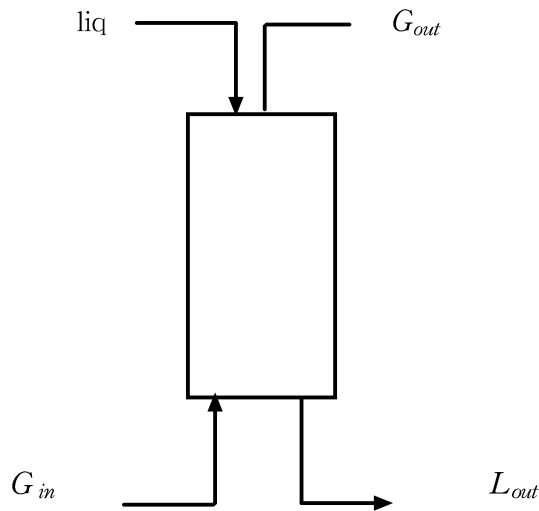


3. Mass Balances for continuous contact towers

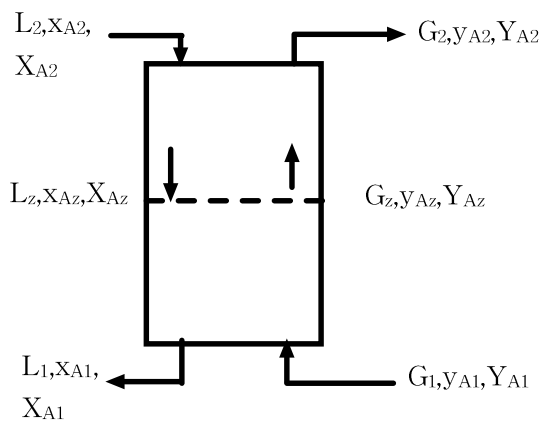
- Operating line equation
- Continuous contact towers



- Mass & enthalpy balance : conservation of mass & energy
- Interphase equilibrium
- Mass transfer equation(flow)
- Momentum transfer equation

(1) Countercurrent flow

- steady-state mass-transfer operation
- two immiscible phases
- 정의



- Balance equation(tower기준)

moles of A entering the tower = moles of A leaving the tower

- total (1-2) : $G_1 y_{A1} + L_z x_{A,2} = G_2 y_{A,2} + L_1 x_{A1}$
- local ($z=z$) : $G_1 y_{A1} + L_z x_{A,z} = G_2 y_{A,z} + L_1 x_{A1}$

- Solute-free units

$$Y_A = \frac{y_A}{1 - y_A} : \text{moles of A in G per mole of A free G}$$

$$X_A = \frac{x_A}{1 - x_A} : \text{moles of A in L per mole of A free L}$$

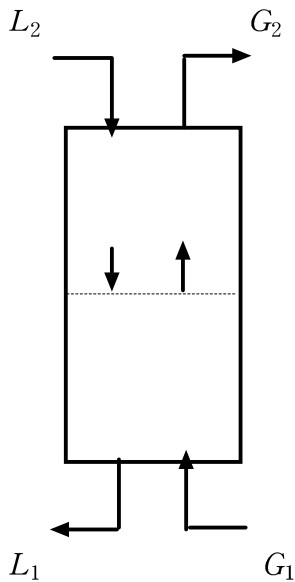
L_s : moles of phase L on solute free basis

G_s : moles of phase G on solute free basis

$$G_s Y_{A_1} + L_s X_{A_2} = G_s Y_{A_2} + L_s X_{A_1} \quad \text{or} \quad G_s (Y_{A_1} - Y_{A_2}) = L_s (X_{A_1} - X_{A_2})$$

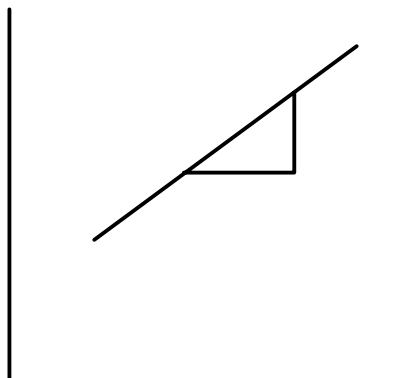
$$\text{at } z=z, \quad \frac{L_s}{G_s} = \frac{Y_{A_1} - Y_{A,z}}{X_{A_1} - Y_{A,z}} : \text{slope (operating line)}$$

- Countercurrent mass exchange

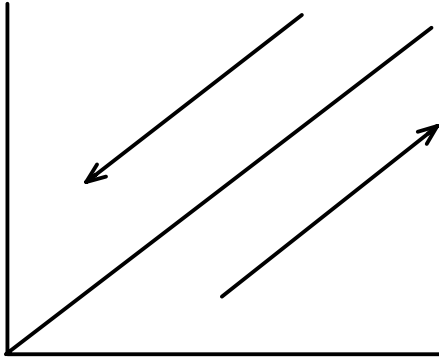


- solute-free basis (mixture 중에서 solute 양을 제거한 양)
- mass balance를 세우면 (for $z=z$)

$$\frac{L_s}{G_s} = \frac{Y_{A_1} - Y_{A,z}}{X_{A_1} - Y_{A,z}}$$



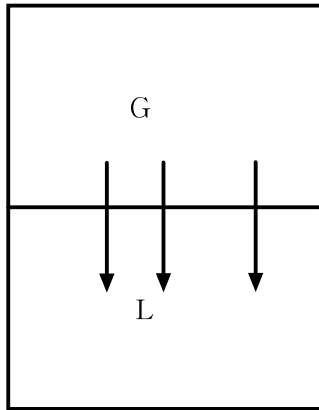
slope from (X_{A_1}, Y_{A_1}) through (X_{A_z}, Y_{A_z})



