343) = \end{aligned}$$

$$164.3$$

$$\therefore \rho_l(550) = M/V_l = 192.2 / 164.4 = 1.17 \text{ (g/cm}^3)$$

- experimental value = 1.16 g/cm<sup>3</sup>(excellent agreement)

\* specific thermal expansivity

$$- e_l = 9.4 \times 10^{-2} / 192.2 = 4.9 \times 10^{-4} (\text{cm}^3/\text{g}\cdot\text{K})$$

$$e_g = 4.2 \times 10^{-2} / 192.2 = 2.2 \times 10^{-4} (\text{cm}^3/\text{g}\cdot\text{K})$$

(excellent agreement with the exp value)

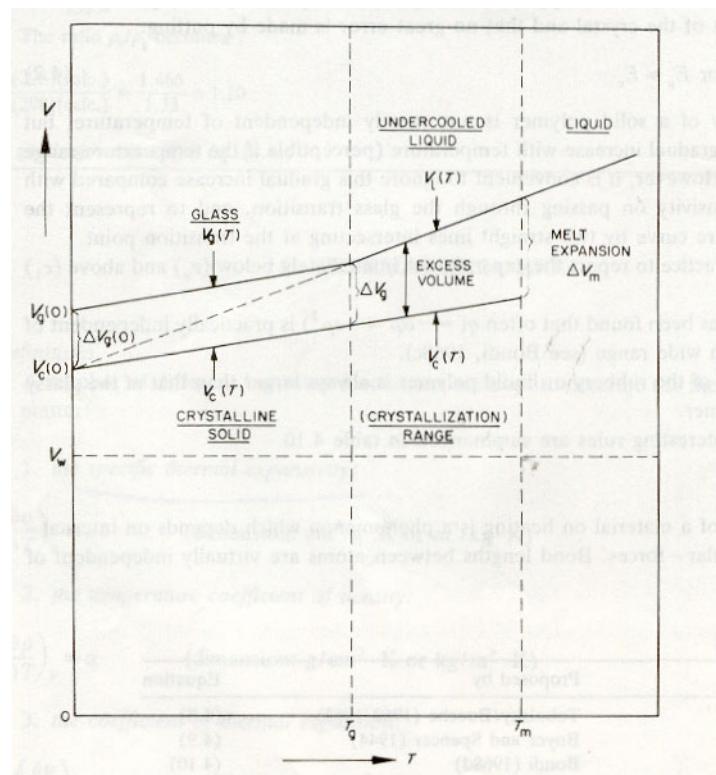


Fig 4.2 Thermal expansion model of polymers (based on a concept of Simha and Boyer)

$$V_r(T) = V_l(T) = V_r(298) + E_l(T - 298)$$

$$V_g(T) = V_g(298) + E_g(T - 298) = V_g(298) + E_c(T - 298) \quad (4.26)$$

$$V_c(T) = V_c(298) + E_c(T-298)$$

\* Melt density of Polycarbonate at 250°C ?

- The formula for molar volume at (273+250=523K) is

$$V_l(523) = V_g(298) + E_g(T_g-298) + E_l(523-T_g)$$

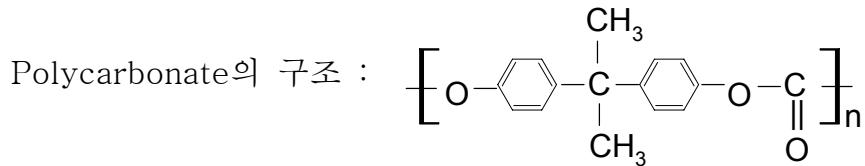
Where

·  $V_l$  is molar volume of the liquid ( $\text{cm}^3/\text{mol}$ )

·  $V_g$  is the molar volume of glassy polymer at 25°C (see Table 4.5)

·  $E_g$  is the molar thermal expansivity ( $\text{cm}^3/\text{g}\cdot\text{K}$ ) in the glassy state

·  $E_l$  is the molar thermal expansivity in the liquid state ( $\text{cm}^3/\text{g}\cdot\text{K}$ )



$$\text{여기서 } V_g(298) = M_{pc} / \rho_{pc} = 254.3/1.20 = 211.92(\text{cm}^3/\text{mol})$$

polycarbonate의

$$E_g = 613 \times 10^{-4} (\text{cm}^3/\text{mol}\cdot\text{K}) \quad (\text{see p.94})$$

$$E_l = 1362 \times 10^{-4} (\text{cm}^3/\text{mol}\cdot\text{K}) \quad (\text{see p.94})$$

$$T_g = 148 + 273 = 421\text{K}$$

$$\begin{aligned} \therefore V_l(523) &= V_g(298) + E_g(T_g-298) + E_l(523-T_g) \\ &= 211.92(\text{cm}^3/\text{mol}) + 613 \times 10^{-4}(421-298) \\ &\quad + 1362 \times 10^{-4}(523-421) (\text{cm}^3/\text{mol}) \\ &= 233.35 (\text{cm}^3/\text{mol}) \end{aligned}$$

$$\begin{aligned} \therefore \rho(523\text{K}) &= M_{pc}/V_l(523) = 1.089(\text{g/cm}^3) \\ M_{pc} &= 254.3(\text{g/mol}) \end{aligned}$$

◦ Melt densities of literature and calculated value\*

\* Kim and Burns, Polym.Eng.Sci., 28, 1115(1988)

Polymers	Densities <sup>a</sup>	Melt Densities (g/cm <sup>3</sup> ) <sup>b</sup>
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		Literature	Calculated <sup>c</sup>
PC	1.200	1.080 <sup>d</sup>	1.089
PS	1.050	0.950 <sup>e</sup>	0.941
SAN	1.078	-	0.973
PBT	1.389	-	1.200

a Densities at 25°C (g/cm<sup>3</sup>)

b Densities at 25°C

c Estimated from Van Drevelen (1980)

d Z. Dobkowski, Polimery(Warsaw), 25, 110 (1978)

e Chee and Rudin (1973)

(Ex) 170°C에서 polypropylene의 melt density?

(hint) PP의 T<sub>g</sub>는 약 -10°C(263K)

$$\begin{aligned}
 (\text{sol}) V_l(273+170) &= V_r(298) + E_l(443-298) \\
 &= 49.5(\text{cm}^3/\text{mol}) + 314 \times 10^{-4}(443-298) \\
 &= 54.05 \text{ (cm}^3/\text{mol})
 \end{aligned}$$

$$\therefore \rho(443\text{K}) = M/V_l = 42.1 / 54.05 = 0.779 \text{ (g/cm}^3)$$