거리를 짧게 생각하면

$$L_s dX_A = G_s dY_A \text{ for } dz :$$

moles transfer from one phase to 2nd phase per hour cross-sectional area in dz



solute-free basis

G_s, L_s 양이 없으므로 이동변화량 없다

$$G = G_s + (\text{solute의 양})$$

$$L = L_s + (\text{solute의 양})$$

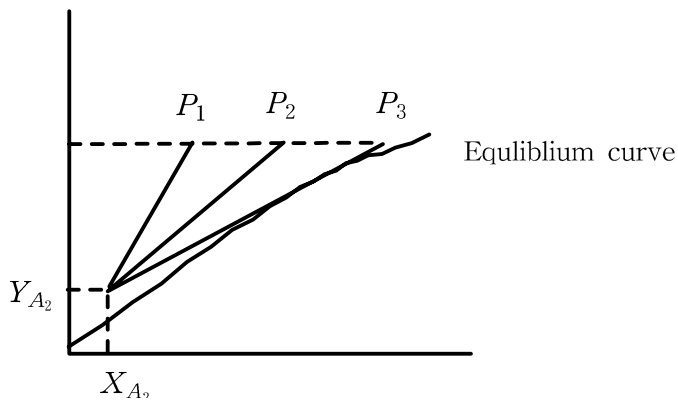
$$L : G_1 y_{A_1} + L_z x_{A_z} = G_z y_{A_1} + L_1 x_{A_1}$$

$$L_s : G_s (Y_{A_1} - Y_{A,z}) = L_s (X_{A_1} - X_{A,z})$$

$$\frac{L_s}{G_s} = \text{slope (linear profile): operating line}$$

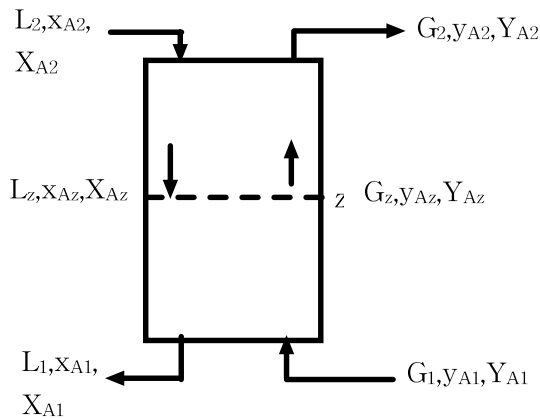
ex) Given one -phase-flow rate

3 of 4 entering & existing composition



$Y_{A_1} \rightarrow Y_{A_2}$ 로 목표치에 해당하는 물질전달이 수행된다 (1st \rightarrow 2nd)

4. Enthalpy balance



온도가 다른 물질 유입 유출되는 경우
(물질의 비열) × (온도차) = 열에너지

엔탈피 수지식 : $L_2 H_{L_2} + G H_G = G_2 H_{G_2} + L H_L$

normal enthalpy 식: $H_L = c_{pL}(T_L - T_O)M_{avg} + \Delta H_S$

같은 기준온도와 표준상태의 용질에 대한 기체의 몰 엔탈피는

$$H_G = [y_{solute} c_{p, G\ solute} M_{solute} + (1 - y_{solute})(c_{p, G\ solute-free\ G-phase} (M_{solute-free\ G-phase}))](T_G - T_O) + y_{solute} h_{f-g\ solute} M_{solute}$$

5. Mass transfer capacity coefficient

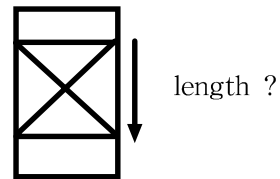
개별 물질전달계수: k_G

$$N_A = k_G(p_{A,G} - p_{A,i}) \quad \text{individual}$$

$$N_A = K_G(p_{A,G} - p_A^*) \quad \text{overall}$$

$$N_A \left[\frac{\text{moles of A transferred}}{(\text{hr})(\text{interfacial area})} \right] \left[a \left(\frac{\text{interfacial area}}{\text{ft}^3} \right) \right] dz (\text{ft})$$

$$= \frac{\text{moles of A transferred}}{(\text{hr})(\text{cross-sectional area})}$$



$$N_A a dz = k_G a (p_{A,G} - p_{A,i}) dz \quad k_G a : \text{individual capacity coefficient}$$

$$N_A a dz = K_G a (p_{A,G} - p_A^*) dz \quad K_G a : \text{overall capacity coefficient}$$

$$\Rightarrow k_G a, K_G a \frac{\text{moles of A transferred}}{(\text{hr})(\text{volume}) \times (\text{pressure})}$$

$$N_A a dz = k_L a (c_{A,i} - c_{A,L}) dz$$

$$N_A a dz = K_L a (c_A^* - c_{A,L}) dz$$

$$\Rightarrow k_L a, K_L a : \frac{\text{moles of A}}{(\text{hr})(V) \times (\text{mole}/V)}$$